

$\Lambda(1405)$ as a Feshbach resonance



Tetsuo Hyodo

Yukawa Institute for Theoretical Physics, Kyoto Univ.

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Introduction

- Clustering in hadron physics / resonances



Current status of $\Lambda(1405)$

- Analysis of $\bar{K}N$ scattering

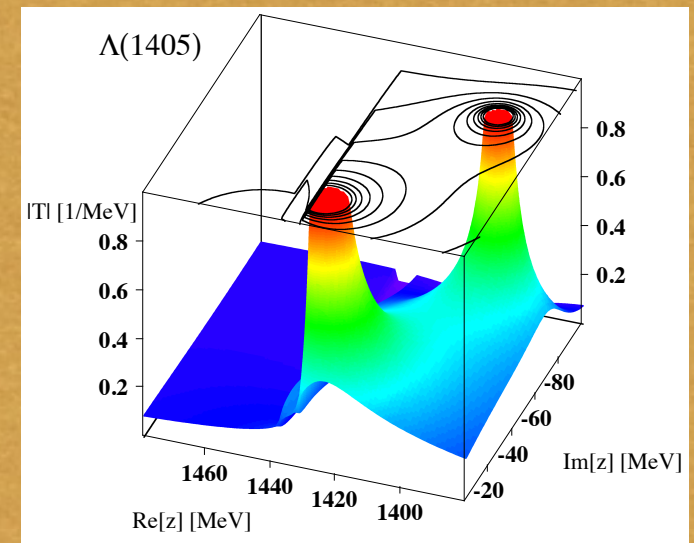


Two-pole structure

- Interpretation



Summary

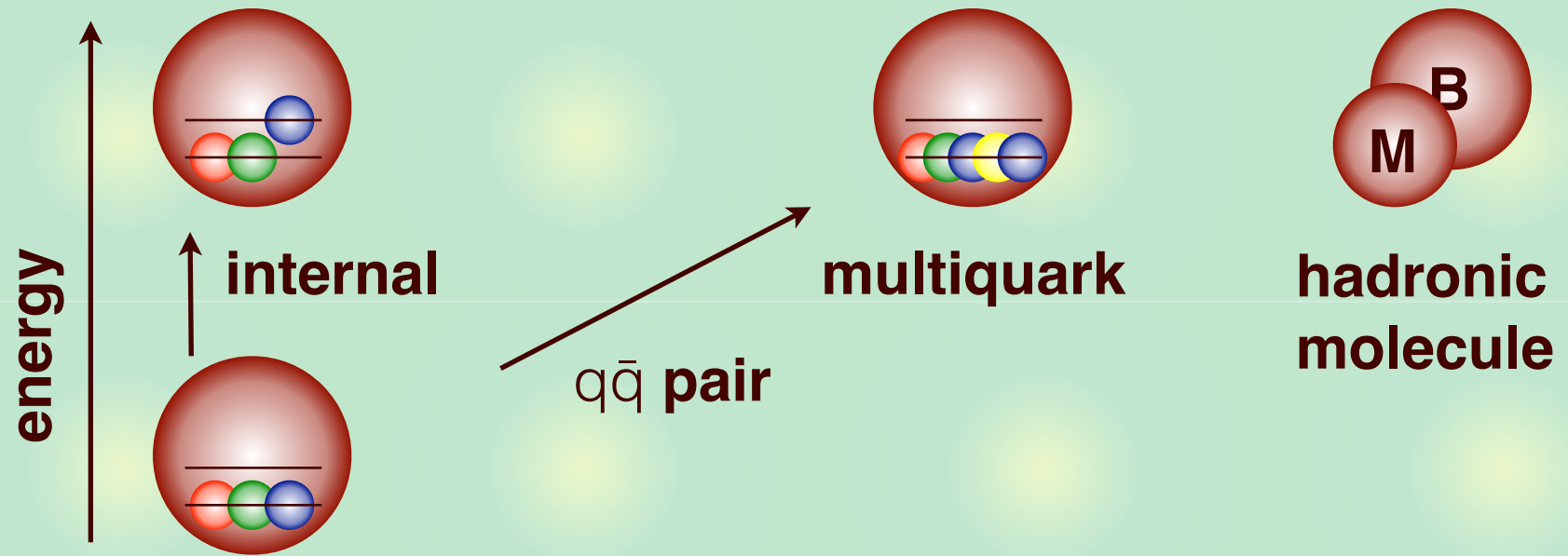


Excitation of hadrons

Excitation mechanisms

Standard (quark model)

Exotic excitation



Exotic structure : excitation inherent in QCD ($q\bar{q}$ pair creation), different from standard (shell-like) excitation

- Verification? → compositeness (poster by Kamiya)
- Are they **stable** particles?

