

# $X(3872)$ , $T_{cc}$ , and heavy meson interactions





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2022, Oct. 1st

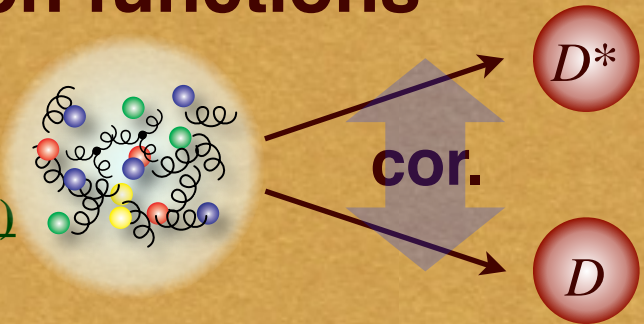
# Contents


 Introduction —  $T_{cc}$  and  $X(3872)$

  $DD^*$ ,  $D\bar{D}^*$  momentum correlation functions

- Hadron molecule picture

[Y. Kamiya, T. Hyodo, A. Ohnishi, EPJA58, 131 \(2022\)](#)



 Mixture of compact quark states

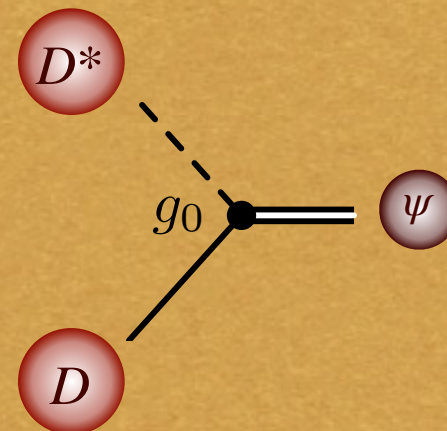
-  $DD^*$ ,  $D\bar{D}^*$  potentials

[I. Terashima, T. Hyodo, in preparation](#)

- Compositeness

[T. Kinugawa, T. Hyodo, in preparation](#)

 Summary

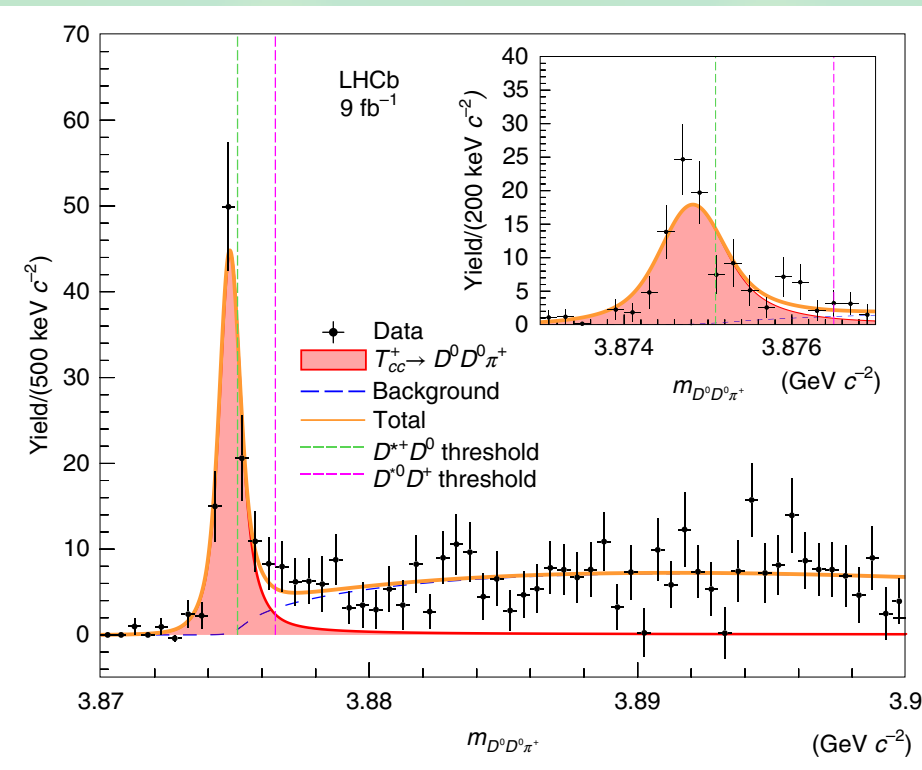
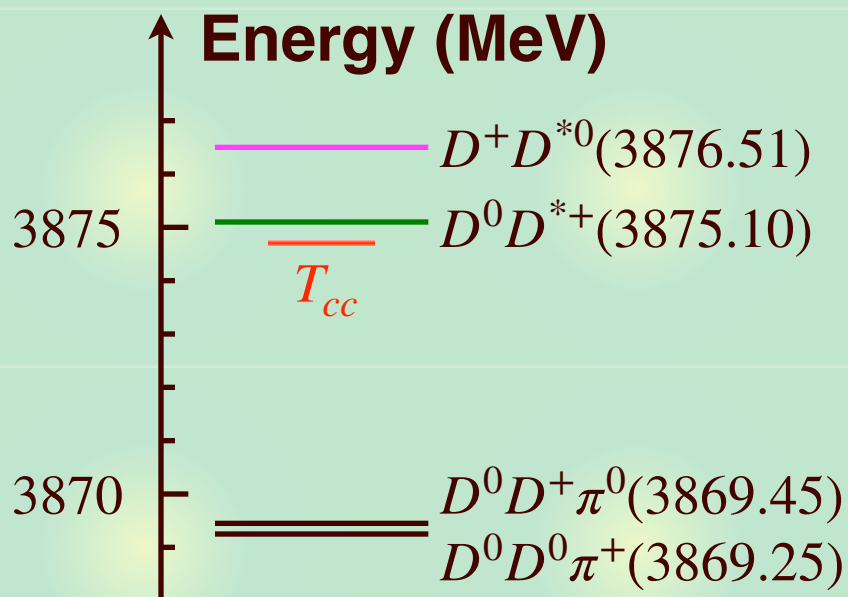


