

$\Lambda(1405)$ as a hadronic molecule



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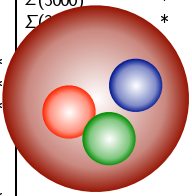
2020, Nov. 5th 1

Observed hadrons (2018)

PDG 2018 edition

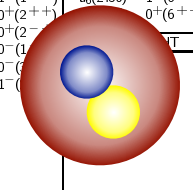
<http://pdg.lbl.gov/>

p	$1/2^+$	****	$\Delta(1232)$	$3/2^+$	****	Σ^+	$1/2^+$	****	Ξ^0	$1/2^+$	****	Λ_c^+	$1/2^+$	****
n	$1/2^+$	****	$\Delta(1600)$	$3/2^+$	***	Σ^0	$1/2^+$	****	Ξ^-	$1/2^+$	****	$\Lambda_c(2595)^+$	$1/2^-$	***
$N(1440)$	$1/2^+$	****	$\Delta(1620)$	$1/2^-$	****	Σ^-	$1/2^+$	****	$\Xi(1530)$	$3/2^+$	****	$\Lambda_c(2625)^+$	$3/2^-$	***
$N(1520)$	$3/2^-$	****	$\Delta(1700)$	$3/2^-$	****	$\Sigma(1385)$	$3/2^+$	****	$\Xi(1620)$	*		$\Lambda_c(2765)^+$	*	
$N(1535)$	$1/2^-$	****	$\Delta(1750)$	$1/2^+$	*	$\Sigma(1480)$	*		$\Xi(1690)$	***		$\Lambda_c(2880)^+$	$5/2^+$	***
$N(1650)$	$1/2^-$	****	$\Delta(1900)$	$1/2^-$	**	$\Sigma(1560)$	*		$\Xi(1820)$	$3/2^-$	***	$\Lambda_c(2940)^+$	****	
$N(1675)$	$5/2^-$	****	$\Delta(1905)$	$5/2^+$	****	$\Sigma(1580)$	$3/2^-$	**	$\Xi(1950)$	***		$\Sigma_c(2455)$	$1/2^+$	****
$N(1680)$	$5/2^+$	****	$\Delta(1910)$	$1/2^+$	****	$\Sigma(1620)$	$1/2^-$	*	$\Xi(2030)$	$\geq 5/2^?$	***	$\Sigma_c(2520)$	$3/2^+$	****
$N(1685)$	*		$\Delta(1920)$	$3/2^+$	***	$\Sigma(1660)$	$1/2^+$	***	$\Xi(2120)$	**		$\Sigma_c(2800)$	****	
$N(1700)$	$3/2^-$	***	$\Delta(1930)$	$5/2^-$	***	$\Sigma(1670)$	$3/2^-$	****	$\Xi(2250)$	**		Ξ_c^+	$1/2^+$	****
$N(1710)$	$1/2^+$	***	$\Delta(1940)$	$3/2^-$	**	$\Sigma(1690)$	**		$\Xi(2370)$	**		Ξ_c^0	$1/2^+$	****
$N(1720)$	$3/2^+$	****	$\Delta(1950)$	$7/2^+$	****	$\Sigma(1730)$	$3/2^+$	*	$\Xi(2500)$	*		Ξ_c^-	$1/2^+$	****
$N(1860)$	$5/2^+$	**	$\Delta(2000)$	$5/2^+$	**	$\Sigma(1750)$	$1/2^-$	***	Ω^-	$3/2^+$	****	Ξ_c^0	$1/2^+$	****
$N(1875)$	$3/2^-$	***	$\Delta(2150)$	$1/2^-$	*	$\Sigma(1770)$	$1/2^+$	*	$\Omega(2250)^-$	****		Ξ_c^+	$1/2^+$	****
$N(1880)$	$1/2^+$	**	$\Delta(2200)$	$7/2^-$	*	$\Sigma(1775)$	$5/2^-$	****	$\Omega(2380)^-$	**		Ξ_c^0	$1/2^+$	****
$N(1895)$	$1/2^-$	**	$\Delta(2300)$	$9/2^+$	**	$\Sigma(1840)$	$3/2^+$	**	$\Omega(2470)^-$	**		Ξ_c^-	$1/2^+$	****
$N(1900)$	$3/2^+$	***	$\Delta(2350)$	$5/2^-$	*	$\Sigma(1880)$	$1/2^+$	**				Ξ_c^0	$1/2^+$	****
$N(1990)$	$7/2^+$	**	$\Delta(2390)$	$7/2^+$	*	$\Sigma(1900)$	$1/2^-$	*				Ξ_c^+	$1/2^+$	****
$N(2000)$	$5/2^+$	**	$\Delta(2400)$	$9/2^-$	**	$\Sigma(1915)$	$5/2^+$	****				Ξ_c^0	$1/2^+$	****
$N(2040)$	$3/2^+$	*	$\Delta(2420)$	$11/2^+$	****	$\Sigma(1940)$	$3/2^+$	**				Ξ_c^-	$1/2^+$	****
$N(2060)$	$5/2^-$	**	$\Delta(2750)$	$13/2^-$	**	$\Sigma(1940)$	$3/2^-$	***				Ω_c^0	$1/2^+$	****
$N(2100)$	$1/2^+$	*	$\Delta(2950)$	$15/2^+$	**	$\Sigma(2000)$	$1/2^-$	*				$\Omega_c(2770)^0$	$3/2^+$	****
$N(2120)$	$3/2^-$	**			$\Sigma(2030)$	$7/2^+$	****							
$N(2190)$	$7/2^-$	****	Λ	$1/2^+$	****	$\Sigma(2070)$	$5/2^+$	*						
$N(2220)$	$9/2^+$	****	$\Lambda(1405)$	$1/2^-$	****	$\Sigma(2080)$	$3/2^+$	**						
$N(2250)$	$9/2^-$	****	$\Lambda(1520)$	$3/2^-$	****	$\Sigma(2100)$	$7/2^-$	*						
$N(2300)$	$1/2^+$	**	$\Lambda(1600)$	$1/2^+$	***	$\Sigma(2250)$	****							
$N(2570)$	$5/2^-$	**	$\Lambda(1670)$	$1/2^-$	****	$\Sigma(2455)$	**							
$N(2600)$	$11/2^-$	***	$\Lambda(1690)$	$3/2^-$	****	$\Sigma(2620)$	**							
$N(2700)$	$13/2^+$	**	$\Lambda(1710)$	$1/2^+$	*	$\Sigma(3000)$	*							
			$\Lambda(1800)$	$1/2^-$	***	$\Sigma(3000)$	*							
			$\Lambda(1810)$	$1/2^+$	***	$\Sigma(3000)$	*							
			$\Lambda(1820)$	$5/2^+$	****	$\Sigma(3000)$	*							
			$\Lambda(1830)$	$5/2^-$	****	$\Sigma(3000)$	*							
			$\Lambda(1890)$	$3/2^+$	****	$\Sigma(3000)$	*							
			$\Lambda(2000)$	*		$\Sigma(3000)$	*							
			$\Lambda(2020)$	$7/2^+$	*	$\Sigma(3000)$	*							
			$\Lambda(2050)$	$3/2^-$	*	$\Sigma(3000)$	*							
			$\Lambda(2100)$	$7/2^-$	****	$\Sigma(3000)$	*							
			$\Lambda(2110)$	$5/2^+$	***	$\Sigma(3000)$	*							
			$\Lambda(2325)$	$3/2^-$	*	$\Sigma(3000)$	*							
			$\Lambda(2350)$	$9/2^+$	**	$\Sigma(3000)$	*							
			$\Lambda(2585)$	**		$\Sigma(3000)$	*							