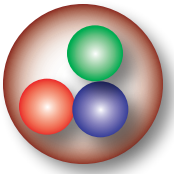
Unstable states via strong interaction

Many hadron states

PDG2018 : <http://pdg.lbl.gov/>

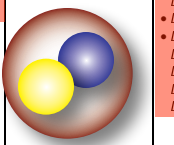
p	$1/2^+$ ****	$\Delta(1232)$	$3/2^+$ ****	Σ^+	$1/2^+$ ****	Ξ^0	$1/2^+$ ****	Λ_c^+	$1/2^+$ ****
n	$1/2^+$ ****	$\Delta(1600)$	$3/2^+$ ***	Σ^0	$1/2^+$ ****	Ξ^-	$1/2^+$ ****	$\Lambda_c(2595)^+$	$1/2^-$ ***
$N(1440)$	$1/2^+$ ****	$\Delta(1620)$	$1/2^-$ ****	Σ^-	$1/2^+$ ****	$\Xi(1530)$	$3/2^+$ ****	$\Lambda_c(2625)^+$	$3/2^-$ ***
$N(1520)$	$3/2^-$ ****	$\Delta(1700)$	$3/2^-$ ****	$\Sigma(1385)$	$3/2^+$ ****	$\Xi(1620)$	***	$\Lambda_c(2765)^+$	*
$N(1535)$	$1/2^-$ ****	$\Delta(1750)$	$1/2^+$ *	$\Sigma(1480)$	*	$\Xi(1690)$	***	$\Lambda_c(2880)^+$	$5/2^+$ ***
$N(1650)$	$1/2^-$ ****	$\Delta(1900)$	$1/2^-$ **	$\Sigma(1560)$	**	$\Xi(1820)$	$3/2^-$ ***	$\Lambda_c(2940)^+$	***
$N(1675)$	$5/2^-$ ****	$\Delta(1905)$	$5/2^+$ ****	$\Sigma(1580)$	$3/2^-$ **	$\Xi(1950)$	***	$\Sigma_c(2455)$	$1/2^+$ ****
$N(1680)$	$5/2^+$ ****	$\Delta(1910)$	$1/2^+$ ****	$\Sigma(1620)$	$1/2^-$ *	$\Xi(2030)$	$\geq 5/2^?$ ***	$\Sigma_c(2520)$	$3/2^+$ ****
$N(1685)$	*	$\Delta(1920)$	$3/2^+$ ***	$\Sigma(1660)$	$1/2^+$ ***	$\Xi(2120)$	*	$\Sigma_c(2800)$	***
$N(1700)$	$3/2^-$ ***	$\Delta(1930)$	$5/2^-$ ***	$\Sigma(1670)$	$3/2^-$ ****	$\Xi(2250)$	**	Ξ_c	$1/2^+$ ***
$N(1710)$	$1/2^+$ ***	$\Delta(1940)$	$3/2^-$ **	$\Sigma(1690)$	**	$\Xi(2370)$	**	Ξ_c	$1/2^+$ ***
$N(1720)$	$3/2^+$ ****	$\Delta(1950)$	$7/2^+$ ****	$\Sigma(1730)$	$3/2^+$ **	$\Xi(2500)$	*	Ξ_c	$1/2^+$ ***
$N(1860)$	$5/2^+$ **	$\Delta(2000)$	$5/2^+$ **	$\Sigma(1750)$	$1/2^-$ ***			Ξ_c	$1/2^+$ ***
$N(1875)$	$3/2^-$ ***	$\Delta(2150)$	$1/2^-$ *	$\Sigma(1770)$	$1/2^+$ **	Ω^-	$3/2^+$ ****	Ξ_c	$1/2^+$ ***
$N(1880)$	$1/2^+$ **	$\Delta(2200)$	$7/2^-$ *	$\Sigma(1775)$	$5/2^-$ ****	$\Omega(2250)$	***	Ξ_c	$3/2^+$ ****
$N(1895)$	$1/2^-$ **	$\Delta(2300)$	$9/2^+$ **	$\Sigma(1840)$	$3/2^+$ **	$\Omega(2380)^-$	**	Ξ_c	$1/2^-$ ***
$N(1900)$	$3/2^+$ ***	$\Delta(2350)$	$5/2^-$ **	$\Sigma(1880)$	$1/2^+$ **	$\Omega(2470)^-$	**	Ξ_c	$3/2^-$ ****
$N(1990)$	$7/2^+$ **	$\Delta(2390)$	$7/2^+$ *	$\Sigma(1900)$	$1/2^-$ **			Ξ_c	***
$N(2000)$	$5/2^+$ **	$\Delta(2400)$	$9/2^-$ **	$\Sigma(1915)$	$5/2^+$ ****			Ξ_c	***
$N(2040)$	$3/2^+$ *	$\Delta(2420)$	$11/2^+$ ****	$\Sigma(1940)$	$3/2^+$ **			Ξ_c	***
$N(2060)$	$5/2^-$ **	$\Delta(2750)$	$13/2^-$ **	$\Sigma(1940)$	$3/2^-$ ***			Ξ_c	***
$N(2100)$	$1/2^+$ *	$\Delta(2950)$	$15/2^+$ **	$\Sigma(2000)$	$1/2^-$ **			Ξ_c	***
$N(2120)$	$3/2^-$ **			$\Sigma(2030)$	$7/2^+$ ****			Ω_c^0	$1/2^+$ ***
$N(2190)$	$7/2^-$ ****	Λ	$1/2^+$ ****	$\Sigma(2070)$	$5/2^+$ **			$\Omega_c(2770)^0$	$3/2^+$ ***
$N(2220)$	$9/2^+$ ****	$\Lambda(1405)$	$1/2^-$ ****	$\Sigma(2080)$	$3/2^+$ **			Ξ_{cc}^+	*
$N(2250)$	$9/2^-$ ****	$\Lambda(1520)$	$3/2^-$ ****	$\Sigma(2100)$	$7/2^-$ **			Λ_b^0	$1/2^+$ ***
$N(2300)$	$1/2^+$ **	$\Lambda(1600)$	$1/2^+$ ***	$\Sigma(2250)$	***			$\Lambda_b(5912)^0$	$1/2^-$ ***
$N(2570)$	$5/2^-$ **	$\Lambda(1670)$	$1/2^-$ ****	$\Sigma(2455)$	**			$\Lambda_b(5920)^0$	$3/2^-$ ***
$N(2600)$	$11/2^-$ ***	$\Lambda(1690)$	$3/2^-$ ****	$\Sigma(2620)$	**			Σ_b	$1/2^+$ ***
$N(2700)$	$13/2^+$ **	$\Lambda(1710)$	$1/2^+$ *	$\Sigma(3000)$	*			Σ_b^+	$3/2^+$ ****
		$\Lambda(1800)$	$1/2^-$ ***	$\Sigma(3170)$	*			Ξ_b^+ , Ξ_b^-	$1/2^+$ ***
		$\Lambda(1810)$	$1/2^+$ ***					Ξ_b^0 , Ξ_b^-	$1/2^+$ ***
		$\Lambda(1820)$	$5/2^+$ ****					Ξ_b^+	$3/2^+$ ****
		$\Lambda(1830)$	$5/2^-$ ****					Ξ_b^0	$3/2^+$ ****
		$\Lambda(1890)$	$3/2^+$ ****					Ξ_b^+	$3/2^+$ ****
		$\Lambda(2000)$	*					Ω_b	$1/2^+$ ***
		$\Lambda(2020)$	$7/2^+$ *						
		$\Lambda(2050)$	$3/2^-$ *						
		$\Lambda(2100)$	$7/2^-$ ****						
		$\Lambda(2110)$	$5/2^+$ ***						
		$\Lambda(2325)$	$3/2^-$ *						
		$\Lambda(2350)$	$9/2^+$ ***						
		$\Lambda(2585)$	**						