# Observation of $T_{cc}$

$T_{cc}$  observed in  $D^0 D^0 \pi^+$  spectrum

LHCb collaboration, *Nature Phys.*, **18**, 751 (2022); *Nature Comm.*, **13**, 3351 (2022)

- Signal near  $DD^*$  threshold
- Charm  $C = +2$  :  $\sim cc\bar{u}\bar{d}$
- Level structure

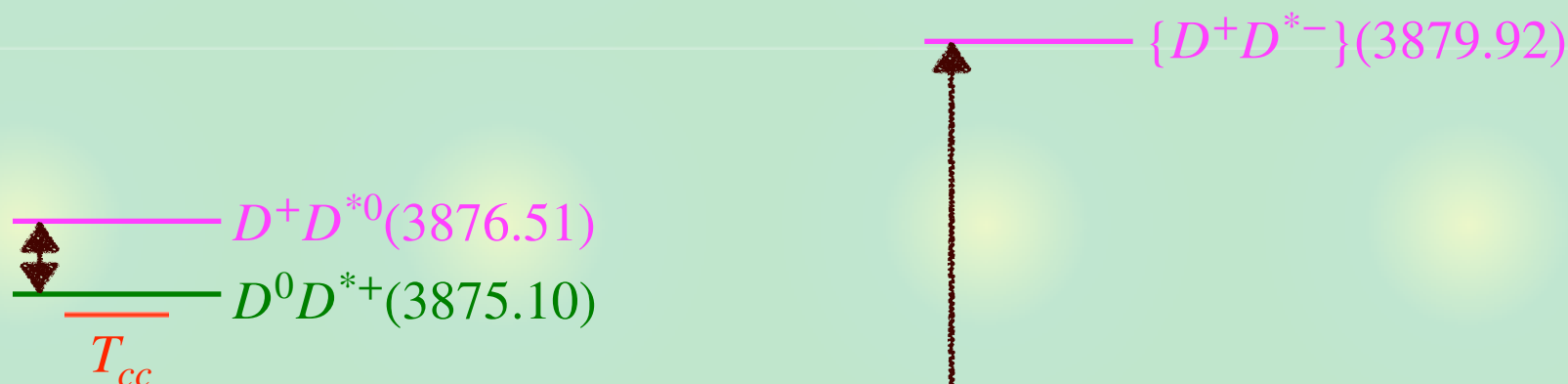


- Very small (**few MeV ~ keV**) energy scale involved



# Simplified picture

In this talk, we consider two-body channels



$$E_h = -0.36 - i \frac{0.048}{2} \text{ MeV}$$

(pole mass by LHCb)

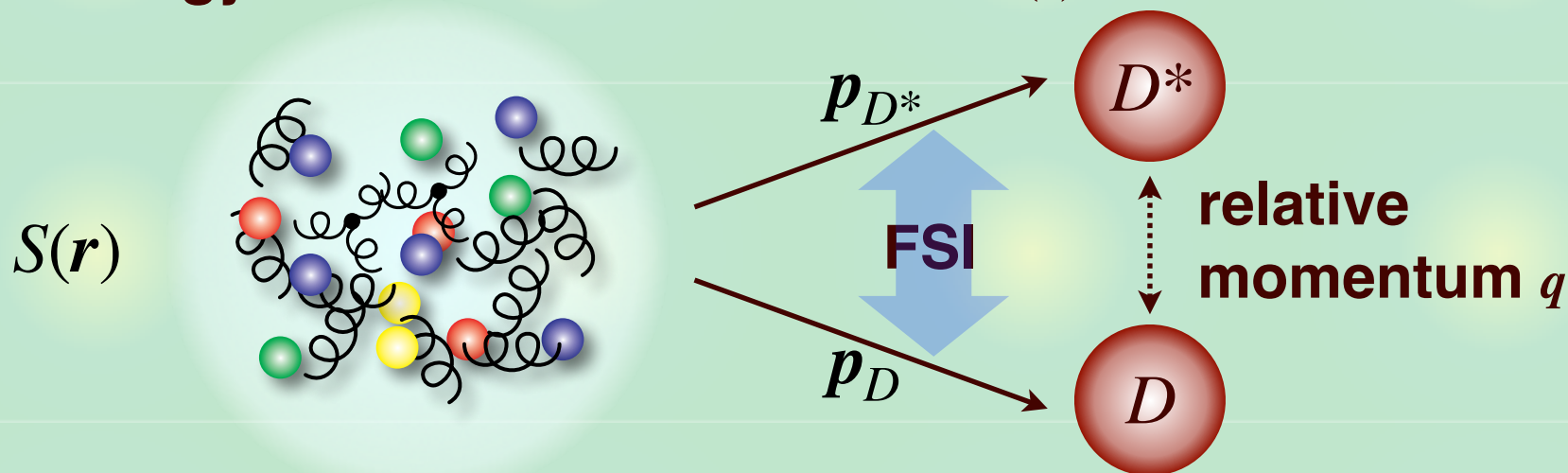
$$E_h = -0.04 - i \frac{1.19}{2} \text{ MeV}$$

(mass and width by PDG)

- **Binding energy** :  $T_{cc} > X(3872)$
- **Decay width** :  $T_{cc} < X(3872)$
- **Isospin breaking** :  $T_{cc} \sim 1.41 \text{ MeV}$  ,  $X(3872) \sim 8.23 \text{ MeV}$

# Correlation function and hadron interaction

High-energy collision: chaotic source  $S(\mathbf{r})$  of hadron emission



## - Definition

$$C(\mathbf{q}) = \frac{N_{DD^*}(\mathbf{p}_D, \mathbf{p}_{D^*})}{N_D(\mathbf{p}_D)N_{D^*}(\mathbf{p}_{D^*})} \quad (= 1 \text{ in the absence of FSI})$$

