Size and structure of near-threshold states





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Introduction

Usual hadrons <-- quarks

Classification of hadrons

PDG2018 : http://pdg.lbl.gov/

n	1/2+ ****	A(1232)	3/2+ ****	Σ^+	1/2+ *	** =	=0	$1/2^{+}$	****	A ⁺	1/2+	****	1		LIGHT UN	IFLAVORED		STRA (S = +1, (NGE = B = 0	CHARMED, STRANG $(C = S = \pm 1)$	-	CT F(PC)
n	1/2+ ****	$\Delta(1202)$	3/2+ ***	Σ ⁰	1/2+ *	** =	_	$\frac{1}{2^+}$	****	/'c A_(2595)+	1/2	***			P(JPC)	1	$f^{C}(f^{PC})$	(, -	l(P)	(<i>I</i>)	• nd(15)	$0^{+}(0^{-}+)$
 N(1440	$1/2^+$ ****	$\Delta(1620)$	1/2 ****	Σ-	1/2+ *	** =	- -(1530)	$3/2^+$	****	$\Lambda_{-}(2625)^{+}$	3/2-	***		• π^{\pm}	$1^{-}(0^{-})$	 \(\phi\)(1680) 	0-(1)	• K±	1/2(0-)	• D _s [±] 0(0 ⁻)	 J/ψ(1S) 	0-(1)
N(1520) 3/2 ⁻ ****	$\Delta(1700)$	3/2 ****	- Σ(1385)	3/2+ **	** =	=(1620)	-/ -	*	$\Lambda_{c}(2765)^{+}$	0/2	*		• π ⁰	$1^{-}(0^{-+})$	 ρ₃(1690) 	$1^{+}(3^{})$	• K ⁰	1/2(0-)	• D _s ^{*±} 0(??)	• $\chi_{c0}(1P)$	$0^+(0^++)$
N(1535	$1/2^{-} ****$	$\Delta(1750)$	1/2+ *	$\Sigma(1480)$	*	-	=(1690)		***	A-(2880)+	$5/2^{+}$	***		• η • fs(500)	$0^+(0^+)$	• $\rho(1700)$ $2\pi(1700)$	$1^{+}(1^{})$ $1^{-}(2^{++})$	• K ⁰ _S	$1/2(0^{-})$	• $D_{s0}^*(2317)^{\pm} 0(0^{\pm})$	• $\chi_{c1}(1P)$ • $h_{c1}(1P)$	$\frac{0}{(1 + -)}$
N(1650) 1/2 ⁻ ****	$\Delta(1900)$	1/2 **	$\Sigma(1560)$	**		=(1820)	$3/2^{-}$	***	Λ ₋ (2040)+	0/2	***		 ρ(770) 	1+(1)	 f₀(1710) 	$0^{+}(0^{+}+)$	K [*] (800)	$1/2(0^+)$	• $D_{s1}(2460)^{-}$ $0(1^{+})$ • $D_{c1}(2536)^{\pm}$ $0(1^{+})$	 χ_{c2}(1P) 	$0^{+}(2^{+}+)$
N(1675) 5/2 ⁻ ****	$\Delta(1905)$	5/2 ⁺ ****	$\Sigma(1580)$	3/2- *	-	=(1950)	0/2	***	$\Sigma_{-}(2455)$	$1/2^{+}$	****		 ω(782) 	0-(1)	$\eta(1760)$	0+(0-+)	• K*(892)	1/2(1-)	• D ₅₂ (2573) 0(??)	 η_c(2S) 	0+(0 - +)
N(1680	$5/2^+$ ****	$\Delta(1910)$	1/2+ ****	$\Sigma(1620)$	1/2 *		=(2030)	$> \frac{5}{2}$?	***	$\Sigma_{c}(2520)$	3/2+	***		 η'(958) f (990) 	$0^+(0^{-+})$	 π(1800) f (1810) 	$1^{-}(0^{-+})$	 K₁(1270) 	$1/2(1^+)$	• $D_{s1}^*(2700)^{\pm} 0(1^{-})$	 ψ(2S) ψ(3770) 	$0^{-}(1^{-})$