$\Lambda(1405)$



~ 150 baryons

LIGHT UNFLAVORED (S = C = B = 0)		STRANGE (S = ±1, C = B = 0)		CHARMED, STRANGE (C = S = ±1)	$c\bar{c}$ $F_1(F_2)$
$F_1(F_2)$	$F_1(F_2)$	$F_1(F_2)$	$F_1(F_2)$	$F_1(F_2)$	$F_1(F_2)$
π^+	$1(0^-)$	$\rho(1680)$	$0^-(1^-)$	D_s^+	$0(0^-)$
π^0	$1(0^+)$	$\rho_3(1690)$	$1^+(3^-)$	D_s^0	$0(0^2)$
η	$0^+(0^{++})$	$\rho(1700)$	$1^+(1^-)$	D_{s1}^+	$0(1^+)$
$\eta(500)$	$0^+(0^{++})$	$\rho_3(1700)$	$1^-(2^{++})$	$D_{s1}(2317)^0$	$0(0^+)$
$\rho(770)$	$1^+(1^-)$	$\eta(1710)$	$0^+(0^{++})$	$D_{s1}(2536)^+$	$0(1^+)$
$\omega(782)$	$0^-(1^-)$	$\eta(1760)$	$0^+(0^{++})$	$D_{s1}(2573)$	$0(0^2)$
$\eta(958)$	$0^+(0^{++})$	$\eta(1800)$	$1^-(0^+)$	$D_{s1}(2700)^+$	$0(1^-)$
$\eta(980)$	$0^+(0^{++})$	$f_0(1810)$	$0^+(2^{++})$	$D_{s1}(2860)^+$	$0(0^2)$
$\omega(980)$	$0^-(1^-)$	$X(1835)$	$?^?(2^-)$	$D_{s1}(3040)^+$	$0(0^2)$
$\phi(1020)$	$0^-(1^-)$	$X(1840)$	$?^?(2^?)$		
$h_1(1170)$	$0^-(1^+)$	$\eta_3(1850)$	$0^-(3^-)$		
$b_1(1235)$	$1^+(1^+)$	$\eta_3(1880)$	$0^+(2^+)$		
$\omega(1260)$	$1^+(1^+)$	$\rho_3(1870)$	$1^-(2^+)$		
$f_2(1270)$	$0^+(2^{++})$	$\rho(1900)$	$1^+(1^-)$		
$f_1(1285)$	$0^+(1^+)$	$f_0(1910)$	$0^+(2^{++})$		
$\eta(1295)$	$0^+(0^+)$	$f_0(1950)$	$0^+(2^{++})$		
$\pi(1300)$	$1^+(0^+)$	$\eta_3(1990)$	$1^+(3^-)$		
$\omega(1320)$	$1^-(2^+)$	$f_0(2010)$	$0^+(2^+)$		
$f_0(1370)$	$0^+(0^{++})$	$f_0(2020)$	$0^+(0^{++})$		
$h_1(1380)$	$?^?(1^+)$	$\omega_3(2040)$	$1^-(4^+)$		
$\Lambda(1405)$	$1^-(1^+)$	$f_0(2050)$	$0^+(4^+)$		
$\eta(1405)$	$0^+(0^+)$	$\eta_3(2100)$	$1^-(2^+)$		
$f_1(1420)$	$0^+(1^+)$	$f_0(2100)$	$0^+(0^{++})$		
$\omega(1420)$	$0^-(1^-)$	$f_2(2150)$	$0^+(2^+)$		
$f_2(1430)$	$0^+(2^+)$	$\rho(2150)$	$1^+(1^-)$		
$\omega(1450)$	$1^-(0^+)$	$\rho(2170)$	$0^-(1^-)$		
$\rho(1450)$	$1^+(1^-)$	$f_0(2200)$	$0^+(0^{++})$		
$\eta(1475)$	$0^+(0^+)$	$f_2(2220)$	$0^+(2^{++})$		
$f_0(1500)$	$0^+(0^{++})$	$\eta(2225)$	$0^+(0^+)$		
$f_1(1510)$	$0^+(1^+)$	$\eta_3(2250)$	$1^+(3^-)$		
$f_2^+(1525)$	$0^+(2^{++})$	$f_0(2300)$	$0^+(2^+)$		
$f_2^-(1565)$	$0^+(2^+)$	$f_0(2300)$	$0^+(4^+)$		
$\omega(1570)$	$1^+(1^+)$	$f_0(2330)$	$0^+(0^{++})$		
$h_1(1595)$	$0^-(1^+)$	$f_0(2340)$	$0^+(2^+)$		
$\pi_1(1600)$	$1^-(1^+)$	$\eta_3(2350)$	$1^+(5^-)$		
$\omega_1(1640)$	$1^-(1^+)$	$\omega_3(2450)$	$1^-(6^+)$		
$f_2(1640)$	$0^+(2^+)$	$\omega_3(2510)$	$0^+(6^+)$		
$\eta_2(1645)$	$0^+(2^+)$				
$\omega(1650)$	$0^-(1^-)$				
$\omega_3(1670)$	$0^-(3^-)$				
$\pi_2(1670)$	$1^-(2^+)$				



