

# Toward realistic prediction of the $\Lambda(1405)$ production in $K$ - $d$ reaction




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# Contents

 Introduction: recent developments

 Realistic  $\bar{K}N$ - $\pi\Sigma$  interaction with SIDDHARTA

[Y. Ikeda, T. Hyodo, W. Weise, PLB 706, 63 \(2011\); NPA 881 98 \(2012\)](#)

  $K$ - $d \rightarrow \pi\Sigma n$  reaction for J-PARC E31

[S. Ohnishi, Y. Ikeda, T. Hyodo, E. Hiyama, W. Weise, arXiv:1408.0118](#)



S. Ohnishi



Y. Ikeda



E. Hiyama



W. Weise

# $\bar{K}$ meson and $\bar{K}N$ interaction

## Two aspects of $K(\bar{K})$ meson

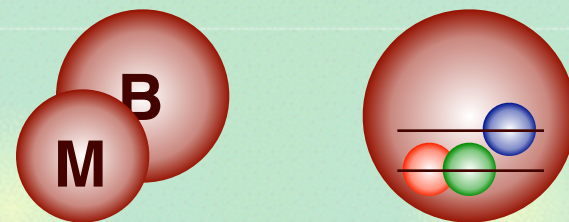
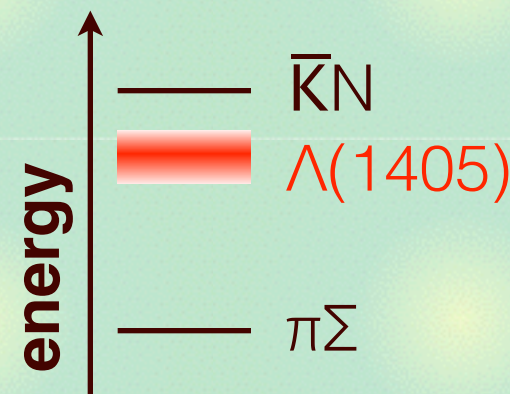
- **NG boson** of chiral  $SU(3)_R \otimes SU(3)_L \rightarrow SU(3)_V$
- **massive** by strange quark:  $m_K \sim 496$  MeV
- > **spontaneous/explicit** symmetry breaking

## $\bar{K}N$ interaction ...

- is coupled with  $\pi\Sigma$  channel
- has a resonance below threshold
- >  $\Lambda(1405)$

meson-baryon v.s.  $qqq$  state, ...

- is fundamental building block for  $\bar{K}$ -nuclei,  $\bar{K}$  in medium, ...



# $\bar{K}$ nuclei v.s. normal nuclei

## $\bar{K}N$ interaction

- strong attraction
- no repulsive core?

	$l=0$	$l=1$
NN	deuteron (2 MeV)	attractive
$\bar{K}N$	$\Lambda(1405)$ (15-30 MeV)	attractive

## Possible (quasi-)bound $\bar{K}$ in nuclei

- deep binding, high density?

Y. Nogami, Phys. Lett. 7, 288, (1963);

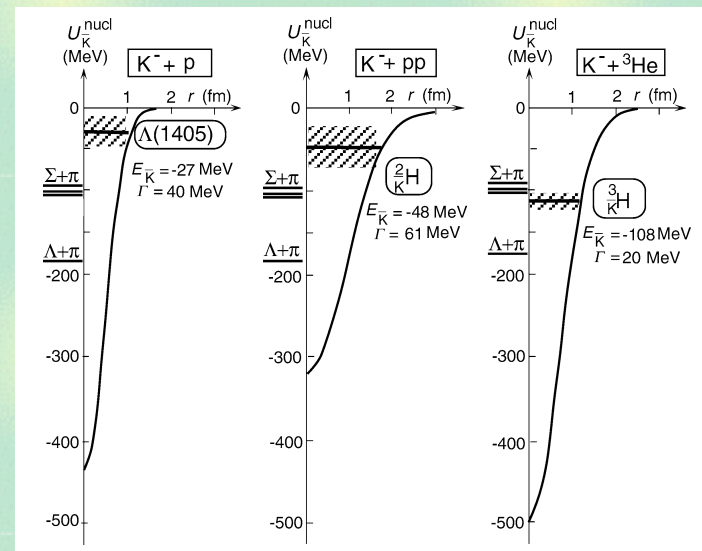
T. Yamazaki, Y. Akaishi, Phys. Lett. B535, 70 (2002);