## - Theory (Koonin-Pratt formula)

$$C(\mathbf{q}) \simeq \int d^3\mathbf{r} S(\mathbf{r}) |\Psi_q^{(-)}(\mathbf{r})|^2$$

Source function  $\longleftrightarrow$  two-body wave function (FSI)



$DD^*, D\bar{D}^*$  potentials

## Coupled-channel potentials

$$V_{DD^*/D\bar{D}^*} = \frac{1}{2} \begin{pmatrix} V_{I=1} + V_{I=0} & V_{I=1} - V_{I=0} \\ V_{I=1} - V_{I=0} & V_{I=1} + V_{I=0} + V_c \end{pmatrix} \begin{matrix} D^0 D^{*+} / \{D^0 \bar{D}^{*0}\} \\ D^+ D^{*0} / \{D^+ D^{*-}\} \end{matrix}$$

↑ **Coulomb for  $\{D^+ D^{*-}\}$**

-  $I = 0$  : **one-range gaussian potentials,  $I = 1$  neglected**

$$V_{I=0} = V_0 \exp\{-m_\pi^2 r^2\}, \quad V_{I=1} = 0$$

↑ **range by  $\pi$  exchange**

$V_0 \in \mathbb{C}$  ← **scattering lengths (molecule picture)**

-  $T_{cc}$  :  $a_0^{D^0 D^{*+}} = -7.16 + i1.85$  fm (**LHCb analysis**)

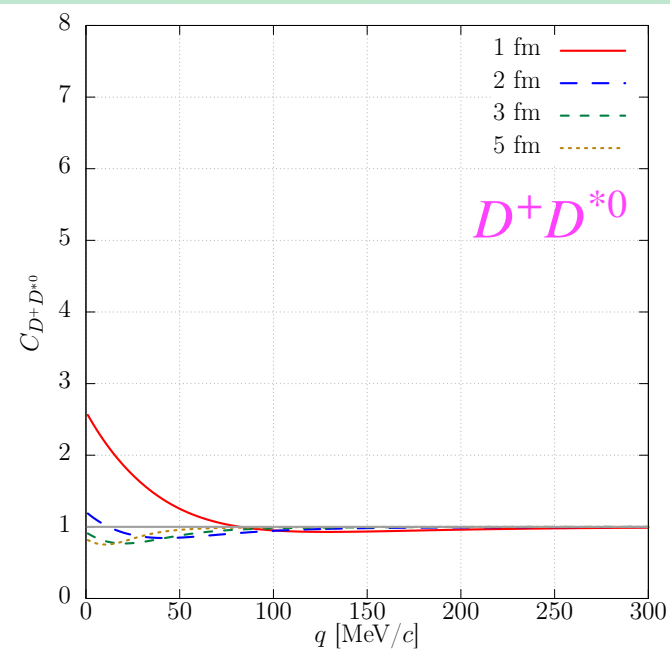
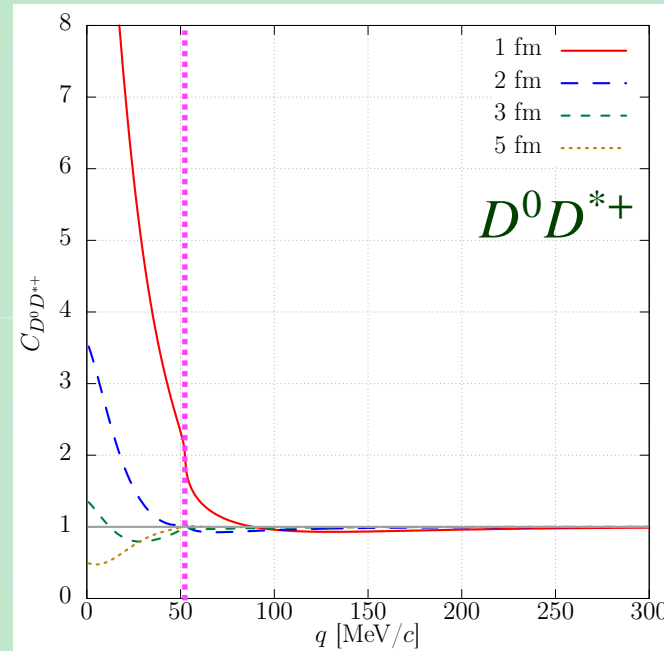
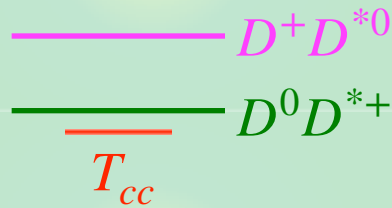
**LHCb collaboration, Nature Comm., 13, 3351 (2022)**

-  $X(3872)$  :  $a_0^{D^0 \bar{D}^{*0}} = -4.23 + i3.95$  fm ( $a_0 = -i/\sqrt{2\mu E_h}$  **with PDG  $E_h$** )

$DD^* \sim T_{cc}$  sector

$D^0D^{*+}$  and  $D^+D^{*0}$  correlation functions ( $cc\bar{u}\bar{d}$ , exotic)

Y. Kamiya, T. Hyodo, A. Ohnishi, EPJA58, 131 (2022)



- Bound state feature (source size dep.) in both channels
- Strong signal in  $D^0D^{*+}$ , weaker one in  $D^+D^{*0}$
- $D^+D^{*0}$  cusp in  $D^0D^{*+}$  ( $q \sim 52$  MeV) is not very prominent