N(1685) *	$\Delta(1920)$	3/2+ ***	$\Sigma(1660)$	1/2+ **	* =	=(2120)	- 2	*	$\Sigma_{1}(2800)$	5/2	***		• a ₀ (980)	$1^{-}(0^{++})$	X(1835)	$\frac{1}{2}(2^{-}+)$	• $K_1(1400)$ • $K^*(1410)$	$\frac{1}{2(1^{-})}$	$D_{sJ}^*(2860)^{\pm} = 0(?^{\pm})$	X(3823)	??(??-)
N(1700) 3/2 ⁻ ***	$\Delta(1930)$	5/2 ***	$\Sigma(1670)$	3/2 **	** =	=(2250)		**	=+	$1/2^{+}$	***		 φ(1020) 	0-(1)	X(1840)	??(???)	 K[*]₀(1430) 	1/2(0+)	$D_{s,J}(3040) = 0(:)$	• X(3872)	0+(1++)
N(1710) 1/2 ⁺ ***	$\Delta(1940)$	3/2 **	$\Sigma(1690)$	-/- *>		=(2370)		**	-c =0	1/2+	***		 h1(1170) h(1005) 	$0^{-}(1^{+-})$	 φ₃(1850) 	0-(3)	• K [*] ₂ (1430)	1/2(2+)	BOTTOM $(B = \pm 1)$	X(3900) [±] X(3900) [±] X(3000) [€]	(1^+)
N(1720) 3/2 ⁺ ****	$\Delta(1950)$	7/2+ ****	$\Sigma(1730)$	3/2+ *		=(2500)		*	$\frac{-c}{='+}$	1/2+	***		• $D_1(1235)$ • $a_1(1260)$	$1^{-1}(1^{+})$ $1^{-}(1^{+})$	$\eta_2(1870)$ • $\pi_2(1880)$	$1^{-}(2^{-+})$	K(1460)	$1/2(0^{-})$	• B [±] 1/2(0 ⁻	- x (3900)*	$(1^{+})^{+}$
N(1860	$5/2^+ **$	$\Delta(2000)$	5/2+ **	$\Sigma(1750)$	1/2 *	* -	=(2000)			-c =0	1/2	***		 f₂(1270) 	$0^{+}(2^{+}+)$	ρ(1900)	1+(1)	K(1630)	$\frac{1}{2(2)}$ $\frac{1}{2(?)}$	• B ⁰ 1/2(0	$() \bullet \chi_{c2}(2P)$	$0^{+}(2^{+})$
N(1875) 3/2 ***	$\Delta(2150)$	1/2 *	$\Sigma(1770)$	$\frac{1}{2^{+}} *$	S	2-	$3/2^{+}$	****	$= \frac{1}{C}$	2/2+	***		 f₁(1285) 	$0^{+}(1^{++})$	f ₂ (1910)	0+(2++)	$K_1(1650)$	$1/2(1^+)$	B [±] /B ⁰ ADMIXTURE	X(3940)	?!(?!!)
N(1880) 1/2 ⁺ **	$\Delta(2200)$	7/2- *	$\Sigma(1775)$	5/2 **	** 5	$2(2250)^{-1}$		***	$=_{C}(2045)$	3/2 -	***		 η(1295) π(1300) 	$0^+(0^+)$ $1^-(0^+)$	• f ₂ (1950)	$0^+(2^++)$ $1^+(3^-+)$	• K*(1680)	$1/2(1^{-})$	■ B [±] /B ⁰ /B ⁰ /B ⁰ /b-baryon ADMIXTURE	X(4020)-	- ((?)) = -(1)
N(1895	$1/2^{-} **$	$\Delta(2300)$	9/2+ **	$\Sigma(1840)$	3/2+ *	6	$2(2380)^{-1}$		**	$=_{c}(2790)$	2/2-	***		• a)(1320)	$1^{-}(2^{+}+)$	• f ₂ (2010)	$0^{+}(2^{+}+)$	• K ₂ (170) • K [±] (1780)	$\frac{1}{2(2^{-})}$	V _{cb} and V _{ub} CKM Ma	X(4050) [±]	* ?(? [?])
N(1900) 3/2 ⁺ ***	$\Delta(2350)$	5/2 *	$\Sigma(1880)$	1/2+ *	S	$2(2470)^{-1}$		**	$=_{C}(2015)$	3/2	*	_	• f ₀ (1370)	0+(0++)	f ₀ (2020)	0+(0++)	• K ₂ (1820)	$1/2(2^{-})$	• B* 1/2(1) X(4140)	0 ⁺ (??+)