155 baryons

LIGHT UNFLAVORED (S = C = B = 0)		STRANGE (S = ±1, C = B = 0)		CHARMED, STRANGE (C = S = ±1)		CC F(C)	
F(J ^{PC})	F(J ^{PC})	F(J ^{PC})	F(J ^{PC})	F(J ^{PC})	F(J ^{PC})	F(C)	F(C)
π^\pm	$1^-(0^-)$	$\rho(1680)$	$0^-(1^-)$	K^\pm	$1/2(0^-)$	D_s^\pm	$0^-(0^-)$
π^0	$1^-(0^-)$	$\rho(1690)$	$1^+(3^-)$	K_S^0	$1/2(0^-)$	D_s^\pm	$0^-(?)$
η	$0^+(0^-)$	$\rho(1700)$	$1^+(1^-)$	K_L^0	$1/2(0^-)$	$D_{s1}^{\pm}(2317)^+$	$0^+(0^+)$
$\eta(500)$	$0^+(0^+)$	$a_2(1700)$	$1^-(2^+)$	K_1^0	$1/2(0^+)$	$D_{s1}^*(2460)^+$	$0^+(1^+)$
$\rho(770)$	$1^+(1^-)$	$\omega(1710)$	$0^+(0^+)$	$K_0^*(800)$	$1/2(0^+)$	$D_{s1}^*(2536)^+$	$0^+(1^+)$
$\omega(782)$	$0^+(0^+)$	$\eta(1760)$	$0^+(0^+)$	$K^*(892)$	$1/2(1^-)$	$D_{s2}^*(2573)$	$0^+(?)$
$\eta(958)$	$0^+(0^+)$	$\pi(1800)$	$1^-(0^+)$	$K_1(1270)$	$1/2(1^+)$	$D_{s1}^*(2700)^+$	$0^-(1^-)$
$\phi(980)$	$0^+(0^+)$	$f_2(1810)$	$0^+(2^+)$	$K_1(1400)$	$1/2(1^+)$	$D_{s1}^*(2860)^+$	$0^-(?)$
$a_0(980)$	$1^-(0^+)$	$X(1835)$	$?^?(2^-)$	$K^*(1410)$	$1/2(1^-)$	$D_{s1}^*(3040)^+$	$0^-(?)$
$\omega(1020)$	$0^-(1^-)$	$X(1840)$	$?^?(?)$	$K_0^*(1430)$	$1/2(0^+)$		
$h_1(1170)$	$0^-(1^+)$	$\omega_3(1850)$	$0^-(3^-)$	$K_0^*(1430)$	$1/2(2^+)$	BOTTOM (B = ±1)	
$b_1(1235)$	$1^+(1^+)$	$\eta_2(1870)$	$0^+(2^-)$	$K(1460)$	$1/2(0^-)$	B^\pm	$1/2(0^-)$
$a_1(1260)$	$1^-(1^+)$	$\pi_2(1880)$	$1^-(2^+)$	$K_2(1580)$	$1/2(2^-)$	B^0	$1/2(0^-)$
$f_1(1270)$	$0^+(2^+)$	$\rho(1900)$	$1^+(1^-)$	$K_1(1630)$	$1/2(1^+)$	B^+ / B^0	ADMIXTURE
$f_1(1285)$	$0^+(1^+)$	$f_2(1910)$	$0^+(2^+)$	$K_1(1650)$	$1/2(1^+)$	$B^+ / B^0 / B_s^0 / b$	ADMIXTURE
$\eta(1295)$	$0^+(0^+)$	$f_2(1950)$	$0^+(2^+)$	$K^*(1680)$	$1/2(1^-)$	V_b and V_{cb}	CKM Matrix Elements
$\pi(1300)$	$1^-(0^+)$	$f_3(1990)$	$1^+(3^-)$	$K_2^*(1770)$	$1/2(1^-)$	B^*	$1/2(1^-)$
$a_2(1320)$	$1^-(2^+)$	$f_2(2010)$	$0^+(2^+)$	$K_3^*(1820)$	$1/2(3^-)$	$B_1(5721)^+$	$1/2(1^+)$
$f_0(1370)$	$0^+(0^+)$	$f_0(2020)$	$0^+(0^+)$	$K_3^*(1870)$	$1/2(3^-)$	$B_1(5721)^0$	$1/2(1^+)$
$h_1(1380)$	$?^-(1^+)$	$f_2(2040)$	$1^-(4^+)$	$K_0^*(1880)$	$1/2(2^-)$	$B_2^*(5732)$	$?^?(?)$
$\pi_1(1400)$	$1^-(1^+)$	$f_0(2050)$	$0^+(4^+)$	$K_1(1830)$	$1/2(0^+)$	$B_2^*(5747)^0$	$1/2(2^+)$
$\eta(1405)$	$0^+(0^+)$	$\pi_2(2100)$	$1^-(2^+)$	$K_0^*(1950)$	$1/2(0^+)$	$B_2^*(5747)^+$	$1/2(2^+)$
$f_1(1420)$	$0^+(1^+)$	$f_0(2100)$	$0^+(0^+)$	$K_1^*(1980)$	$1/2(2^+)$	$B_3^*(5970)^+$	$?^?(?)$
$\omega(1420)$	$0^-(1^-)$	$f_2(2150)$	$0^+(2^+)$	$K_1^*(2045)$	$1/2(4^+)$	$B_3^*(5970)^0$	$?^?(?)$
$f_2(1430)$	$0^+(2^+)$	$\rho(2150)$	$1^+(1^-)$	$K_2^*(2250)$	$1/2(2^-)$	$B(5970)^+$	$?^?(?)$
$a_0(1450)$	$1^-(0^+)$	$\omega(2170)$	$0^-(1^-)$	$K_3^*(2330)$	$1/2(3^+)$	$B(5970)^0$	$?^?(?)$
$\phi(1450)$	$1^-(1^-)$	$f_0(2200)$	$0^+(0^+)$	$K_3^*(2380)$	$1/2(5^-)$		
$\eta(1475)$	$0^+(0^+)$	$f_2(2220)$	$0^+(2^+)$	$K_4^*(2500)$	$1/2(4^-)$		
$f_0(1500)$	$0^+(0^+)$	$\eta(2250)$	$0^+(0^+)$	$K(3100)$	$?^?(?)$	BOTTOM, STRANGE (B = ±1, S = ±1)	
$f_1(1510)$	$0^+(1^+)$	$\rho_3(2250)$	$1^+(3^-)$			B_s^\pm	$0^-(0^-)$
$f_2(1525)$	$0^+(2^+)$	$f_2(2300)$	$0^+(2^+)$			B_s^0	$0^-(1^-)$
$f_2(1565)$	$0^+(2^+)$	$f_0(2300)$	$0^+(4^+)$	D^\pm	$1/2(0^-)$	$B_{s1}^*(5830)^0$	$0^+(1^+)$
$\rho(1570)$	$1^+(1^-)$	$f_0(2330)$	$0^+(0^+)$	D^0	$1/2(0^-)$	$B_{s2}^*(5840)^0$	$0^+(2^+)$
$h_1(1595)$	$0^-(1^+)$	$f_2(2340)$	$0^+(2^+)$	$D^*(2017)^0$	$1/2(1^-)$	$B_{s1}^*(5850)$	$?^?(?)$
$\pi_1(1600)$	$1^-(1^+)$	$\rho_3(2350)$	$1^+(5^-)$	$D^*(2017)^+$	$1/2(1^-)$		
$a_1(1640)$	$1^-(1^+)$	$a_6(2450)$	$0^+(6^+)$	$D_1^*(2000)^0$	$1/2(0^+)$	BOTTOM, CHARMED (B = C = ±1)	
$f_2(1640)$	$0^+(2^+)$			$D_0^*(2000)^+$	$1/2(0^+)$	B_c^\pm	$0^-(0^-)$
Σ_b	$3/2^+$			$D_1^*(2000)^+$	$1/2(1^+)$	$B_c(25)^+$	$?^?(?)$
Ξ_b	$1/2^+$			$D_1(2430)^0$	$1/2(1^+)$		
Ξ_b^-	$1/2^+$			$D_1(2420)^+$	$1/2(1^+)$		
$\Xi_b(5935)^0$	$1/2^+$			$D_1(2430)^+$	$1/2(1^+)$		
$\Xi_b(5945)^0$	$3/2^+$			$D_2^*(2460)^0$	$1/2(2^+)$		
$\Xi_b(5955)^+$	$3/2^+$			$D_2^*(2460)^+$	$1/2(2^+)$		
Ω_b	$1/2^+$			$D(2550)^0$	$1/2(0^-)$		
				$D(2600)$	$1/2(?)$		
				$D^*(2640)^+$	$1/2(?)$		
				$D(2750)$	$1/2(?)$		