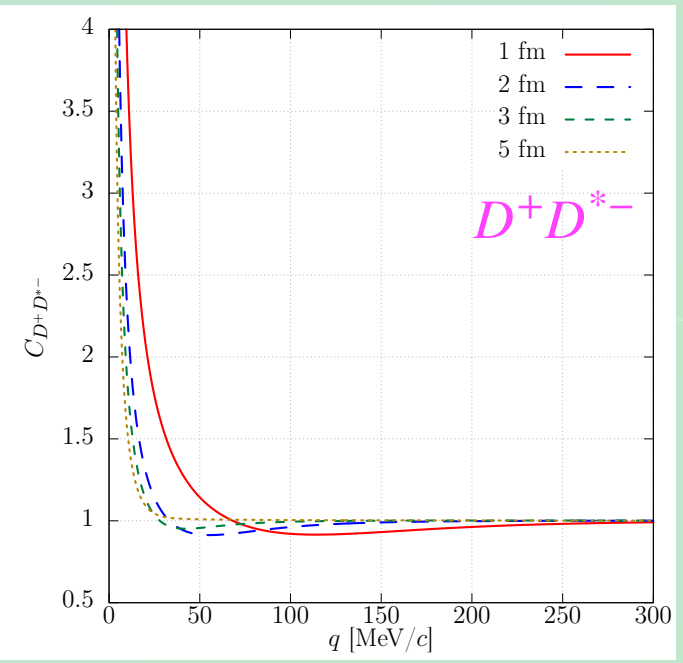
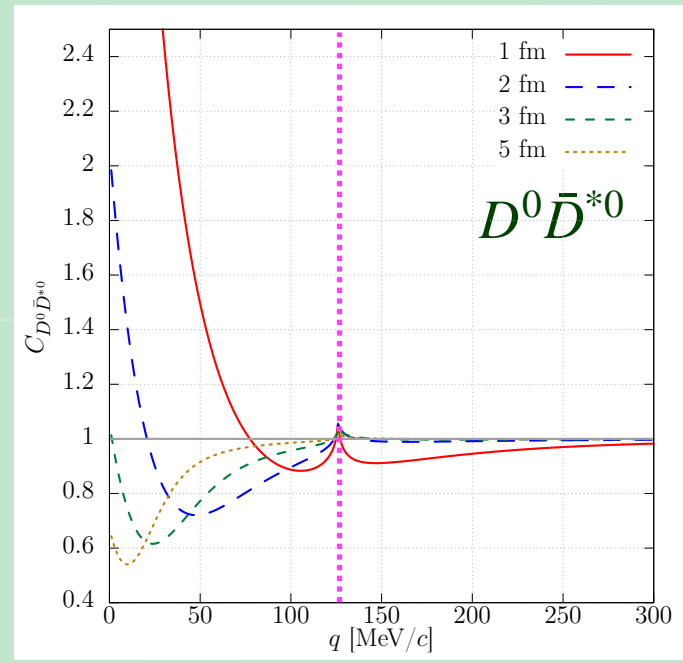
$D\bar{D}^* \sim X(3872)$  sector

$D^0\bar{D}^{*0}$  and  $D^+D^{*-}$  correlation functions ( $c\bar{c}q\bar{q}$ )

Y. Kamiya, T. Hyodo, A. Ohnishi, EPJA58, 131 (2022)

$D^+D^{*-}$

$D^0\bar{D}^{*0}$   
 $X(3872)$

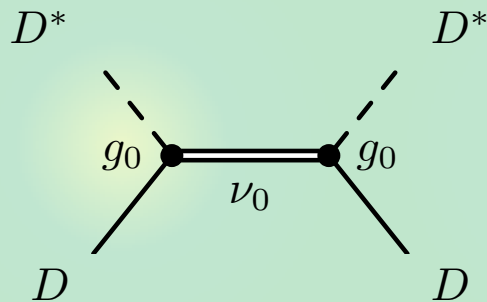


- Bound state feature in  $D^0\bar{D}^{*0}$  correlation
- Sizable  $D^+D^{*-}$  cusp in  $D^0\bar{D}^{*0}$  ( $q \sim 126$  MeV)
- $D^+D^{*-}$  correlation : Coulomb attraction dominance

# Effect of compact quark states

Coupling to compact quark states  $\rightarrow DD^*, D\bar{D}^*$  potentials?

- s-channel exchange of bare state  $\psi \sim cc\bar{u}\bar{d}, c\bar{c}$



Feshbach method : effective  $DD^*$  potential with  $\psi$  effect

H. Feshbach, *Ann. Phys.* **5**, 357 (1958); *ibid*, **19**, 287 (1962)

$$\langle \mathbf{r}'_{DD^*} | V_{\text{eff}}^{DD^*}(E) | \mathbf{r}_{DD^*} \rangle = V^{DD^*}(\mathbf{r})\delta(\mathbf{r}' - \mathbf{r}) + \frac{\langle \mathbf{r}'_{DD^*} | V^t | \psi \rangle \langle \psi | V^t | \mathbf{r}_{DD^*} \rangle}{E - \nu_0}$$

$$= V(\mathbf{r}'_{DD^*}, \mathbf{r}_{DD^*}; E)$$

- Effective potential is **non-local** and **energy-dependent**

I. Terashima, T. Hyodo, arXiv:2208.14075 [nucl-th]

# local approximation

**Non-local potential with Yukawa FF**  $\langle r_{DD^*} | V^t | \psi \rangle = g_0 e^{-\Lambda r} / r$

S. Aoki and K. Yazaki, PTEP2022, 033B04 (2022)

- Wave function  $\psi_k(r)$  is analytically solvable ( $k = \sqrt{2\mu E}$ )