A. Dote, *et al.*, Phys. Lett. B590, 51 (2004)

## Rigorous calculations (2007-)

- bound in few-nucleon systems
- binding energy depends on the employed  $\bar{K}N$  interaction

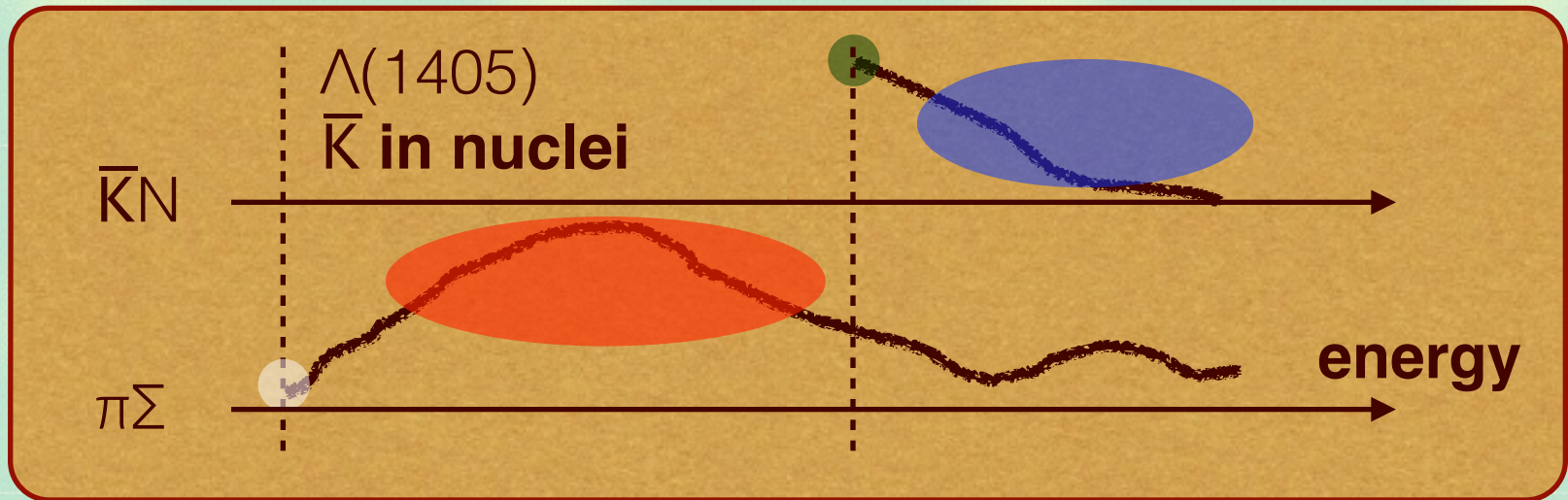
—> We need a **realistic  $\bar{K}N$  interaction.**



# Experimental constraints for the $\bar{K}N$ interaction

Above the  $\bar{K}N$  threshold:

- $K$ - $p$  total cross sections (old data)
- $\bar{K}N$  threshold branching ratios (old data)
- $K$ - $p$  scattering length (new data by SIDDHARTA) ←