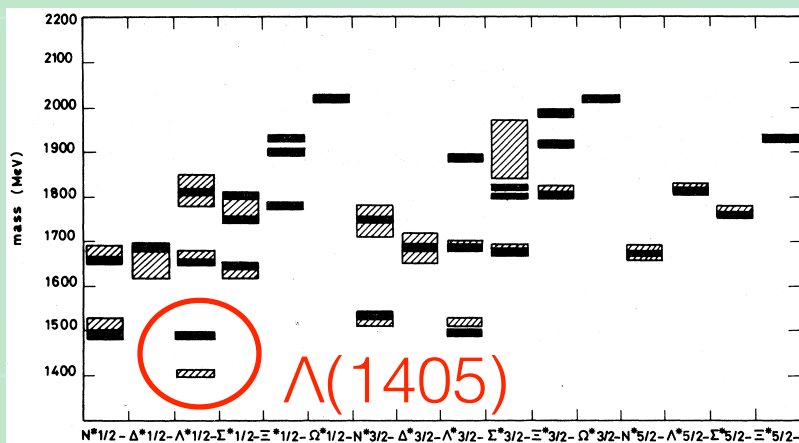
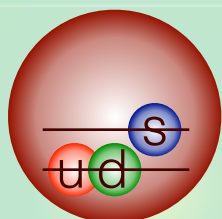
~ 210 mesons

- stable/unstable via strong interaction
- Excited states are mostly unstable. → resonances

$\Lambda(1405)$ and $\bar{K}N$ scattering

$\Lambda(1405)$ does not fit in standard picture \rightarrow exotic candidate

N. Isgur and G. Karl, Phys. Rev. D18, 4187 (1978)

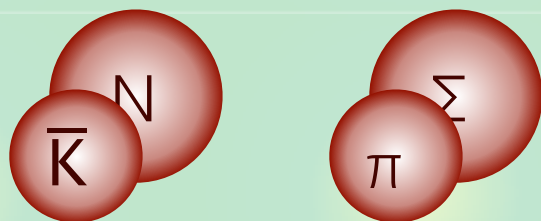


— : theory

▨ : experiment

Resonance in coupled-channel scattering

- coupling to MB states



energy \uparrow

— $\bar{K}N$ threshold

▨ $\Lambda(1405)$

— $\pi\Sigma$ threshold

Detailed analysis of $\bar{K}N$ - $\pi\Sigma$ scattering is necessary.

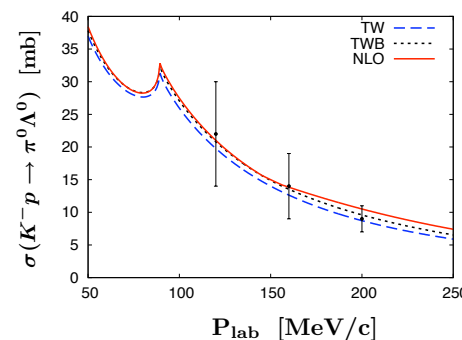
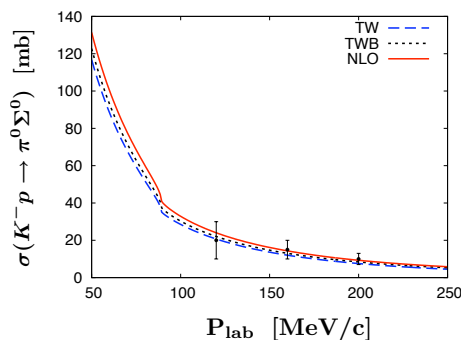
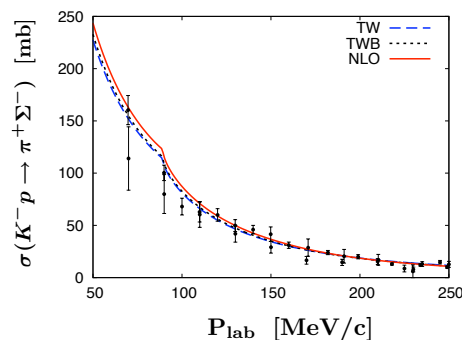
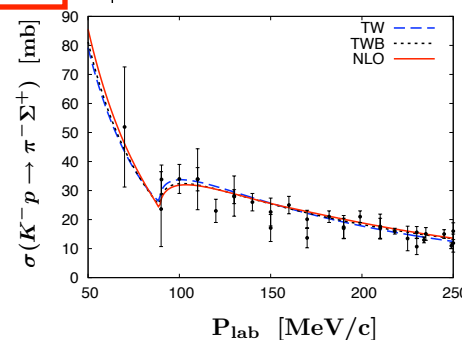
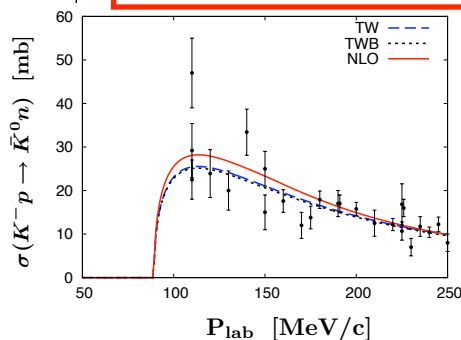
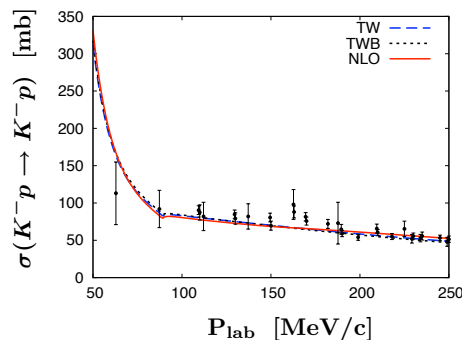
$\bar{K}N$ scattering by NLO chiral SU(3) dynamics