206 mesons

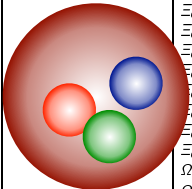
All ~ 370 hadrons emerge from single QCD Lagrangian.

Observed hadrons (2020)

PDG 2020 edition

<http://pdg.lbl.gov/>

ρ	$1/2^+$	****	$\Delta(1232)$	$3/2^+$	****	Σ^+	$1/2^+$	****	Ξ^0	$1/2^+$	****	Ξ^{++}	***	
n	$1/2^+$	****	$\Delta(1600)$	$3/2^+$	****	Σ^0	$1/2^+$	****	Ξ^-	$1/2^+$	****	Ξ_{cc}^{++}	***	
$N(1440)$	$1/2^+$	****	$\Delta(1620)$	$1/2^-$	****	Σ^-	$1/2^+$	****	$\Xi(1530)$	$1/2^+$	****	Λ_b^0	$1/2^+$	***
$N(1520)$	$3/2^-$	****	$\Delta(1700)$	$3/2^-$	****	$\Sigma(1385)$	$3/2^+$	****	$\Xi(1620)$	*		$\Lambda_b(5912)^0$	$1/2^-$	***
$N(1535)$	$1/2^-$	****	$\Delta(1750)$	$1/2^+$	*	$\Sigma(1580)$	$3/2^-$	*	$\Xi(1690)$	****		$\Lambda_b(5920)^0$	$3/2^-$	***
$N(1650)$	$1/2^-$	****	$\Delta(1900)$	$1/2^-$	***	$\Sigma(1620)$	$1/2^-$	*	$\Xi(1820)$	$3/2^-$	***	$\Lambda_b(6146)^0$	$3/2^+$	***
$N(1675)$	$5/2^-$	****	$\Delta(1905)$	$5/2^+$	****	$\Sigma(1660)$	$1/2^+$	***	$\Xi(1950)$	****		$\Lambda_b(6152)^0$	$5/2^+$	***
$N(1680)$	$5/2^+$	****	$\Delta(1910)$	$1/2^+$	****	$\Sigma(1670)$	$3/2^-$	****	$\Xi(2030)$	$\geq \frac{3}{2}^?$	****	Σ_b	$1/2^+$	***
$N(1700)$	$3/2^-$	***	$\Delta(1920)$	$3/2^+$	***	$\Sigma(1750)$	$1/2^-$	***	$\Xi(2120)$	*		Σ_b^-	$3/2^+$	***
$N(1710)$	$1/2^+$	****	$\Delta(1930)$	$5/2^-$	****	$\Sigma(1775)$	$5/2^-$	****	$\Xi(2250)$	**		$\Sigma_b(6097)^+$	***	
$N(1720)$	$3/2^+$	****	$\Delta(1940)$	$3/2^-$	**	$\Sigma(1780)$	$3/2^+$	**	$\Xi(2370)$	**		$\Sigma_b(6097)^-$	***	
$N(1860)$	$5/2^+$	**	$\Delta(1950)$	$7/2^+$	****	$\Sigma(1880)$	$1/2^+$	**	$\Xi(2500)$	*		Ξ_b^0	$1/2^+$	***
$N(1875)$	$3/2^-$	***	$\Delta(2000)$	$5/2^+$	**	$\Sigma(1900)$	$1/2^-$	**				Ξ_b^-	$1/2^+$	***
$N(1880)$	$1/2^+$	***	$\Delta(2150)$	$1/2^-$	*	$\Sigma(1910)$	$3/2^-$	***	$\Omega(2012)$	$?$	****	$\Xi_b(5935)$	$1/2^+$	***
$N(1895)$	$1/2^-$	****	$\Delta(2200)$	$7/2^-$	***	$\Sigma(1915)$	$5/2^+$	****	$\Omega(2120)$	$?$	****	$\Xi_b(5945)^0$	$3/2^+$	***
$N(1890)$	$3/2^+$	****	$\Delta(2300)$	$9/2^+$	***	$\Sigma(1940)$	$3/2^+$	**	$\Omega(2380)$	**		$\Xi_b(5955)$	$3/2^+$	***
$N(1990)$	$7/2^+$	**	$\Delta(2350)$	$5/2^-$	*	$\Sigma(2010)$	$3/2^-$	**	$\Omega(2380)$	**		$\Xi_b(6227)$	***	
$N(2000)$	$5/2^+$	**	$\Delta(2390)$	$7/2^+$	**	$\Sigma(2030)$	$7/2^+$	****	$\Omega(2470)$	**		Ω_b	$1/2^+$	***
$N(2040)$	$3/2^+$	*	$\Delta(2400)$	$9/2^-$	**	$\Sigma(2070)$	$5/2^+$	*				$P_c(4312)^+$	*	
$N(2060)$	$5/2^-$	***	$\Delta(2420)$	$11/2^-$										
$N(2100)$	$1/2^+$	***	$\Delta(2750)$	$13/2^-$										
$N(2120)$	$3/2^-$	***	$\Delta(2950)$	$15/2^-$										
$N(2190)$	$7/2^-$	****												
$N(2220)$	$9/2^+$	****	Λ	$1/2$										
$N(2250)$	$9/2^-$	****	Λ	$1/2^-$	**	$\Sigma(2455)$	**		$\Lambda_c(2880)^+$	$5/2^+$	***			
$N(2300)$	$1/2^+$	**	$\Lambda(1405)$	$1/2^-$	***	$\Sigma(2620)$	**		$\Lambda_c(2940)^+$	$3/2^-$	****			
$N(2570)$	$5/2^-$	**	$\Lambda(1520)$	$3/2^-$	****	$\Sigma(3000)$	*		$\Sigma_c(2455)$	$1/2^+$	****			
$N(2600)$	$11/2^-$	***	$\Lambda(1600)$	$1/2^+$	****	$\Sigma(3170)$	*		$\Sigma_c(2520)$	$3/2^+$	***			
$N(2700)$	$13/2^+$	**	$\Lambda(1670)$	$1/2^-$	****				$\Sigma_c(2800)$	****				
			$\Lambda(1690)$	$3/2^-$	****				Ξ_c^+	$1/2^+$	***			
			$\Lambda(1710)$	$1/2^+$	*				Ξ_c^0	$1/2^+$	****			
			$\Lambda(1800)$	$1/2^-$	***				Ξ_c^+	$1/2^+$	***			
			$\Lambda(1810)$	$1/2^+$	****				Ξ_c^0	$1/2^+$	***			
			$\Lambda(1820)$	$5/2^+$	****				Ξ_c^+	$1/2^+$	***			
			$\Lambda(1830)$	$5/2^-$	****				$\Xi_c(2645)$	$3/2^+$	***			
			$\Lambda(1890)$	$3/2^+$	****				$\Xi_c(2790)$	$1/2^-$	***			
			$\Lambda(2000)$	$1/2^-$	*				$\Xi_c(2815)$	$3/2^-$	***			
			$\Lambda(2050)$	$3/2^-$	*				$\Xi_c(2930)$	**				
			$\Lambda(2070)$	$3/2^+$	*				$\Xi_c(2970)$	***				
			$\Lambda(2080)$	$5/2^-$	*				$\Xi_c(3055)$	***				
			$\Lambda(2085)$	$7/2^+$	**				$\Xi_c(3080)$	***				
			$\Lambda(2100)$	$7/2^-$	****				$\Xi_c(3123)$	*				
			$\Lambda(2110)$	$5/2^+$	****				Ω_c^0	$1/2^+$	***			
			$\Lambda(2325)$	$3/2^-$	*				$\Omega_c(2720)^0$	$3/2^+$	****			
			$\Lambda(2350)$	$9/2^+$	***									
			$\Lambda(2585)$	**										