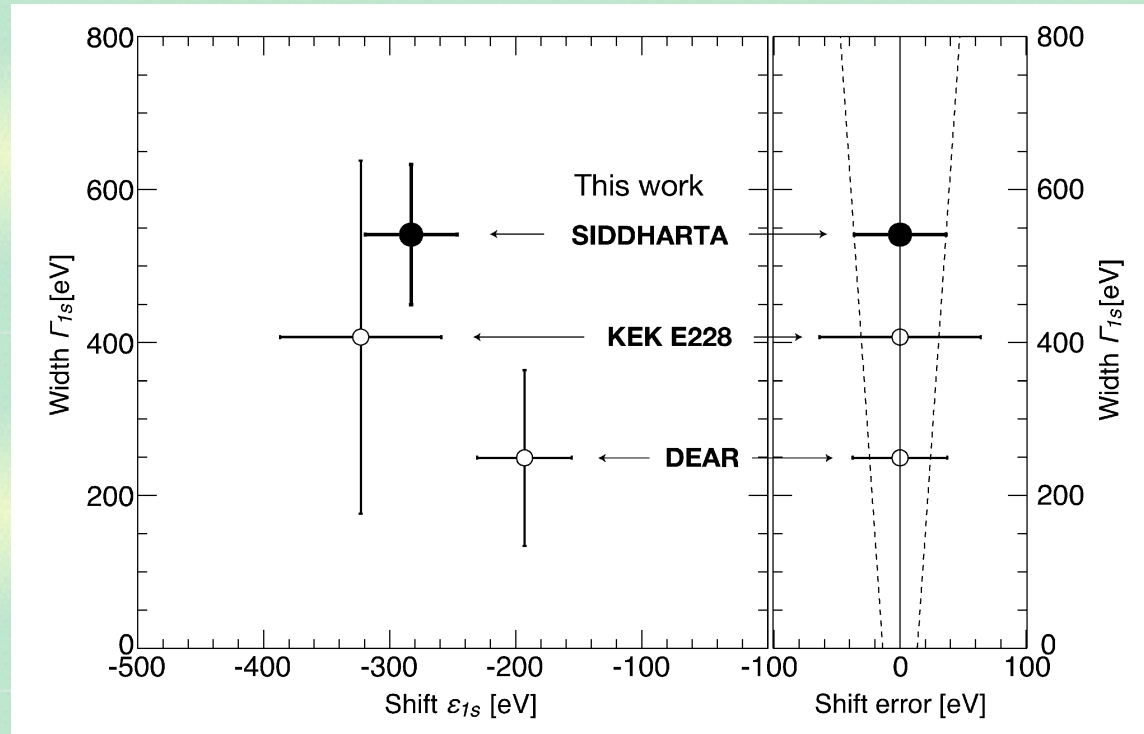
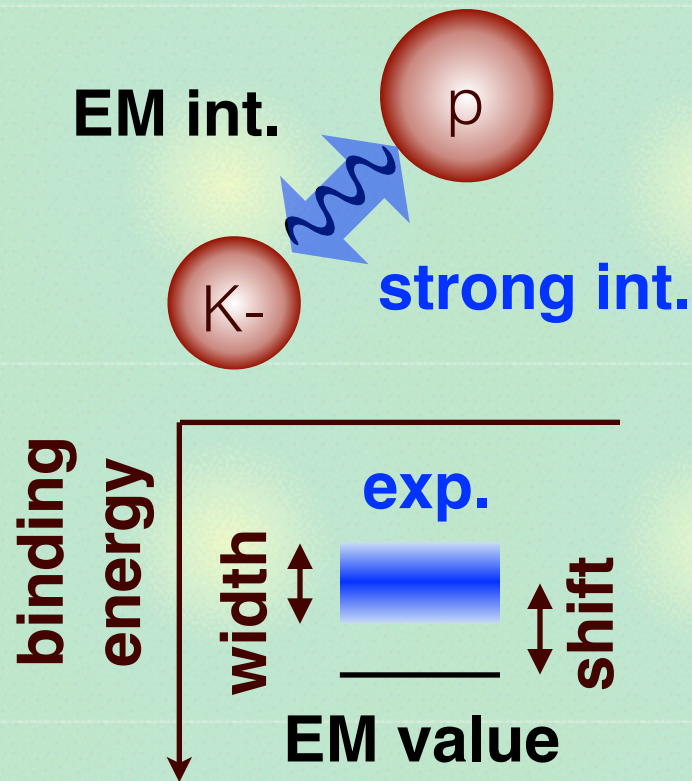
Below the  $\bar{K}N$  threshold:

- $\pi\Sigma$  mass spectra (new data by LEPS, CLAS, HADES,...) ←
- $\pi\Sigma$  scattering length (no data at present)

# SIDDHARTA measurement

## Precise measurement of the kaonic hydrogen X-rays

M. Bazzi, *et al.*, Phys. Lett. B704, 113 (2011); Nucl. Phys. A881, 88 (2012)



- shift and width of atomic state  $\longleftrightarrow$  K-p scattering length

U.-G. Meissner, U. Raha, A. Rusetsky, Eur. Phys. J. C35, 349 (2004)