N(1990) 7/2 ⁺ **	$\Delta(2390)$	7/2+ *	$\Sigma(1900)$	1/27 *					$=_{C}(2950)$		***		$h_1(1380)$	$?^{-}(1^{+-})$	• a4(2040)	$1^{-}(4^{++})$	K(1830)	1/2(0-)	• B1(5721)+ 1/2(1	$\psi(4160)$	$\frac{0^{-}(1^{-})}{2^{2}(2^{2})}$
N(2000) 5/2 ⁺ **	$\Delta(2400)$	9/2 **	Σ(1915)	5/2+ *	**				$=_{C}(2900)$ = (20FF)		***		 η(1400) η(1405) 	$0^{+}(0^{-}+)$	$\pi_2(2100)$	$1^{-}(2^{-+})$	$K_0^*(1950)$	$1/2(0^+)$ $1/2(2^+)$	• $B_1(5/21)^0$ 1/2(1 $B^*(5732)$ 2(7?)) X(4230)	?(1)
N(2040	∬ 3/2 ⁺ ∗	$\Delta(2420)$	11/2+ ****	Σ(1940)	3/2+ *					$=_{C}(3099)$		***		• f1(1420)	0 ⁺ (1 ⁺ +)	f ₀ (2100)	0+(0++)	• K*(2045)	$1/2(2^{+})$ $1/2(4^{+})$	$\bullet B_{2}^{*}(5747)^{+} 1/2(2^{-})^{+}$	-) X(4240)±	? [?] (g [_])
N(2060) 5/2 **	$\Delta(2750)$	13/2- **	Σ(1940)	3/2 **	*				$=_{C}(3000)$		*		 ω(1420) 	$0^{-}(1^{-})$	$f_2(2150)$	$0^+(2^{++})$	$K_2(2250)$	1/2(2-)	• B ₂ [*] (5747) ⁰ 1/2(2 ⁻	$X(4250)^{\pm}$	[±] ?(? [!])
N(2100	$1/2^+ *$	$\Delta(2950)$	15/2+ **	$\Sigma(2000)$	$\frac{1}{2} *$					$=_{C}(3123)$	1/2+	***		$r_2(1430)$ • $a_0(1450)$	$1^{-}(0^{+}+)$	ρ(2150) • φ(2170)	$1^{+}(1^{-})$ $0^{-}(1^{-})$	K ₃ (2320)	1/2(3+)	• B(5970) ⁺ ?(??)	• A(4260) X(4350)	$0^{+}(2^{?+})$
N(2120) 3/2 ⁻ **	()	,	Σ(2030)	7/2+ **	**				2 ² 2 ²	2/2+	***		 ρ(1450) 	1+(1)	f ₀ (2200)	0+(0++)	K ₅ (2380)	$1/2(5^{-})$	• B(5970) ^o ?(? [:])	• X(4360)	??(1)
N(2190) 7/2 ⁻ ****	Λ	1/2+ ****	Σ(2070)	5/2+ *					32 _C (2110)°	3/2 '	-111-		 η(1475) 	$0^+(0^{-+})$	f _f (2220)	0+(2++)	$r 4 \frac{44(2500)}{K(3100)}$??(???)	BOTTOM, STRANGE	 ψ(4415) 	0-(1)
N(2220	ý 9/2 ⁺ ****	<i>A</i> (1405)	1/2 ****	Σ(2080)	3/2+ **					=+		*		 • f₀(1500) € (1510) 	$0^+(0^++)$ $0^+(1^++)$	$\eta(2225)$	$0^+(0^-+)$ $1^+(3^)$	CHAR		$(B = \pm 1, S = \pm 1)$	• X(4430)- • X(4660)	(1') $7^{?}(1)$
N(2250	ý 9/2 ⁻ ****	A(1520)	3/2" ****	Σ(2100)	7/2 *					- <i>cc</i>				• f'_(1525)	$0^{+}(2^{++})$	• f ₂ (2300)	$0^{+}(2^{+}+)$	(C =	±1)	• $B_{\tilde{s}}^{*}$ 0(0 ⁻)	- //(1000)	. (±)
N(2300) 1/2 ⁺ **	A(1600)	1/2+ ***	Σ(2250)	, *>	*				<u>∧</u> 0	$1/2^{+}$	***		$f_2(1565)$	0+(2++)	f ₄ (2300)	0+(4++)	• D [±]	1/2(0-)	• B _{s1} (5830) ⁰ 0(1 ⁺)	(10)	bb