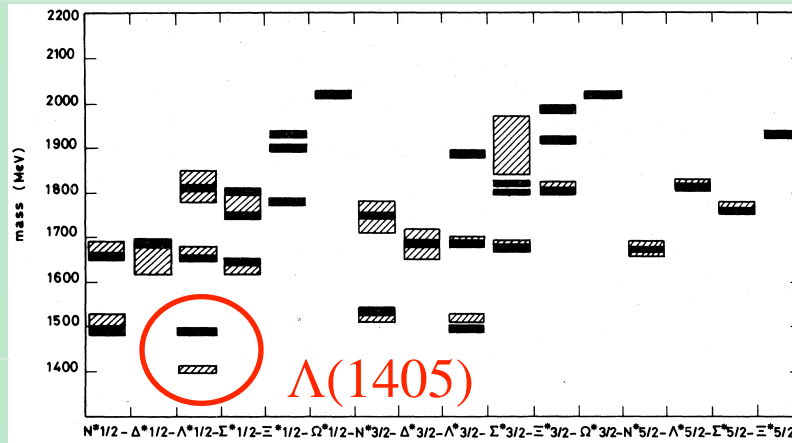
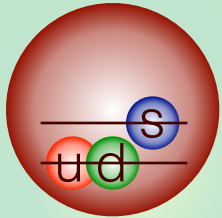
162 baryons

LIGHT UNFLAVORED (S = C = B = 0)		STRANGE (S = ±1, C = B = 0)		CHARMED, STRANGE (C = S = ±1)		c \bar{c} continued $\bar{c}c$	
$F(F^C)$	$F(F^C)$	$I(F)$	$I(F)$	$I(F)$	$I(F)$		
π^\pm	$1(0^-)$	$\pi_2(1670)$	$1(2^-)$	K^\pm	$1/2(0^-)$	D_s^\pm	$0(1^-)$
π^0	$0(0^-)$	$\phi(1680)$	$0(1^-)$	K^0	$1/2(0^-)$	$D_s^{*\pm}$	$0(2^-)$
η	$0^+(0^-)$	$\rho_2(1690)$	$1^+(3^-)$	K_S^0	$1/2(0^-)$	$D_{s1}^*(2317)^0$	$0(0^+)$
$\eta(500)$	$0^+(0^+)$	$\rho(1700)$	$1^+(1^-)$	K_L^0	$1/2(0^-)$	$D_{s1}(2460)^0$	$0(1^+)$
$\eta(770)$	$1^+(1^-)$	$\omega_2(1700)$	$1(2^+)$	$K_S^*(700)$	$1/2(0^+)$	$D_{s1}(2536)^0$	$0(1^+)$
$\omega(782)$	$0(1^-)$	$\phi(1710)$	$0^+(0^+)$	$K_1^*(1270)$	$1/2(1^+)$	$D_{s1}^*(2573)^0$	$0(2^+)$
$\eta(958)$	$0^+(0^+)$	$\phi(1760)$	$0^+(0^+)$	$K_1(1400)$	$1/2(1^+)$	$D_{s1}^*(2700)^0$	$0(1^-)$
$\eta(980)$	$0^+(0^+)$	$\phi(1835)$	$?^+(0^-)$	$K^*(1410)$	$1/2(1^-)$	$D_{s1}^*(2860)^0$	$0(1^-)$
$\omega(980)$	$0^+(0^+)$	$\phi(1835)$	$?^+(0^-)$	$K_S^*(1430)$	$1/2(0^+)$	$D_{s1}^*(3040)^0$	$0(2^+)$
$\omega(1020)$	$0(1^-)$	$\phi_2(1850)$	$0(3^-)$	$K_2^*(1430)$	$1/2(2^+)$	BOTTOM (B = ±1)	
$h_1(1170)$	$0^+(1^+)$	$\phi_2(1870)$	$0^+(2^-)$	$K_1(1650)$	$1/2(1^-)$	B^+	$1/2(0^-)$
$h_1(1235)$	$1^+(1^+)$	$\phi_2(1880)$	$1(2^-)$	$K_1(1650)$	$1/2(1^-)$	B^0	$1/2(0^-)$
$a_1(1260)$	$1^+(1^+)$	$\phi_2(1900)$	$0^+(2^+)$	$K_1(1650)$	$1/2(1^-)$	B^+/\bar{B}^0 ADMIXTURE	$1/2(1^+)$
$f_2(1285)$	$0^+(1^+)$	$\phi_2(1950)$	$0^+(2^+)$	$K_1(1650)$	$1/2(1^-)$	$B^+/\bar{B}^0/B_s^+/\bar{B}_s^0$ b-baryon ADMIXTURE	$1/2(1^+)$
$f_1(1295)$	$0^+(0^+)$	$\phi_2(1950)$	$0^+(2^+)$	$K_1(1650)$	$1/2(1^-)$	V_{cb} and V_{cb} CKM Matrix Elements	$1/2(1^+)$
$\pi(1300)$	$1(0^-)$	$\phi_2(1970)$	$1(4^+)$	$K_2^*(1780)$	$1/2(2^-)$	B^+	$1/2(1^-)$
$\omega(1320)$	$1(0^+)$	$\phi_2(1990)$	$1^+(3^-)$	$K_2^*(1820)$	$1/2(2^-)$	B_s^+	$1/2(1^-)$
$\phi(1370)$	$0^+(0^+)$	$\phi(2005)$	$1(0^-)$			B_s^0	$1/2(1^-)$
$\pi(1400)$	$1(1^-)$					B_s^+	$1/2(1^-)$
						B_s^0	$1/2(1^-)$
						B_s^+	$1/2(1^+)$
						B_s^0	$1/2(1^+)$
						B_s^+	$1/2(2^+)$
						B_s^0	$1/2(2^+)$
						B_s^+	$1/2(2^+)$
						B_s^0	$1/2(2^+)$
						B_s^+	$1/2(2^+)$
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						B_s^0	$1/2(2^+)$
						B_s^+	$1/2(2^+)$
						B_s^0	$1/2(2^+)$
						B_s^+	$1/2(2^+)$
						B_s	