SIDDHARTA

branching ratios

	TW	TWB	NLO	Experiment
ΔE [eV]	373	377	306	$283 \pm 36 \pm 6$ [10]
Γ [eV]	495	514	591	$541 \pm 89 \pm 22$ [10]
γ	2.36	2.36	2.37	2.36 ± 0.04 [11]
R_n	0.20	0.19	0.19	0.189 ± 0.015 [11]
R_c	0.66	0.66	0.66	0.664 ± 0.011 [11]
$\chi^2/\text{d.o.f}$	1.12	1.15	0.96	

cross sections

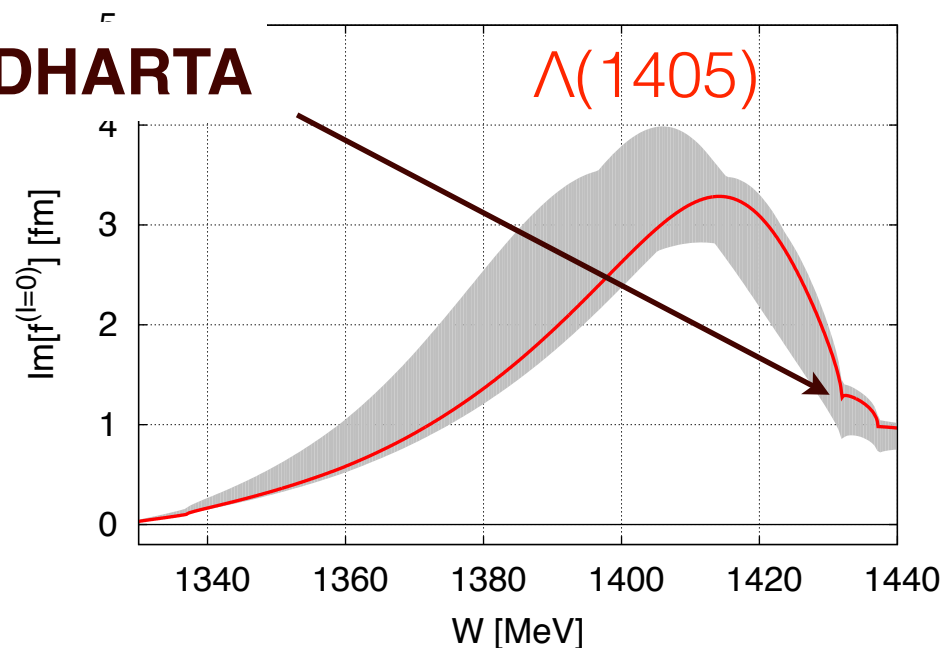
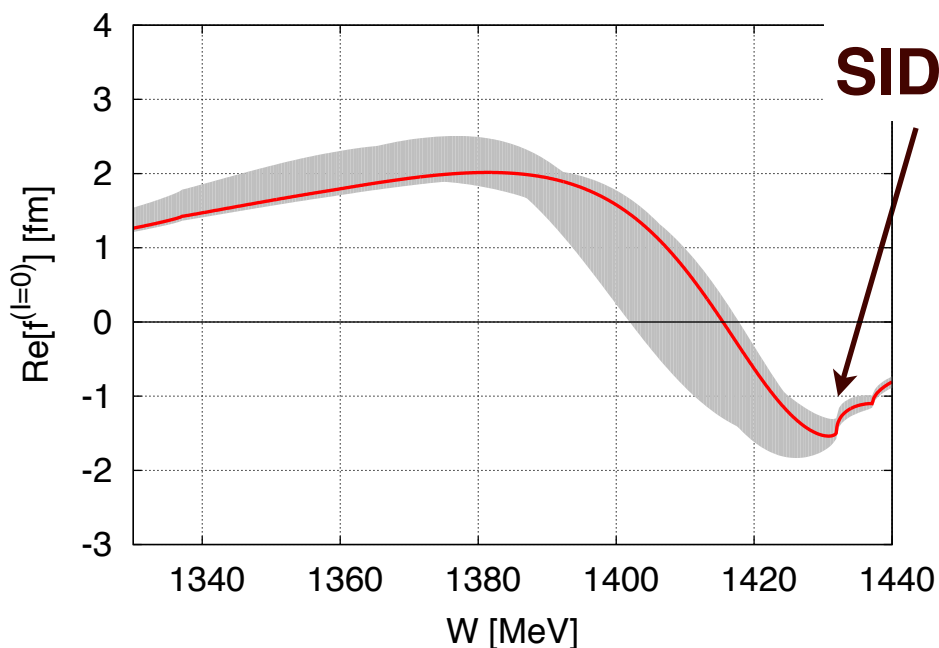