**Direct constraint** on the  $\bar{K}N$  interaction at fixed energy

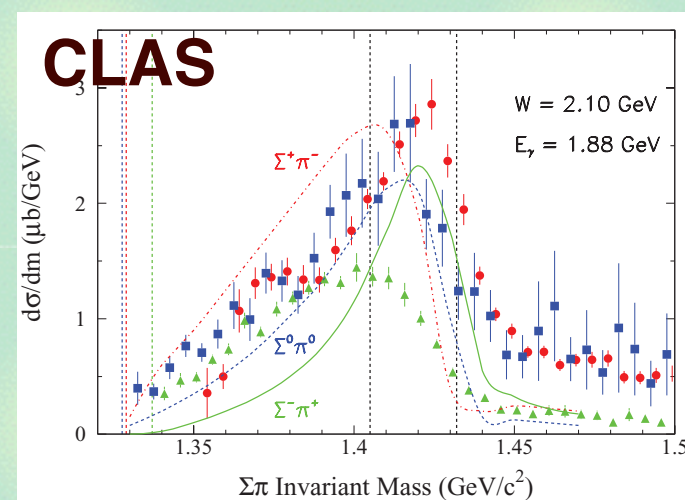
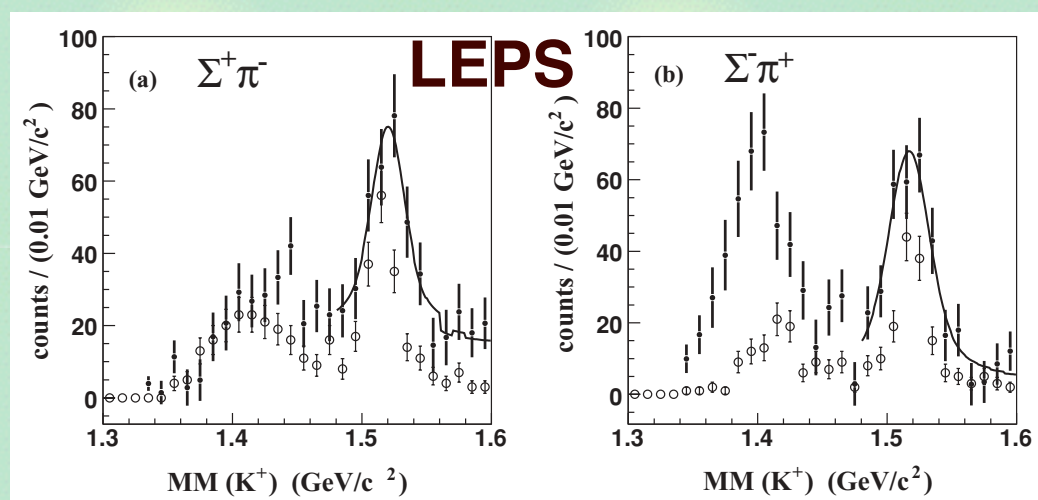
# New $\pi\Sigma$ spectra

Photoproduction experiments:  $\gamma p \rightarrow K^+(\pi\Sigma)^0$

- **LEPS** @  $1.5 < E_\gamma < 2.4$  GeV, **CLAS** @  $1.56 < E_\gamma < 3.83$  GeV

M. Niiyama, *et al.*, Phys. Rev. C78, 035202 (2008);

K. Moriya, *et al.*, Phys. Rev. C87, 035206 (2013)



Hadron-induced reactions:

- **HADES**:  $pp \rightarrow K^+p(\pi\Sigma)^0$

G. Agakishiev, *et al.*, Phys. Rev. C87, 025201 (2013)

- **J-PARC E31(planned)**:  $K-d \rightarrow n(\pi\Sigma)^0$

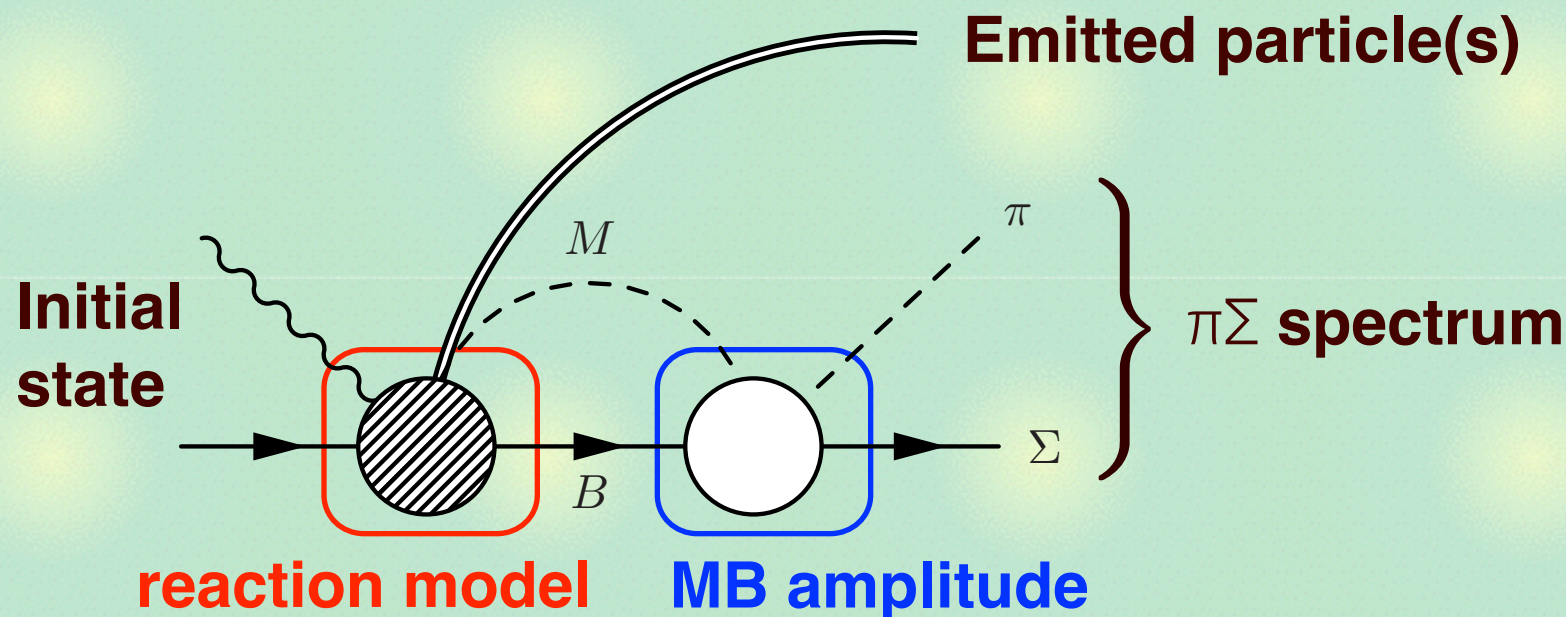
**New and precise spectra are being available.**

# $\pi\Sigma$ spectra and $\bar{K}N$ interaction

Can spectra constrain the **MB amplitude** ( $\bar{K}N$  interaction)?

- **Not directly.**




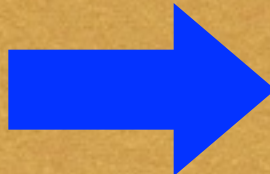
$\Lambda(1405)$  in production reaction:



- Spectra depend on the reaction (ratio of  $\bar{K}N/\pi\Sigma$  in the intermediate state, interference with  $l=1, \dots$ ).
- Event numbers do not constrain the absolute value.
- > Detailed **model analysis** for each reaction