$\Lambda(1405)$ and $\bar{K}N$ scattering

$\Lambda(1405)$ does not fit in standard picture \rightarrow exotic candidate

N. Isgur and G. Karl, Phys. Rev. D18, 4187 (1978)

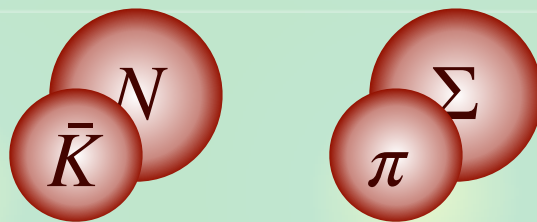


— : theory

▨ : experiment

Resonance in coupled-channel scattering

- coupling to MB states



energy ↑

— $\bar{K}N$ threshold

▭ $\Lambda(1405)$

— $\pi\Sigma$ threshold

Detailed analysis of $\bar{K}N$ - $\pi\Sigma$ scattering is necessary.

Strategy for $\bar{K}N$ interaction

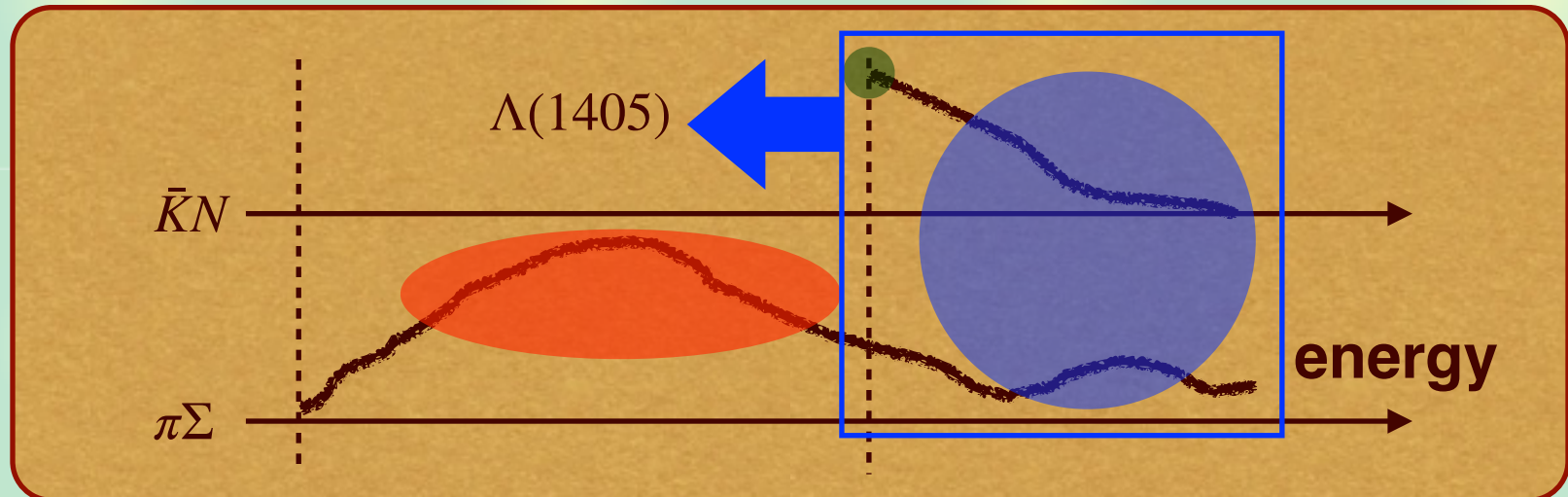
Above the $\bar{K}N$ threshold : direct constraints

- K^-p total cross sections (old data)
- $\bar{K}N$ threshold branching ratios (old data)
- K^-p scattering length (new data : SIDDHARTA)

Y. Ikeda, T. Hyodo, W. Weise, PLB 706, 63 (2011); NPA 881 98 (2012)

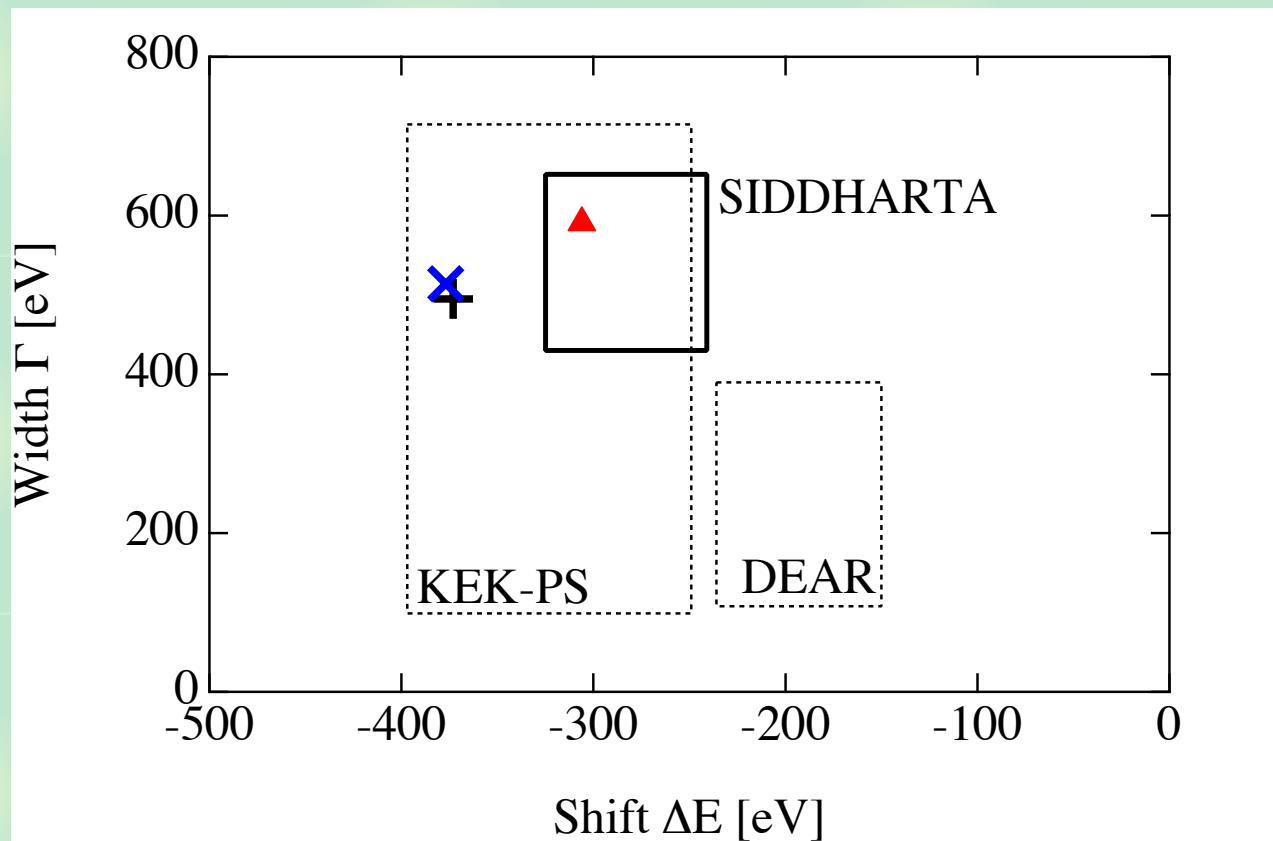
Below the $\bar{K}N$ threshold: indirect constraints