Y. Ikeda, T. Hyodo, W. Weise, PLB 706, 63 (2011); NPA 881 98 (2012)

Accurate description of all existing data ($\chi^2/\text{d.o.f.} \sim 1$)

Subthreshold extrapolation

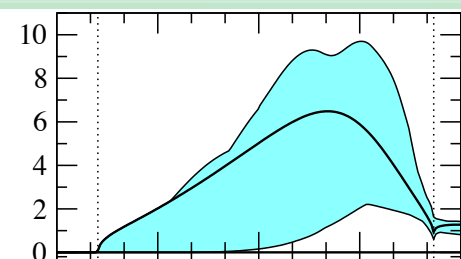
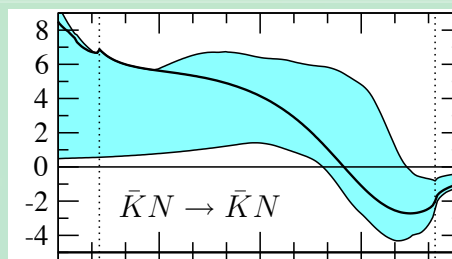
Uncertainty of $\bar{K}N \rightarrow \bar{K}N$ ($l=0$) amplitude below threshold



Y. Kamiya, K. Miyahara, S. Ohnishi, Y. Ikeda, T. Hyodo, E. Oset, W. Weise, NPA 954, 41 (2016)

- c.f. without SIDDHARTA

R. Nissler, Doctoral Thesis (2007)



SIDDHARTA is essential for **subthreshold** extrapolation.

Update in PDG

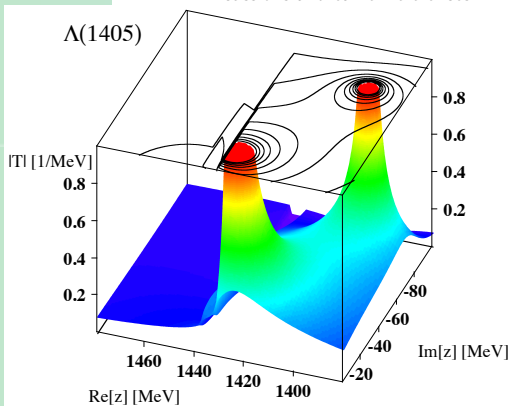
$\Lambda(1405)$ in Particle Data Group (PDG)

M. Tanabashi, et al., PRD 98, 030001 (2018), <http://pdg.lbl.gov/>

$\Lambda(1405) 1/2^-$

$I(J^P) = 0(\frac{1}{2}^-)$ Status **2014**

The nature of the $\Lambda(1405)$ has been a puzzle for decades: t... quark state or hybrid; two poles or one. We cannot here survey the rather extensive literature. See, for example, CIEPLY 10, KISSLINGER 11, SEKIHARA 11, and SHEVCHENKO 12A for discussions and earlier references.



of the chiral-unitary community 400-MeV region. ZYCHOR 08 inst the two-pole model, but this REVAI 09, which finds little basis o-pole models; and IKEDA 12,

1405 fits nicely into a $J^P =$ er members are the $\Lambda_c(2595)^+$, Fig. 1 of our note on "Charmed

MASS

TECN COMMENT

$\Lambda(1405) 1/2^-$

$I(J^P) = 0(\frac{1}{2}^-)$ Status **2018**

In the 1998 Note on the $\Lambda(1405)$ in PDG 98, R.H. Dalitz discussed the S-shaped cusp behavior of the intensity at the $N\bar{K}$ threshold observed in THOMAS 73 and HEMINGWAY 85. He commented that this behavior "is characteristic of S-wave coupling; the other below threshold hyperon, the $\Sigma(1385)$, has no such threshold distortion because its $N\bar{K}$ coupling is P-wave. For $\Lambda(1405)$ this asymmetry is the sole direct evidence that $J^P = 1/2^-$."

A recent measurement by the CLAS collaboration, MORIYA 14, definitively established the long-assumed $J^P = 1/2^-$ spin-parity assignment of the $\Lambda(1405)$. The experiment produced the $\Lambda(1405)$ spin-polarized in the photoproduction process $\gamma p \rightarrow K^+ \Lambda(1405)$ and measured the decay of the $\Lambda(1405)$ (polarized) $\rightarrow \Sigma^+$ (polarized) π^- . The observed isotropic decay of $\Lambda(1405)$ is consistent with spin $J = 1/2$. The polarization transfer to the Σ^+ (polarized) direction revealed negative parity, and thus established $J^P = 1/2^-$.

See the related review(s):
Pole Structure of the $\Lambda(1405)$ Region

$\Lambda(1405)$ REGION POLE POSITIONS

REAL PART

VALUE (MeV)	DOCUMENT ID	TECN
••• We do not use the following data for averages, fits, limits, etc. •••		
1429^{+8}_{-7}	1 MAI 15	DPWA
1325^{+15}_{-15}	2 MAI 15	DPWA
1434^{+2}_{-2}	3 MAI 15	DPWA
1330^{+4}_{-5}	4 MAI 15	DPWA
1421^{+3}_{-2}	5 GUO 13	DPWA
1388^{+9}	6 GUO 13	DPWA
1424^{+7}_{-23}	7 IKEDA 12	DPWA
1381^{+18}_{-6}	8 IKEDA 12	DPWA

105. Pole Structure of the $\Lambda(1405)$ Region

Written November 2015 by Ulf-G. Meißner (Bonn Univ. / FZ Jülich) and Tetsuo Hyodo (YITP, Kyoto Univ.).