N(2570) 5/2 **	A(1670)	1/2 ****	Σ(2455)	**					$\Lambda_{\mu}(5912)^{0}$	1/2-	***		$\rho(1570)$ b. (1505)	$1^+(1^{})$	$f_0(2330)$	$0^+(0^{++})$	• D ⁰	1/2(0-)	• $B_{s2}^{*}(5840)^{0}$ 0(2 ⁺)	η _b (1S) • Υ(1S)	$0^{-}(0^{-})$
N(2600) 11/2 ⁻ ***	A(1690)	3/2 ****	$\Sigma(2620)$	**					$\Lambda_{\mu}(5920)^{0}$	3/2-	***		$\bullet \pi_1(1595)$	$1^{-}(1^{-+})$	 ρ₂(2340) ρ₅(2350) 	$1^{+}(5^{})$	 D*(2007)^o D*(2010)[±] 	$1/2(1^{-})$ $1/2(1^{-})$	$B_{sJ}^{*}(5850)$?(?:)	• χ _{b0} (1P)	0+(0++)
N(2700) 13/2 ⁺ **	A(1710)	1/2+ *	Σ(3000)	*					Σ.	$1/2^+$	***		a1(1640)	$1^{-}(1^{++})$	a ₆ (2450)	1-(6++)	 D[*]₀(2400)⁰ 	1/2(0+)	BOTTOM, CHARMEI	• $\chi_{b1}(1P)$	$0^+(1^+)$
· ·	· ·	A(1800)	1/2 ***	Σ(3170)	*					Σ^*	3/2+	***		$f_2(1640)$	$0^+(2^++)$	f ₆ (2510)	0+(6++)	$D_0^*(2400)^{\pm}$	1/2(0+)	$(B = C = \pm 1)$	$- h_b(1P)$	(1 +)
		A(1810)	1/2+ ***	. ,						=0 =-	1/2+	***		 η₂(1645) ω(1650) 	$0^{-}(2^{-})$ $0^{-}(1^{-})$			• D ₁ (2420) ⁰	$1/2(1^+)$	$B_c(2S)^{\pm} = \frac{0(0^{-})}{7?(7?)}$	$\eta_b(2S)$	$0^{+}(0^{-}+)$
		A(1820)	5/2+ ****							$=b^{\prime}-b$	1/2+	***		 ω₃(1670) 	0-(3)			$D_1(2420)^{-1}$ $D_1(2430)^{0}$	$\frac{1}{2}(1^{+})$	5((20)) . (.	• 7(2S)	0-(1)
		A(1830)	5/2 ****							$=_{b}(3933)$ = (E04E)0	2/2+	***		 π₂(1670) 	$1^{-}(2^{-+})$			$D_2^*(2460)^0$	1/2(2+)		• T(1D)	$0^{-}(2^{-})$
		A(1890)	3/2+ ****							$=b(5945)^{-}$	- 3/2 ·	***						$D_2^{-}(2460)^{\pm}$	1/2(2+)		• XB0(2P)	$0^{+}(1^{+})$
		A(2000)	*							$\Xi_{b}(5955)$	3/2 *	***						D(2550) ⁰	$1/2(0^{-})$		$h_b(2P)$??(1+-)
		A(2020)	7/2+ *							³² b	1/2 .	-111-						D(2000) D*(2640) [±]	1/2(?) 1/2(??)		• χ _{b2} (2P)	$0^+(2^++)$
		A(2050)	3/2 *															D(2750)	1/2(??)		• 1(35) • YM(3P)	0(1) $0^{+}(1^{+})$
		Л(2100)	7/2- ****																		• T(4S)	0-(1)
		A(2110)	5/2+ ***		_																X(10610)	$^{\pm} 1^{+}(1^{+})$
		A(2325)	3/2 *	_	. 1	51	ן ר	5	K) /	hn	0				71	N •	\mathbf{n}	60	nc		X(10610) X(10650)	$1^{\vee} 1^{+}(1^{+})$
		A(2350)	9/2+ ***		~	JL	JN	a	IV		3			\sim	∠	VI	ILC	DC	113)	• 7(10860)	$0^{-}(1^{-})$
		<i>I</i> (2585)	**														_				 <i>γ</i>(11020)) 0-(1)