- $\pi\Sigma$ mass spectra (new data : LEPS, CLAS, HADES, ...)



Comparison with SIDDHARTA

	TW	TWB	NLO
$\chi^2/\text{d.o.f.}$	1.12	1.15	0.957



TW and **TWB** are reasonable, while best-fit requires **NLO**.

Extrapolation to complex energy: two poles

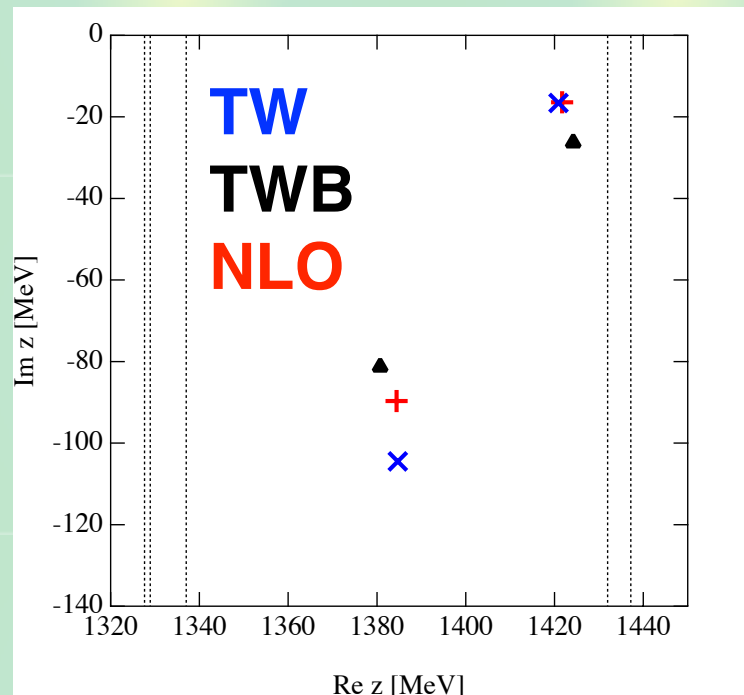
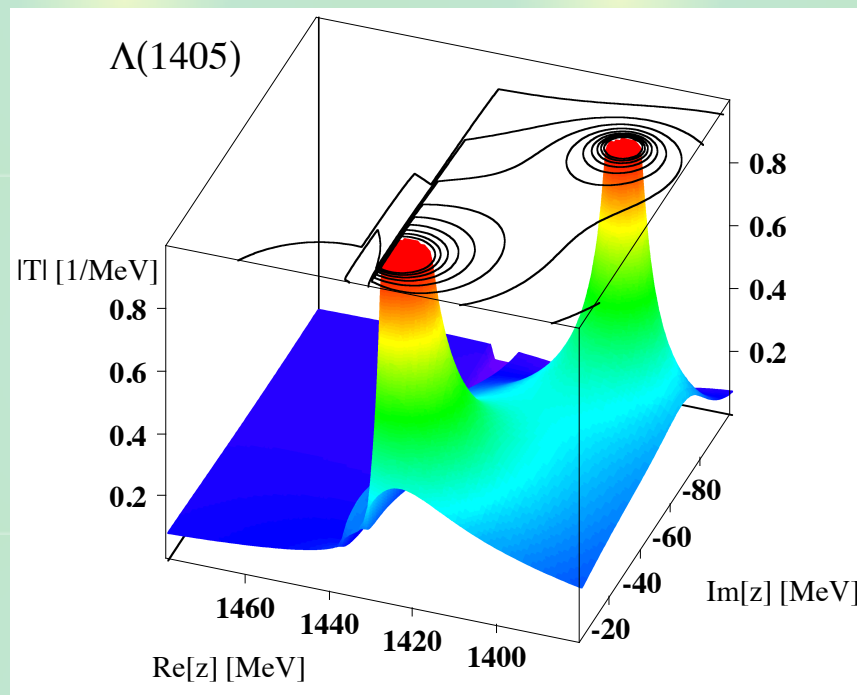
Two poles : superposition of two eigenstates

J.A. Oller, U.G. Meißner, PLB 500, 263 (2001);

D. Jido, J.A. Oller, E. Oset, A. Ramos, U.G. Meißner, NPA 723, 205 (2003);

U.G. Meißner, Symmetry 12, 981 (2020); M. Mai, arXiv: 2010.00056 [nucl-th];

T. Hyodo, M. Niyama, arXiv: 2010.07592 [hep-ph]



T. Hyodo, D. Jido, Prog. Part. Nucl. Phys. 67, 55 (2012)

NLO analysis confirms the two-pole structure.

PDG has changed

2020 update of PDG

P.A. Zyla, et al., PTEP 2020, 083C01 (2020); <http://pdg.lbl.gov/>

- Particle Listing section:

Citation: P.A. Zyla et al. (Particle Data Group), Prog. Theor. Exp. Phys. **2020**, 083C01 (2020)

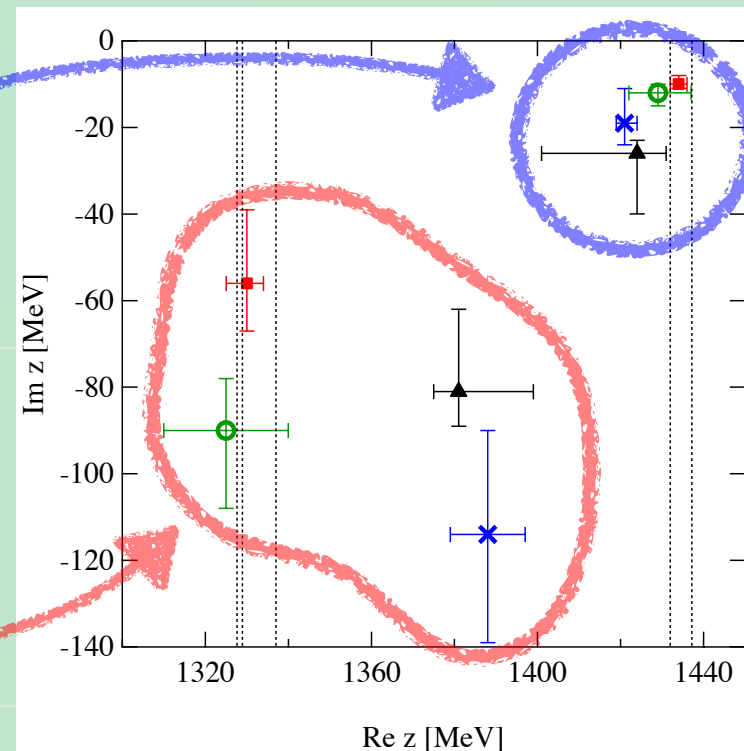
$\Lambda(1405) \ 1/2^-$

$I(J^P) = 0(\frac{1}{2}^-)$ Status: * * * *

Citation: P.A. Zyla et al. (Particle Data Group), Prog. Theor. Exp. Phys. **2020**, 083C01 (2020)