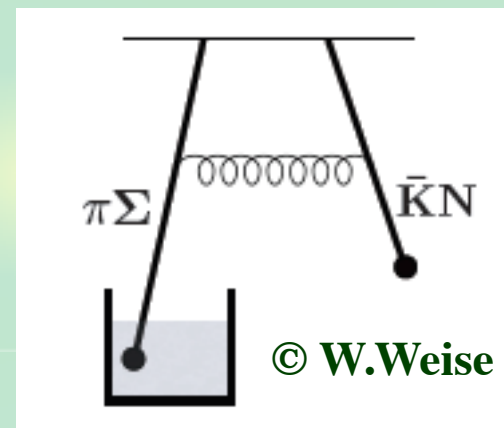
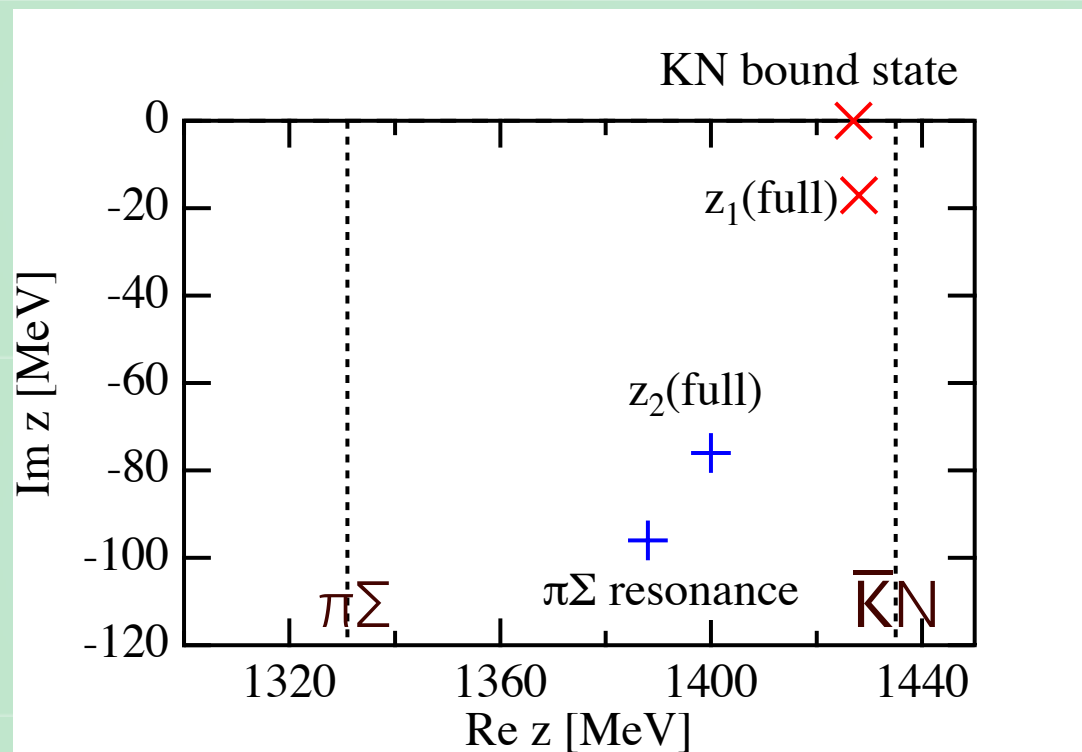
The $\Lambda(1405)$ resonance emerges in the meson-baryon scattering amplitude with the strangeness $S = -1$ and isospin $I = 0$. It is the archetype of what is called a dynamically generated resonance, as pioneered by Dalitz and Tuan [1]. The most powerful and

- Two-pole structure is confirmed.

Origin in physical basis

Attraction exists both in $\bar{K}N$ and $\pi\Sigma$ channels

T. Hyodo, W. Weise, Phys. Rev. C 77, 035204 (2008)



low-energy theorem

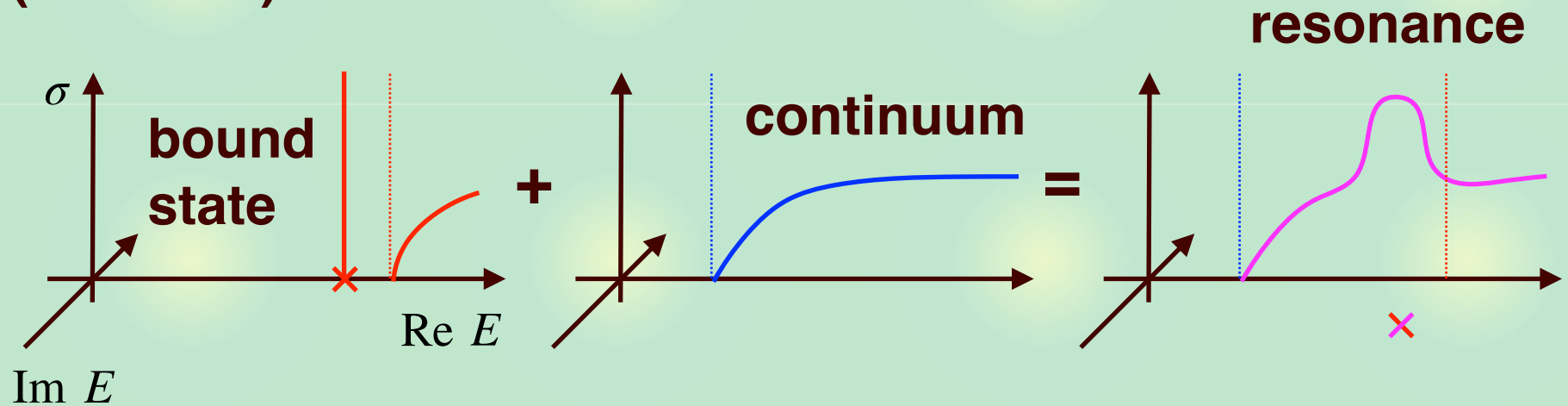


- strong attraction in $\bar{K}N$: bound state
- attraction in $\pi\Sigma$: resonance