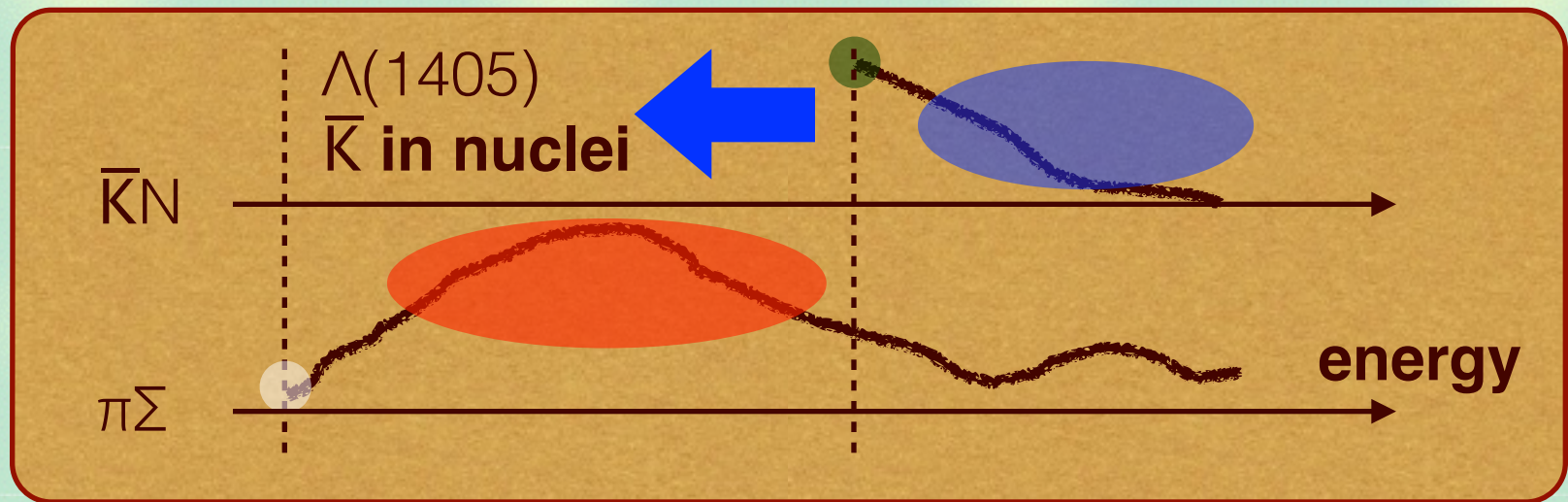
## Short summary of introduction

-   **$\bar{K}N$  interaction** is important both for hadron physics (structure of  $\Lambda(1405)$  resonance) and for nuclear physics ( $\bar{K}$  in nuclei)
  -  Precise **K-p scattering length** by SIDDHARTA  
—> quantitative **constraint** on  $\bar{K}N$  interaction
  -  New  **$\pi\Sigma$  spectra** from various reactions  
—> reliable **reaction model** required
-  **Construct realistic  $\bar{K}N$  scattering model and predict  $\pi\Sigma$  spectrum in K-d reaction.**

## Strategy for $\bar{K}N$ interaction

Above the  $\bar{K}N$  threshold:

- $K$ - $p$  total cross sections (old data)
- $\bar{K}N$  threshold branching ratios (old data)
- $K$ - $p$  scattering length (new data by SIDDHARTA)



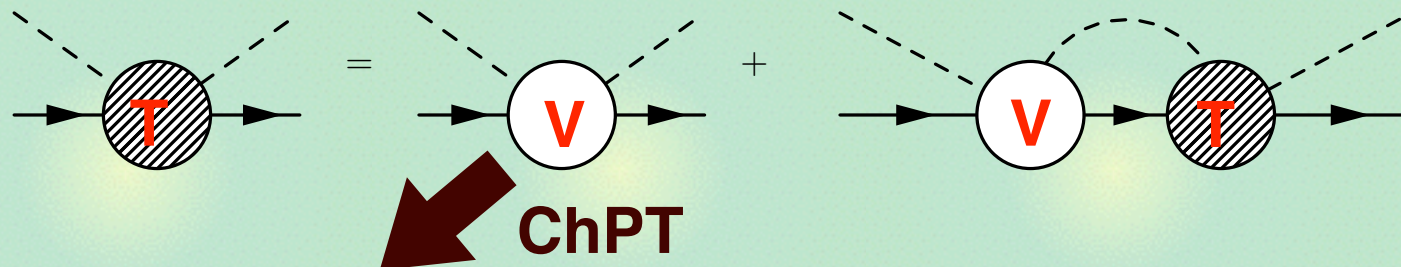
Below the  $\bar{K}N$  threshold:

- $\pi\Sigma$  mass spectra (new data by LEPS, CLAS, HADES,...)
- $\pi\Sigma$  scattering length (no data at present)

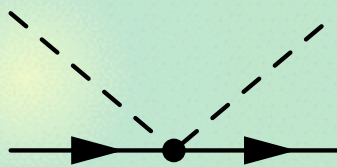
# Construction of the realistic amplitude