$\Lambda(1380) \ 1/2^-$

new! $J^P = \frac{1}{2}^-$ Status: * *



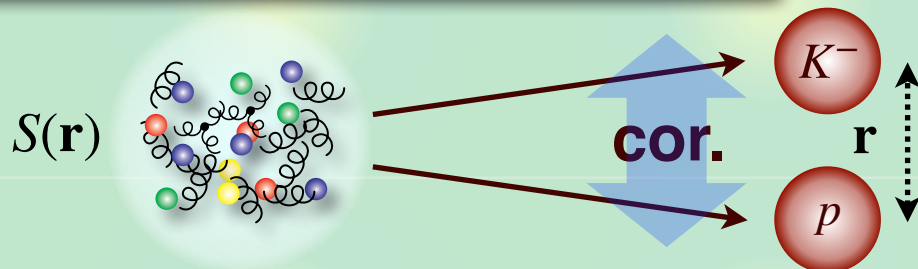
T. Hyodo, M. Niiyama, arXiv: 2010.07592 [hep-ph]

- $\Lambda(1405)$ is no longer at 1405 MeV but ~ 1420 MeV.
- Lower pole: two-star resonance $\Lambda(1380)$

K^-p correlation from high-energy collisions

Correlation function $C(q)$

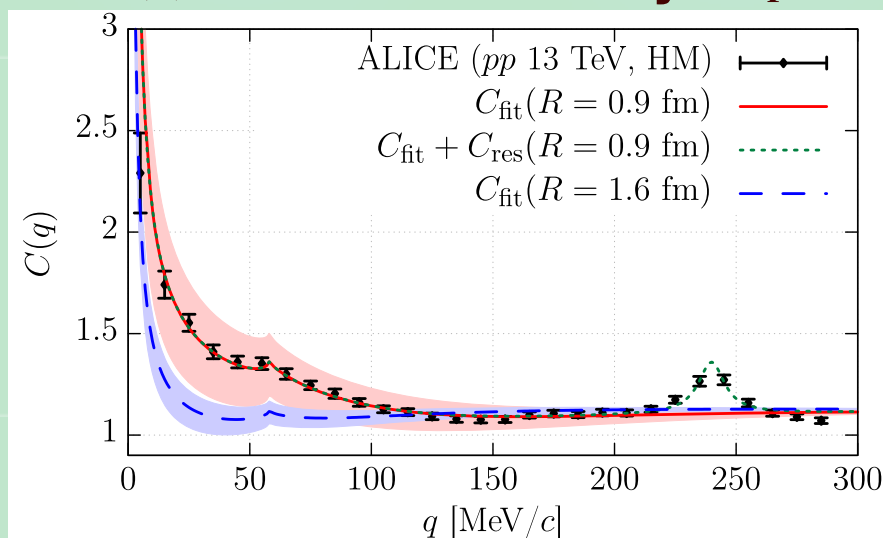
$$C(q) \simeq \int d^3\mathbf{r} S(\mathbf{r}) |\Psi_q^{(-)}(\mathbf{r})|^2$$



- wave function $\Psi_q^{(-)}(\mathbf{r})$: coupled-channel $\bar{K}N$ - $\pi\Sigma$ - $\pi\Lambda$ potential

K. Miyahara, T. Hyodo, W. Weise, PRC98, 025201 (2018)

- source function $S(\mathbf{r})$: determined by K^+p data



S. Acharya, et al., ALICE collaboration, PRL 124, 092301 (2020)

Y. Kamiya, T. Hyodo, K. Morita, A. Ohnishi, W. Weise. PRL124, 132501 (2020)

Correlation function is well reproduced.

Weak-binding relation for stable states

Compositeness X of s-wave **weakly bound** state ($R \gg R_{\text{typ}}$)

S. Weinberg, *Phys. Rev.* **137**, B672 (1965);

T. Hyodo, *Int. J. Mod. Phys. A* **28**, 1330045 (2013)

$$|d\rangle = \sqrt{X} |NN\rangle + \sqrt{1-X} |\text{others}\rangle$$

NN

continuum

deuteron

range of interaction

$$a_0 = R \left\{ \frac{2X}{1+X} + \mathcal{O}\left(\frac{R_{\text{typ}}}{R}\right) \right\}, \quad R = \frac{1}{\sqrt{2\mu B}}$$

↑
↑

scattering length
radius of state

- Deuteron is *NN* composite : $a_0 \sim R \Rightarrow X \sim 1$
- Internal structure from **observable** (a_0, B)

Problem: applicable only for stable states

Effective field theory

Low-energy scattering with near-threshold bound state

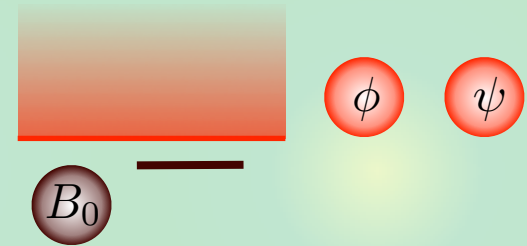
- Nonrelativistic EFT with contact interaction

D.B. Kaplan, Nucl. Phys. B494, 471 (1997)

E. Braaten, M. Kusunoki, D. Zhang, Annals Phys. 323, 1770 (2008)

$$H_{\text{free}} = \int d\mathbf{r} \left[\frac{1}{2M} \nabla \psi^\dagger \cdot \nabla \psi + \frac{1}{2m} \nabla \phi^\dagger \cdot \nabla \phi + \frac{1}{2M_0} \nabla B_0^\dagger \cdot \nabla B_0 + \omega_0 B_0^\dagger B_0 \right]$$

$$H_{\text{int}} = \int d\mathbf{r} \left[g_0 \left(B_0^\dagger \phi \psi + \psi^\dagger \phi^\dagger B_0 \right) + v_0 \psi^\dagger \phi^\dagger \phi \psi \right]$$



$$1/R = \sqrt{2\mu B}, \text{ cutoff } \Lambda \sim 1/R_{\text{typ}}$$

$$a_0 = -f(E=0) = R \left\{ \frac{2X}{1+X} + \mathcal{O}\left(\frac{R_{\text{typ}}}{R}\right) \right\} \text{ renormalization dependent}$$

renormalization independent

If $R \gg R_{\text{typ}}$, correction terms neglected: $X \leftarrow (a_0, B)$

Inclusion of decay channel

Introduce decay channel

$$H'_{\text{free}} = \int d\mathbf{r} \left[\frac{1}{2M'} \nabla \psi'^{\dagger} \cdot \nabla \psi' - \nu_{\psi} \psi'^{\dagger} \psi' + \frac{1}{2m'} \nabla \phi'^{\dagger} \cdot \nabla \phi' - \nu_{\phi} \phi'^{\dagger} \phi' \right]$$