Can one construct a hadron from hadrons?

Introduction

Hadron clusters

Hadrons near an s-wave two-body threshold



"hadronic molecules" (various flavors, baryon numbers, ...)

Introduction

Two-body universal physics

Near-threshold s-wave state: universal physics

E. Braaten, H.-W. Hammer, Phys. Rept. 428, 259 (2006); P. Naidon, S. Endo, Rept. Prog. Phys. 80, 056001 (2017)

- scattering length $|a| \gg$ interaction range R_0

- size of (quasi-)bound state $\sim |a|$: loosely bound
- relation with eigenenergy E

$$a(E) \sim \frac{i}{k} = \frac{i}{\sqrt{2\mu E}}$$

Examples: d, $\Lambda(1405)$, ⁴He dimer

strong

vdW

	<i>NN</i> [fm]	<i>ĒN</i> [fm]	4 He [<i>a</i> ₀]
a(E)	4.3	1.2-0.8i	178
a _{emp}	5.1	1.4-0.9i	189
R_0	1.4	0.4	10



⁴He

Wave function

Why is a weakly bound s-wave state spatially large?

- Radial Schrödinger equation

$$-\frac{\hbar^2}{2\mu}\frac{d^2}{dr^2}u_0(r) + V(r)u_0(r) = Eu_0(r), \quad \psi_0(r) = Y_0^0\frac{u_0(r)}{r}$$

- at large distance (V(r) = 0) with zero energy (E = 0)

 $u_0(r) = C(r-a), \quad (r > R_0)$

- scattering length a : intercept of $u_0(r)$
- bound state with $B = 0 \Rightarrow |a| = \infty$

Wave function is not normalizable

$$\int d^3r |\psi_0(r)|^2 = \int_0^\infty dr |u_0(r)|^2 = \infty$$

B = 0 state is not a bound state (zero-energy resonance)



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Consequences

Mean squared radius

$$\langle r^2 \rangle = \int d^3 r \ r^2 |\psi_0(r)|^2 = \int_0^\infty dr \ r^2 |u_0(r)|^2 = \infty$$

-> size of B = 0 state is infinitely large

Compositeness *X* (weight of the composite component)

T. Hyodo, Phys. Rev. C 90, 055208 (2014)

$$\Psi = \begin{pmatrix} \tilde{\psi}_0(p) \\ c \\ \vdots \end{pmatrix} \qquad X = \int \frac{d^3 p}{(2\pi)^3} |\tilde{\psi}_0(p)|^2 = \int d^3 r |\psi_0(r)|^2 \quad \text{infinite}$$
$$Z = |c|^2 + \cdots \quad \text{finite}$$
$$X + Z = 1$$

-> B = 0 state is completely composite (X = 1, Z = 0)

Weakly bound state ($B \neq 0$, except for fine tuning)

- large spatial size and composite dominance

p-wave state

What about p-wave states?

- Radial Schrödinger equation

$$-\frac{\hbar^2}{2\mu}\frac{d^2}{dr^2}u_1(r) + V(r)u_1(r) + \frac{\hbar^2}{\mu r^2}u_1(r) = Eu_1(r), \quad \psi_1(\mathbf{r}) = Y_1^m(\Omega)\frac{u_1(r)}{r}$$

- at large distance (V(r) = 0) with zero energy (E = 0)

$$u_1(r) = Cr^s, \quad s = 2, -1$$

- bound state with B = 0

$$u_1(r) = \frac{C}{r}, \quad (r > R_0)$$

Wave function is normalizable

$$\int d^3r \, |\psi_1(\mathbf{r})|^2 = \int_0^\infty dr \, |u_1(r)|^2 < \infty$$

B = 0 state is a bound state



Spatial size (p-wave)

Consequences (p-wave)

Mean squared radius

$$\langle r^2 \rangle = \int_0^\infty dr \ r^2 |u_1(r)|^2 = A_{\text{in}} + |C|^2 \int_{R_0}^\infty dr \ 1 = \infty \quad \leftarrow u_1(r) = \frac{C}{r}$$

-> size of B = 0 state is infinitely large

Compositeness *X*

T. Hyodo, Phys. Rev. C 90, 055208 (2014)

$$\Psi = \begin{pmatrix} \tilde{\psi}_1(\mathbf{p}) \\ c \\ \vdots \end{pmatrix} \qquad X = \int \frac{d^3 p}{(2\pi)^3} |\tilde{\psi}_1(\mathbf{p})|^2 = \int d^3 r |\psi_1(\mathbf{r})|^2 \quad \text{finite}$$
$$Z = |c|^2 + \cdots \quad \text{finite}$$
$$X + Z = 1$$

-> B = 0 can have any structure (0 < X < 1)

Weakly bound p-wave state ($B \neq 0$, except for fine tuning)

- large spatial size?