Chiral coupled-channel approach with systematic  $\chi^2$  fitting

Y. Ikeda, T. Hyodo, W. Weise, Phys. Lett. B706, 63 (2011); Nucl. Phys. A881 98 (2012);



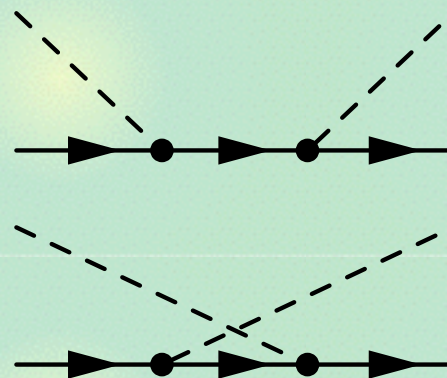
1) TW term



$\mathcal{O}(p)$

**TW model**

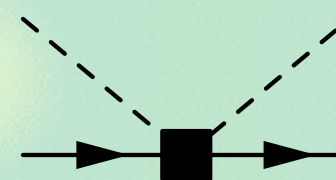
2) Born terms



$\mathcal{O}(p)$

**TWB model**

3) NLO terms



**LECs**

$\mathcal{O}(p^2)$

**NLO model**

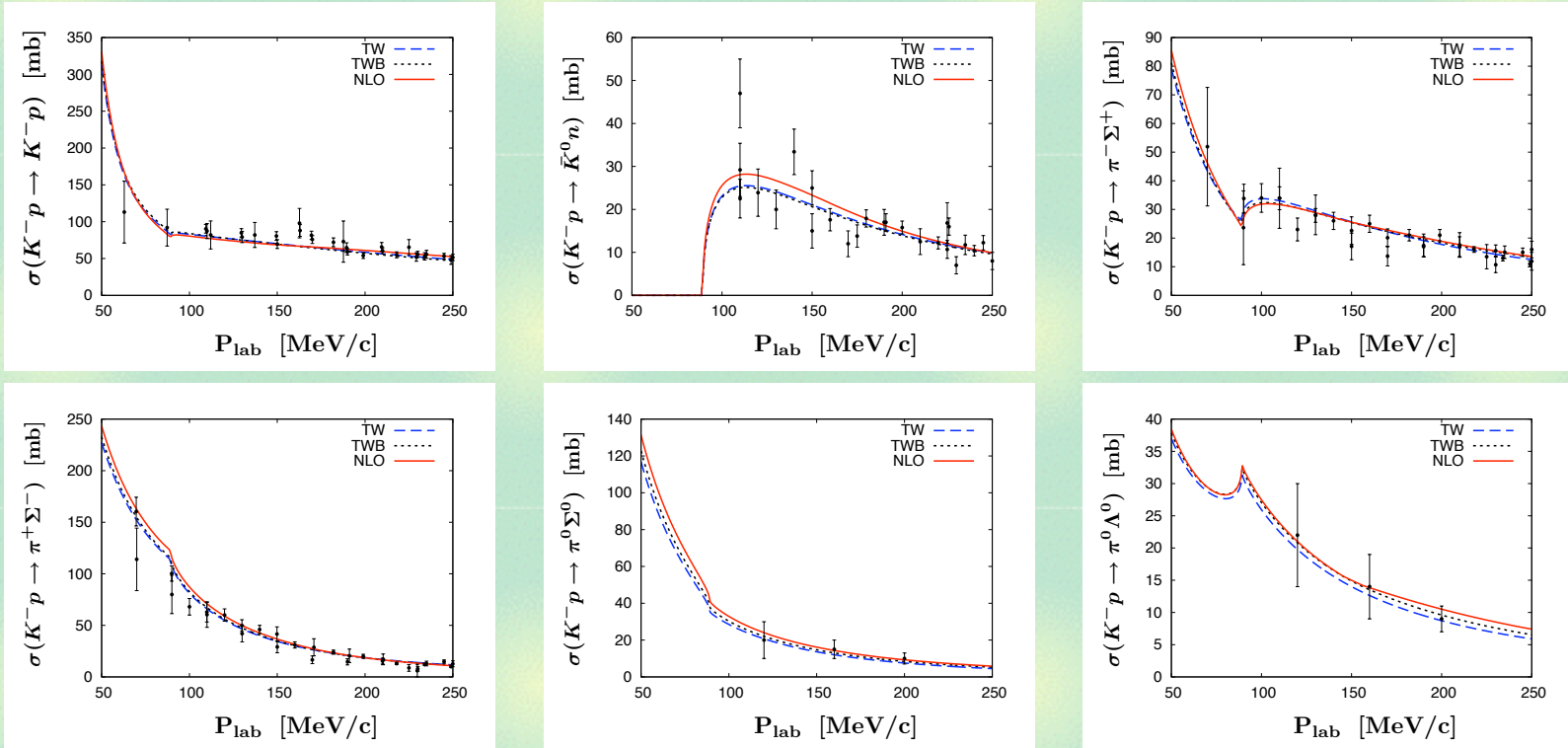
# Best-fit results

**SIDDHARTA**

**Branching ratios**

	TW	TWB	NLO	Experiment
$\Delta E$ [eV]	373	377	306	$283 \pm 36 \pm 6$ [10]
$\Gamma$ [eV]	495	514	591	$541 \pm 89 \pm 22$ [10]
$\gamma$	2.36	2.36	2.37	$2.36 \pm 0.04$ [11]
$R_n$	0.20	0.19	0.19	$0.189 \pm 0.015$ [11]
$R_c$	0.66	0.66	0.66	$0.664 \pm 0.011$ [11]
$\chi^2/\text{d.o.f}$	1.12	1.15	0.96	