**Local approximations :  $\{D^0\bar{D}^{*0}\}$  potentials for  $X(3872)$  at  $E = 0$**

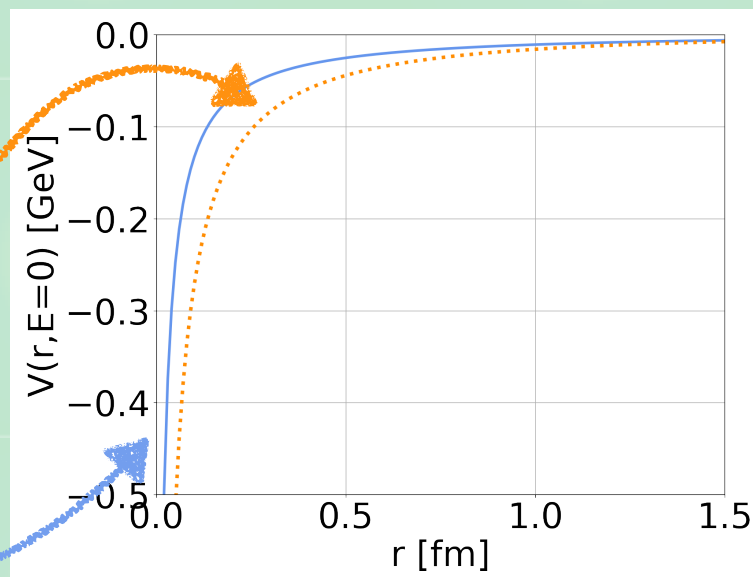
I. Terashima, T. Hyodo, in preparation

- Formal derivative expansion

$$V^{\text{formal}}(r, E) = \frac{4\pi g_0^2}{\Lambda^2(E - \nu_0)} \frac{e^{-\Lambda r}}{r} + \mathcal{O}(\nabla)$$

- HALQCD (reproduces  $\delta(E)$ )

$$V^{\text{HAL}}(r, E) = \frac{1}{2\mu r \psi_k(r)} \frac{d^2}{dr^2} [r \psi_k(r)] + \mathcal{O}(\nabla^2)$$



-  $V(r'_{DD^*}, r_{DD^*}; E)$  can be approximated by  $V^{\text{HAL}}(r, 0)$  around  $E \sim 0$

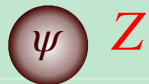
# Compositeness theorem

Near-threshold s-wave states are **all molecules!**

## - Compositeness theorem

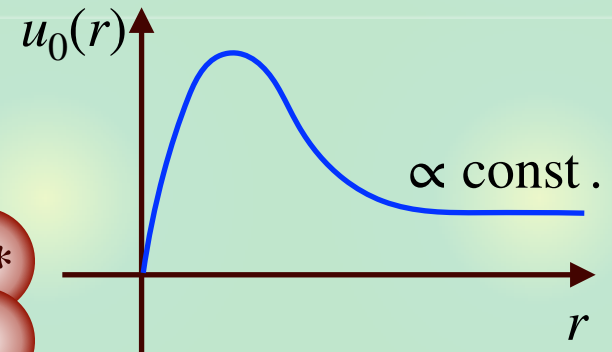
T. Hyodo, PRC90, 055208 (2014)

$$1 = |\langle T_{cc} | \psi \rangle|^2 + \int dr |\langle T_{cc} | r_{DD^*} \rangle|^2$$



$Z$

**compositeness**  $X$



→ Fully molecule state  $X = 1$  in  $B \rightarrow 0$  limit

## - Low-energy universality

E. Braaten, H.-W. Hammer, Phys. Rept. 428, 259 (2006);

P. Naidon, S. Endo, Rept. Prog. Phys. 80, 056001 (2017)

## - Threshold rule of cluster nuclei

H. Horiuchi, K. Ikeda, Y. Suzuki, PTPS 55, 89 (1972)

## - Peculiar pole trajectories

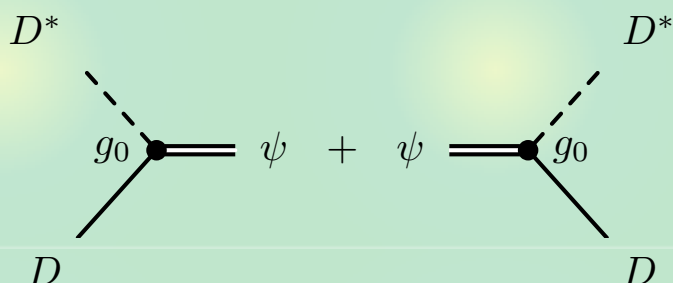
C. Hanhart, A. Nefediev, arXiv:2209.10165 [hep-ph]

# Model setup

## EFT model for $T_{cc}$ (single channel)

T. Kinugawa, T. Hyodo, in preparation

- $DD^*$  coupled with a bare state  $\psi$  (no direct  $DD^*$  int.)



Parameters : coupling  $g_0$  and bare energy  $\nu_0$  (cutoff  $\Lambda = m_\pi$ )

- Bound state condition with  $B \rightarrow g_0(\nu_0; \Lambda, B)$
- $\nu_0$  free parameter (c.f. quark model  $\sim 7$  MeV)