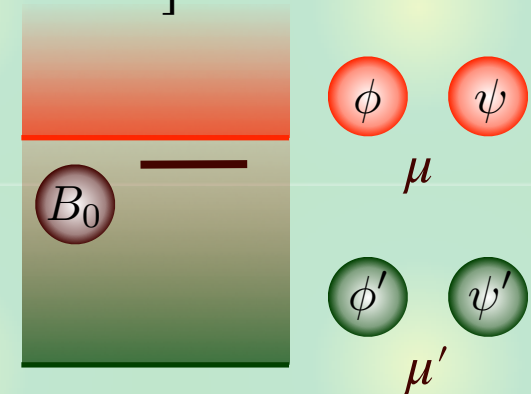
$$H'_{\text{int}} = \int d\mathbf{r} \left[g'_0 \left(B_0^{\dagger} \phi' \psi' + \psi'^{\dagger} \phi'^{\dagger} B_0 \right) + v'_0 \psi'^{\dagger} \phi'^{\dagger} \phi' \psi' + v_0^t (\psi'^{\dagger} \phi'^{\dagger} \phi' \psi' + \psi'^{\dagger} \phi'^{\dagger} \phi \psi) \right]$$

Quasi-bound state : complex eigenvalue

$$H = H_{\text{free}} + H'_{\text{free}} + H_{\text{int}} + H'_{\text{int}}$$

$$H |h\rangle = E_h |h\rangle, \quad E_h \in \mathbb{C}$$

$$\nu_{\psi} + \nu_{\phi} = \nu$$



Generalized relation : **correction** from threshold difference

$$a_0 = R \left\{ \frac{2X}{1+X} + \mathcal{O} \left(\left| \frac{R_{\text{typ}}}{R} \right| \right) + \mathcal{O} \left(\left| \frac{\ell}{R} \right|^3 \right) \right\}, \quad R = \frac{1}{\sqrt{-2\mu E_h}}, \quad \ell \equiv \frac{1}{\sqrt{2\mu\nu}}$$

Y. Kamiya, T. Hyodo, PRC93, 035203 (2016); PTEP2017, 023D02 (2017)

If $|R| \gg (R_{\text{typ}}, \ell)$, **correction terms neglected:** $X \leftarrow (a_0, E_h)$

Evaluation of compositeness

Generalized weak-binding relation

$$a_0 = R \left\{ \frac{2X}{1+X} + \mathcal{O} \left(\left| \frac{R_{\text{typ}}}{R} \right| \right) + \mathcal{O} \left(\left| \frac{\ell}{R} \right|^3 \right) \right\}, \quad R = \frac{1}{\sqrt{-2\mu E_h}}, \quad \ell \equiv \frac{1}{\sqrt{2\mu\nu}}$$

(a_0, E_h) determinations by several groups

- neglecting correction terms:

	E_h [MeV]	a_0 [fm]	$X_{\bar{K}N}$	$\tilde{X}_{\bar{K}N}$	$U/2$
Set 1 [35]	$-10 - i26$	$1.39 - i0.85$	$1.2 + i0.1$	1.0	0.3
Set 2 [36]	$-4 - i8$	$1.81 - i0.92$	$0.6 + i0.1$	0.6	0.0
Set 3 [37]	$-13 - i20$	$1.30 - i0.85$	$0.9 - i0.2$	0.9	0.1
Set 4 [38]	$2 - i10$	$1.21 - i1.47$	$0.6 + i0.0$	0.6	0.0
Set 5 [38]	$-3 - i12$	$1.52 - i1.85$	$1.0 + i0.5$	0.8	0.3

- In all cases, $X \sim 1$ with small $U/2$ (complex nature)

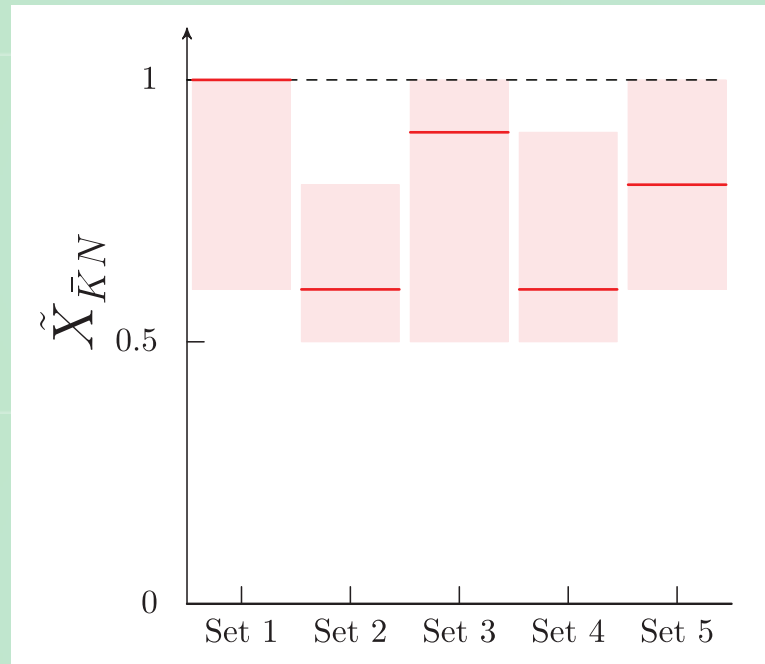
$\Lambda(1405)$: $\bar{K}N$ composite dominance \leftarrow observables

Uncertainty estimation

Estimation of correction terms: $|R| \sim 2$ fm

$$a_0 = R \left\{ \frac{2X}{1+X} + \mathcal{O}\left(\left|\frac{R_{\text{typ}}}{R}\right|\right) + \mathcal{O}\left(\left|\frac{\ell}{R}\right|^3\right) \right\}, \quad R = \frac{1}{\sqrt{-2\mu E_{QB}}}, \quad \ell \equiv \frac{1}{\sqrt{2\mu\nu}}$$


- ρ meson exchange picture: $R_{\text{typ}} \sim 0.25$ fm
- energy difference from $\pi\Sigma$: $\ell \sim 1.08$ fm



$\bar{K}N$ composite dominance holds even **with correction terms.**

Summary

 New hadrons are continuously observed.


 Pole structure of the $\Lambda(1405)$ region is now well constrained by experimental data.

“ $\Lambda(1405)$ ” \rightarrow $\Lambda(1405)$ **and** $\Lambda(1380)$

Y. Ikeda, T. Hyodo, W. Weise, PLB 706, 63 (2011); NPA 881, 98 (2012);

P.A. Zyla, *et al.* (Particle Data Group), PTEP 2020, 083C01 (2020)

T. Hyodo, M. Niiyama, arXiv: 2010.07592 [hep-ph]

 Generalized weak-binding relation shows that (higher-energy) $\Lambda(1405)$ is dominated by **molecular $\bar{K}N$** component.

Y. Kamiya, T. Hyodo, PRC93, 035203 (2016); PTEP2017, 023D02 (2017)