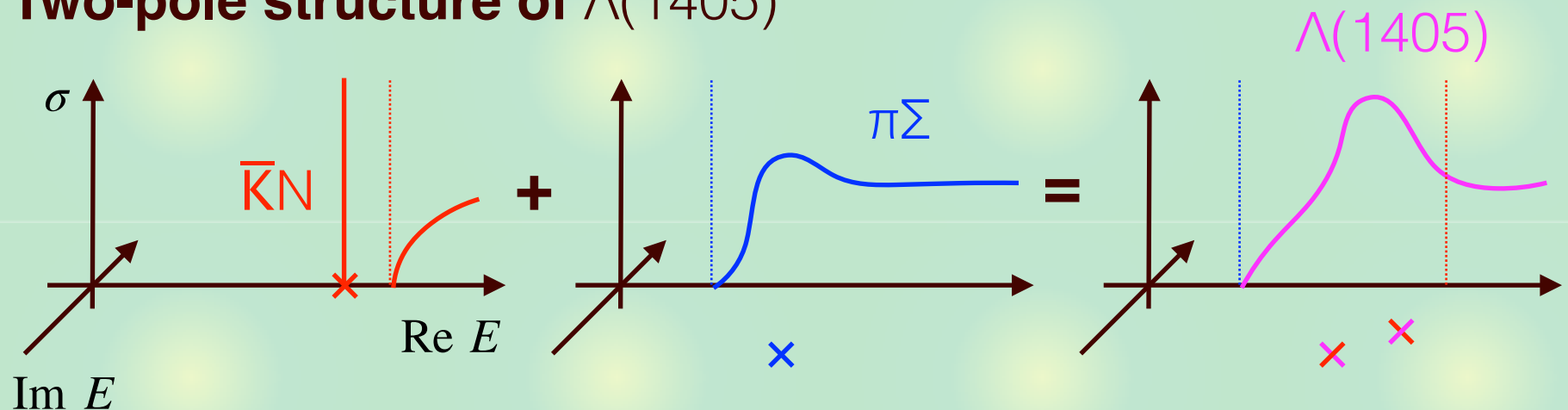
T. Hyodo, Intensive lecture at SNP school (2017)

Spectrum and pole

(standard) Feshbach resonance



Two-pole structure of $\Lambda(1405)$



→ Feshbach resonance in resonating continuum

Corresponding cold atom system?

${}^6\text{Li}$ atom : large background scattering length

I. Bloch, J. Dalibard, W. Zwerger, *Rev. Mod. Phys.* **80**, 885 (2008)

- theoretical study on large a_{bg}

B. Marcellis, *et al.*, *Phys. Rev. A* **70**, 012701 (2004)

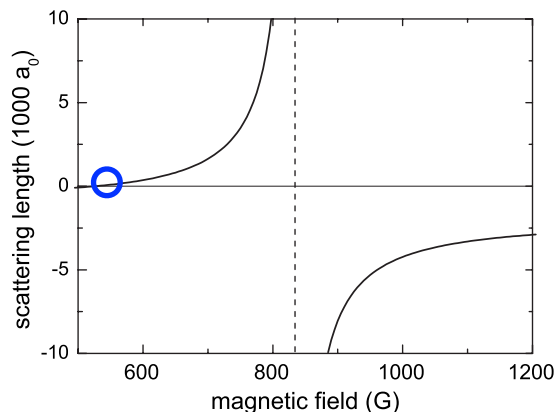
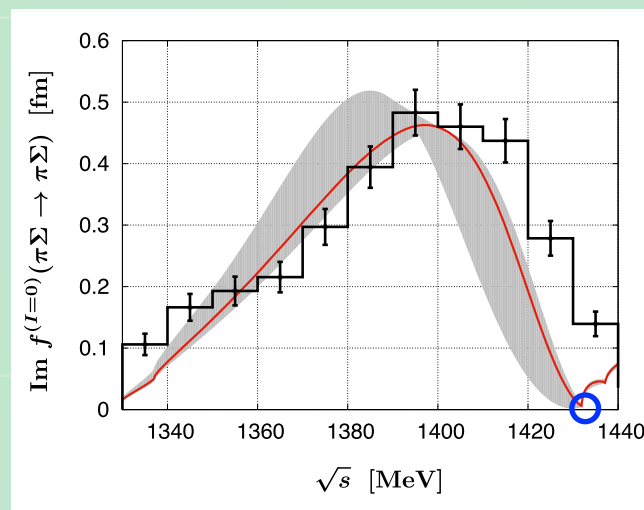


FIG. 2. Magnetic field dependence of the scattering length between the two lowest magnetic substates of ${}^6\text{Li}$ with a Feshbach resonance at $B_0=834$ G and a zero crossing at $B_0+\Delta B=534$ G. The background scattering length $a_{\text{bg}}=-1405a_B$ is exceptionally large in this case (a_B the Bohr radius).

- vanishing of scattering length near the unitary limit

1405 !



CDD zero near pole \rightarrow non-composite nature

Y. Kamiya, T. Hyodo, *Phys. Rev. D* **97**, 054019 (2018)

Summary



On clustering in hadrons

- exotic ($\bar{q}q$) excitation: QCD inherent
- hadrons are mostly unstable



Two-pole structure of $\Lambda(1405)$

- verified by recent analysis
- Feshbach resonance in resonating continuum