M. Karlinar, J.L. Rosner, PRL 119, 202001 (2018)

**Compositeness**  $X(\nu_0; \Lambda, B)$  : fraction of  $DD^*$  molecule

Y. Kamiya, T. Hyodo, PRC93, 035203 (2016); PTEP2017, 023D02 (2017);

T. Kinugawa, T. Hyodo, PRC 106, 015205 (2022)

# Structure of bound state

Natural binding energy ← scale of strong interaction : 1 fm

T. Kinugawa, T. Hyodo, in preparation

$$B \sim \frac{1}{2\mu_{DD^*}(1 \text{ fm})^2} \sim 20 \text{ MeV}$$

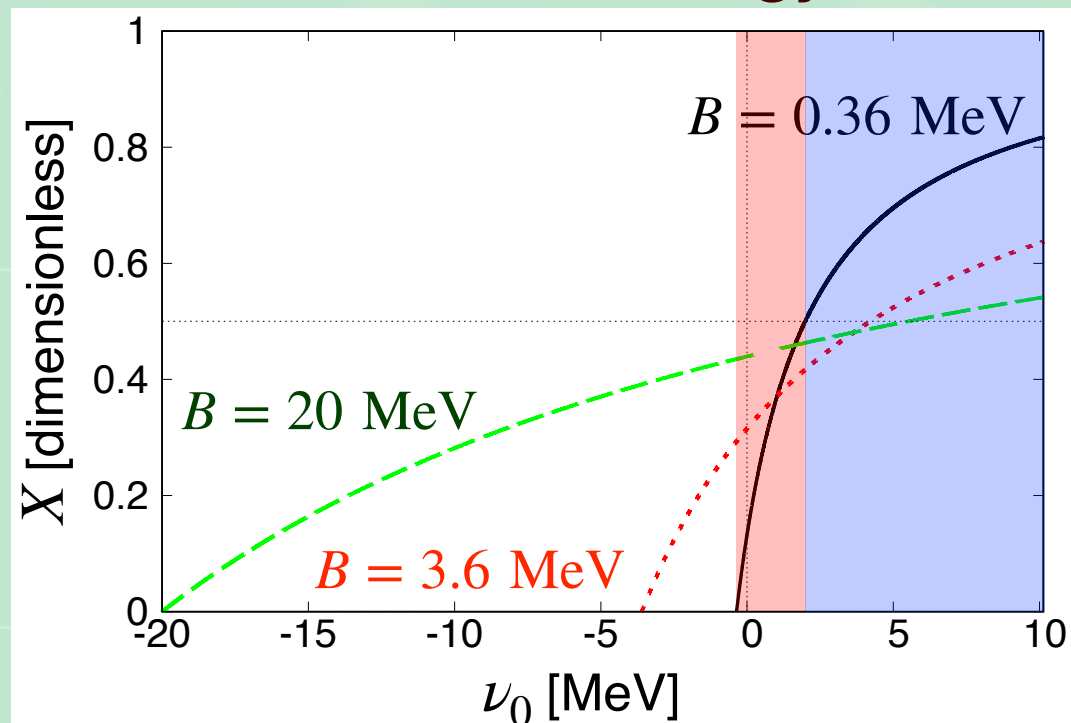
**Natural** :  $B = 20 \text{ MeV}$

- $X > 0.5$  for **15%** of  $\nu_0$
- **Elementary dominance**
- ← **Bare state origin**

**Shallow** :  $B = 0.36 \text{ MeV}$

- $X > 0.5$  for **78%** of  $\nu_0$
- **Composite dominance** even without  $DD^*$  direct interaction
- To have  $X < 0.5$ , **fine tuning of  $\nu_0$**  is necessary

cutoff energy scale ↓

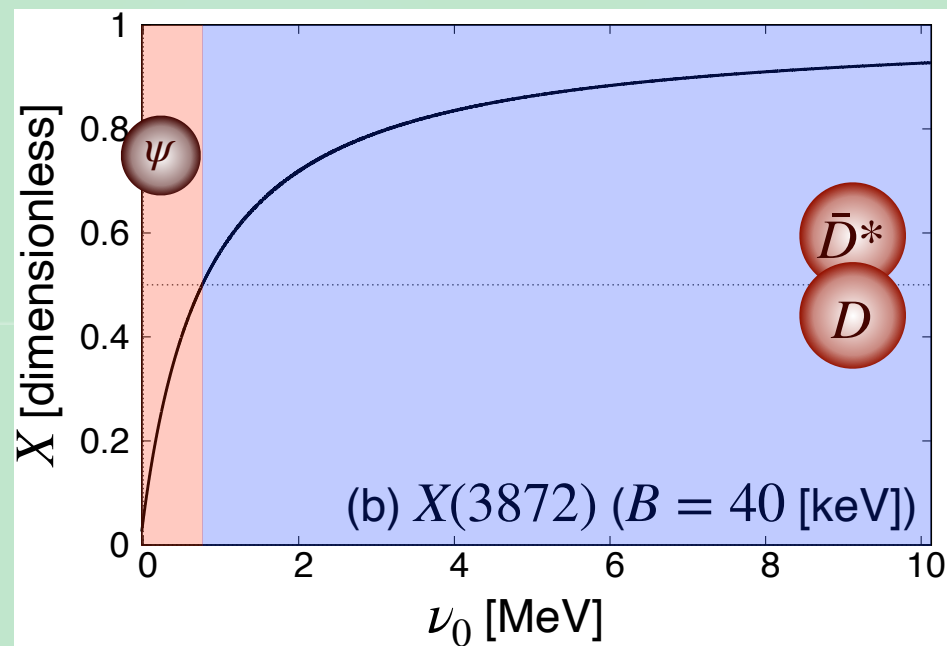
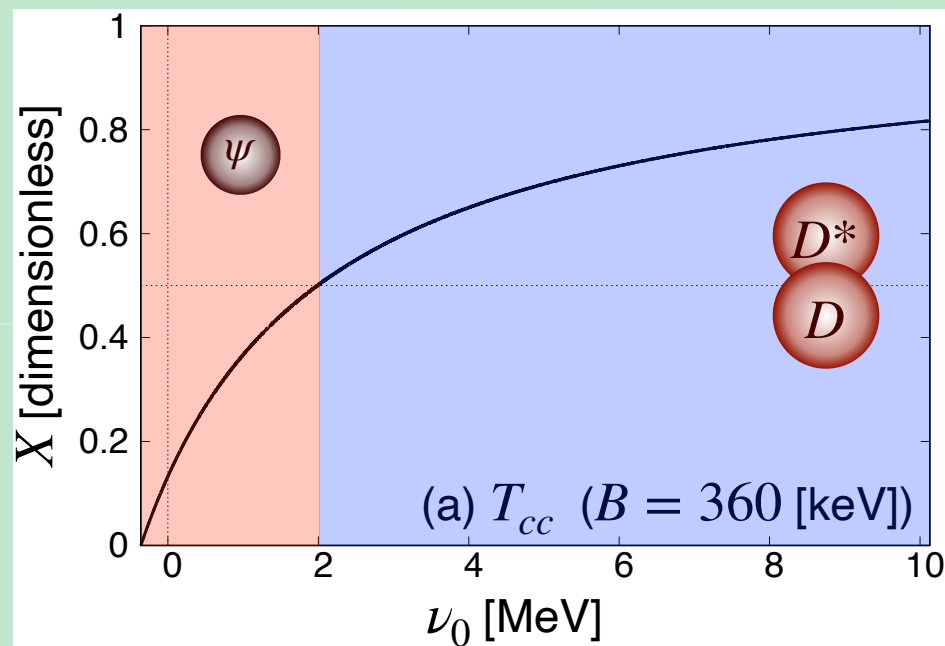