Spatial size (*t*-wave)

Higher partial waves

Wave function of a B = 0 state with angular momentum ℓ

$$u_{\ell}(r) = \frac{C}{r^{\ell}} \quad (r > R_0)$$

- Mean squared radius

$$\langle r^2 \rangle = \int_0^\infty dr \ r^2 |u_\ell(r)|^2 = A_{\rm in} + |C|^2 \int_{R_0}^\infty dr \ r^{2-2\ell} = \infty \quad \text{if} \quad \ell \le 1$$

-> diverges only for s- and p-waves

Generalized radius

$$\sqrt[n]{\langle r^n \rangle} = \sqrt[n]{\int} d^3r \ r^n |\psi(r)|^2 = \infty \quad \text{if} \quad n - 2\ell \ge 0$$

- s-wave: radius diverges for all $n \ge 0$ <— universality
- p-wave: radius diverges for $n \ge 2$
- ℓ -th wave: radius diverges for $n \ge 2\ell$

Examples

example: square well potential

Square well potential

$$V(r) = \begin{cases} -V_0 & 0 \le r \le b\\ 0 & b < r \end{cases}$$

- s-wave

$$\frac{\langle r^2 \rangle}{2} = \left[\frac{b}{2} - \frac{\sin(2kb)}{4k} + \frac{\sin^2(kb)}{2\kappa} \right]^{-1} \left[\frac{1}{k^3} \left(\frac{(kb)^3}{6} + \frac{1 - 2(kb)^2}{8} \sin(2kb) - \frac{kb}{4} \cos(2kb) \right) + \frac{\sin^2(kb)}{2\kappa^3} \left[(\kappa b)^2 + \kappa b + \frac{1}{2} \right] \right]$$

$$k = \frac{\sqrt{2\mu(V_0 - B)}}{\hbar}, \quad \kappa = \frac{\sqrt{2\mu B}}{\hbar}$$

- p-wave

$$\langle r^{2} \rangle = \left[\frac{b}{2} + \frac{\sin(2kb)}{4k} - \frac{\sin^{2}(kb)}{k^{2}b} + \frac{\kappa \left(\sin(kb) - kb \cos(kb)\right)^{2}}{2k^{2} \left(1 + \kappa b\right)^{2}} \left(1 + \frac{2}{\kappa b}\right) \right]^{-1} \\ \times \left[\frac{1}{k^{3}} \left(\frac{3kb + (kb)^{3}}{6} + \frac{-5 + 2(kb)^{2}}{8} \sin(2kb) + \frac{3kb}{4} \cos(2kb) \right) \right. \\ \left. + \frac{\left(\sin(kb) - kb \cos(kb)\right)^{2}}{2\kappa k^{2} \left(1 + \kappa b\right)^{2}} \left[(\kappa b)^{2} + 3\kappa b + \frac{5}{2} \right] \right]$$

Examples

Demonstration

Root mean squared radius $\sqrt{\langle r^2 \rangle}$ **v.s.** $\kappa = \sqrt{2\mu B}/\hbar$



Both radii diverge in the weak binding limit ($\kappa \rightarrow 0$). Dependence on *b* (well width) seems different.

Examples

Weak-binding behavior

Behavior near the weak-binding limit

- s-wave

$$\langle r^2 \rangle = \frac{1}{2\kappa^2} + \mathcal{O}(\kappa^{-1})$$

independent of b (well width)
<- universality</pre>

- p-wave

$$\langle r^2 \rangle = \frac{5b}{6} \frac{1}{\kappa} + \mathcal{O}(\kappa^0)$$

depends on *b* (well width) non-universal divergence



Summary

Size and structure of B = 0 states

	$\langle r^2 \rangle$	compositeness	$\int d^3r \psi ^2$
s-wave	∞ (universal)	X = 1	∞
p-wave	∞ (non-universal)	0 < X < 1	finite

Implication: large mean squared radius of nearthreshold ($B \neq 0$) p-wave bound states



What about resonances?

T. Hyodo, in preparation