# Application to $T_{cc}$ and $X(3872)$

$T_{cc}$  and  $X(3872)$  : single-channel case

T. Kinugawa, T. Hyodo, in preparation

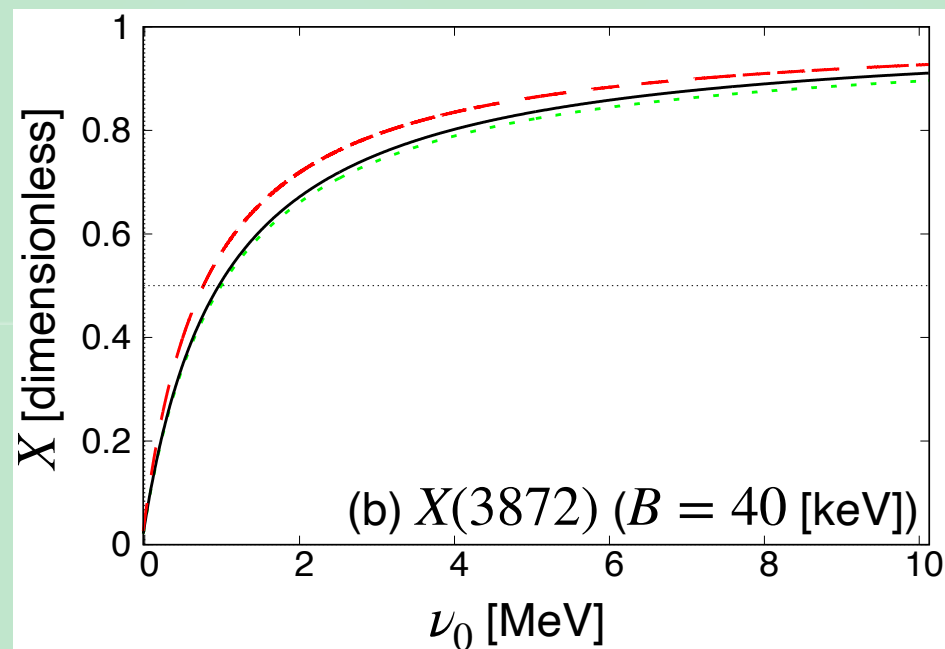
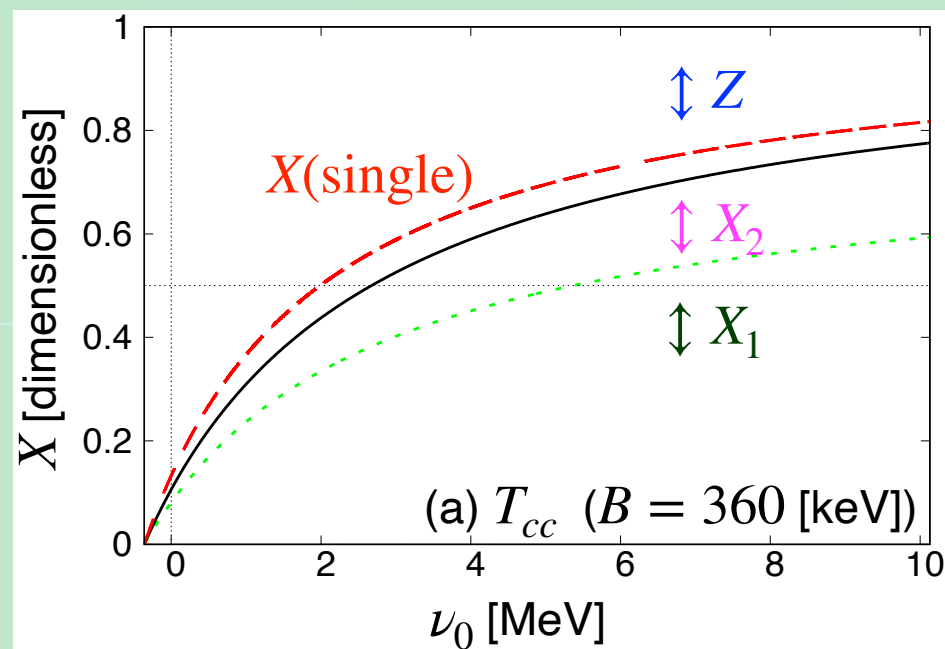


- $X > 0.5$  for **78% of  $\nu_0$**  for  $T_{cc}$ ,  $X > 0.5$  for **92% of  $\nu_0$**  for  $X(3872)$
- $X(3872)$  is more composite ← smaller  $B$
- To have  $X < 0.5$ , **extreme fine tuning of  $\nu_0$**  is necessary

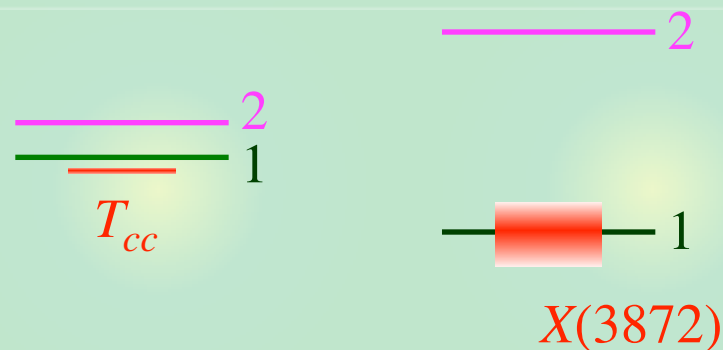
**More realistic  $T_{cc}$  and  $X(3872)$**

$T_{cc}$  and  $X(3872)$  : coupled-channel case

T. Kinugawa, T. Hyodo, in preparation



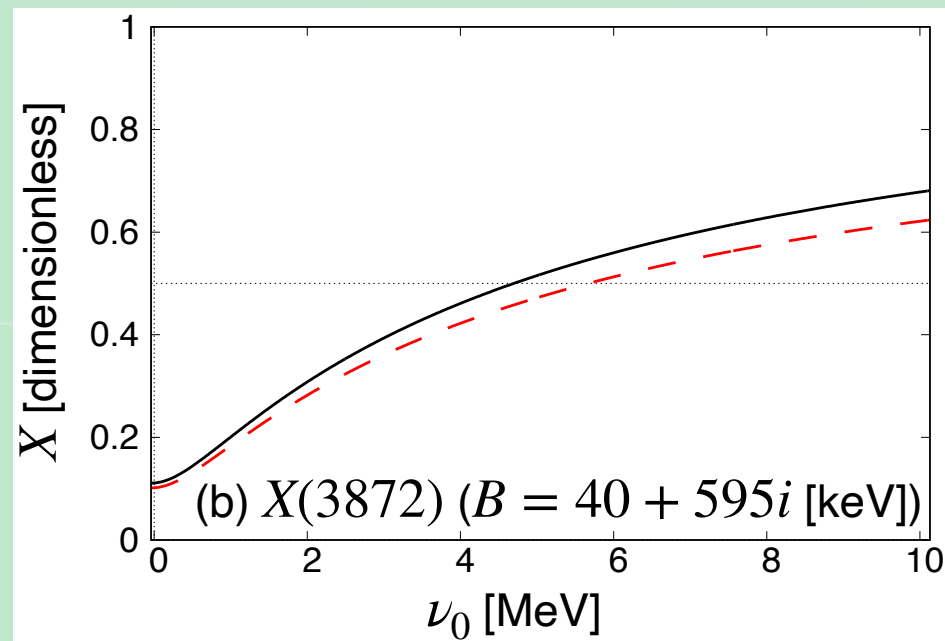
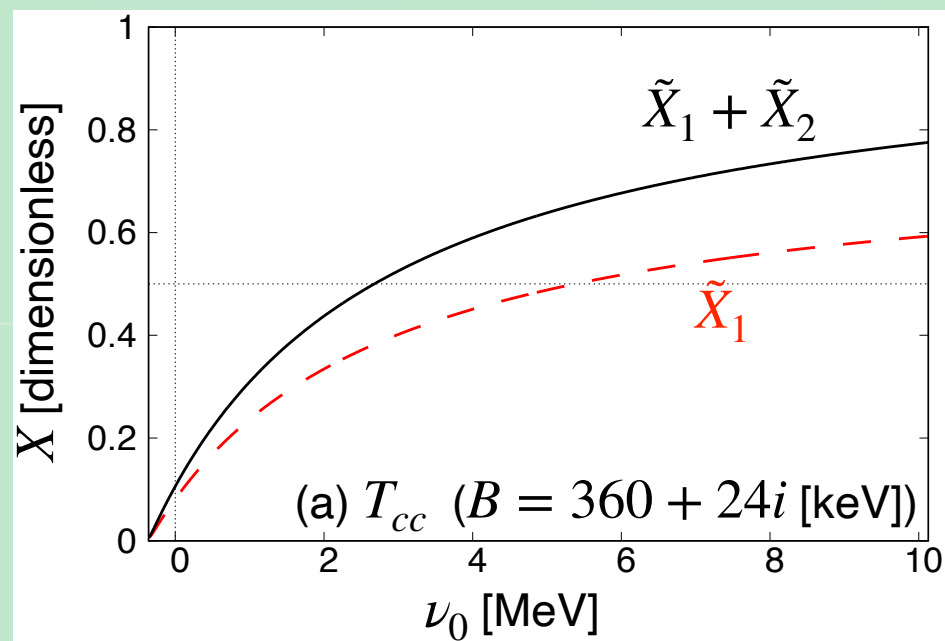
- $X(\text{single}) \sim X_1 + X_2$  :  $Z$  is stable
- $DD^*$  effect is shared by 1 and 2
- $X_{2,T_{cc}} > X_{2,X(3872)} \leftarrow$  closer  $D^+D^{*0}$



# Further realistic $T_{cc}$ and $X(3872)$

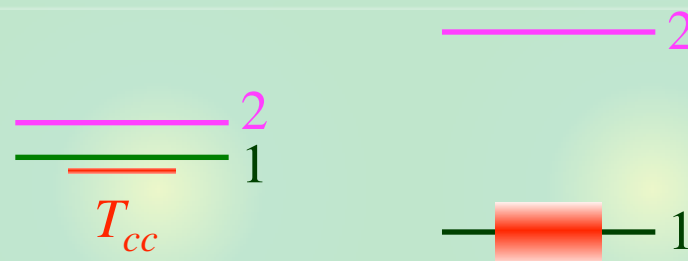
$T_{cc}$  and  $X(3872)$  : coupled-channel case with decay width

T. Kinugawa, T. Hyodo, in preparation



$$- \tilde{X}_i = \frac{|X_i|}{\sum_j |X_j| + |Z|}$$

T. Sekihara, *et al.*, PRC 93, 035204 (2016)



- Important in  $X(3872)$  ← large width

$X(3872)$

# Summary



$D^0 D^{*+}$  and  $D^0 \bar{D}^{*0}$  correlations

- (quasi-)bound nature of  $T_{cc}$  and  $X(3872)$

Y. Kamiya, T. Hyodo, A. Ohnishi, EPJA58, 131 (2022)



Coupling to compact quark states

- Potential becomes non-local and E-dep., but effective **local potential** can be constructed.

I. Terashima, T. Hyodo, in preparation



Compositeness theorem

- Near-threshold **s-wave** states are **molecules**, no matter how you construct them.

T. Hyodo, PRC 90, 055208 (2014); T. Kinugawa, T. Hyodo, in preparation