**cross sections**

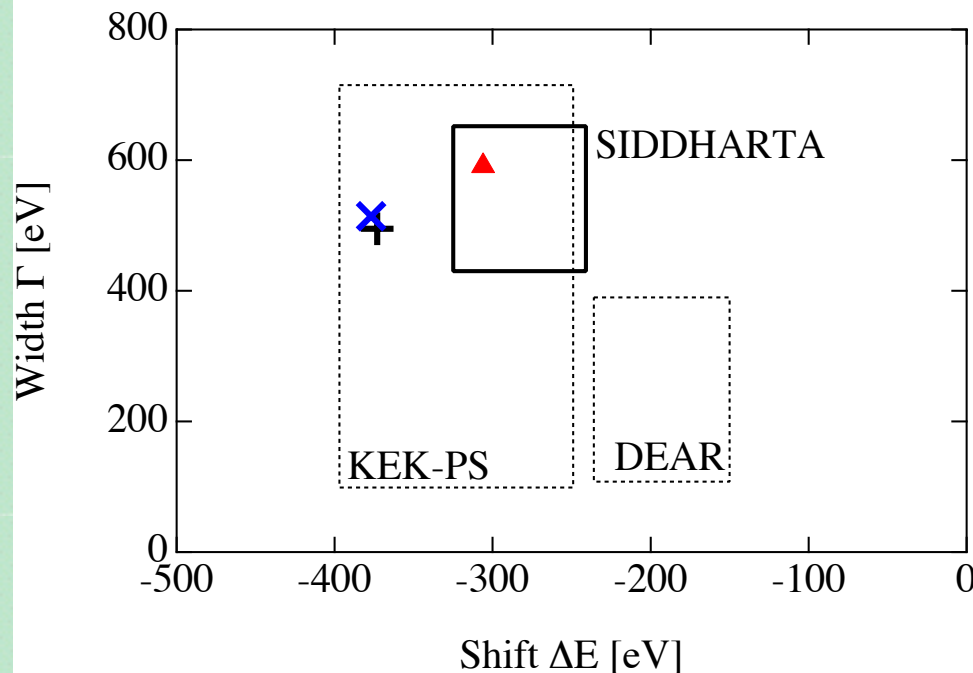


**SIDDHARTA is consistent with cross sections**

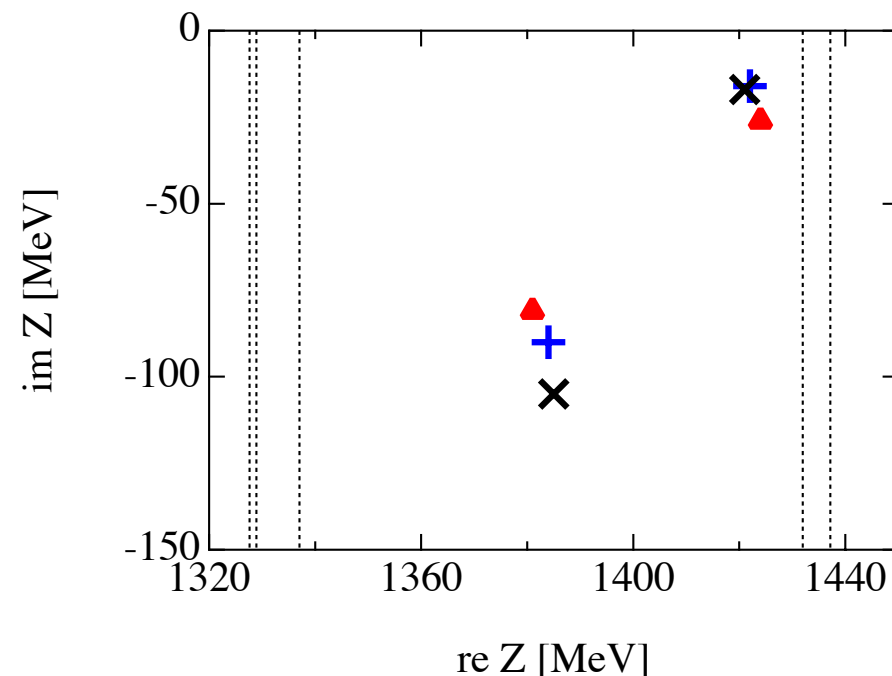
# Shift, width, and pole positions

	TW	TWB	NLO
$\chi$	1.12	1.15	0.957

## Shift and width



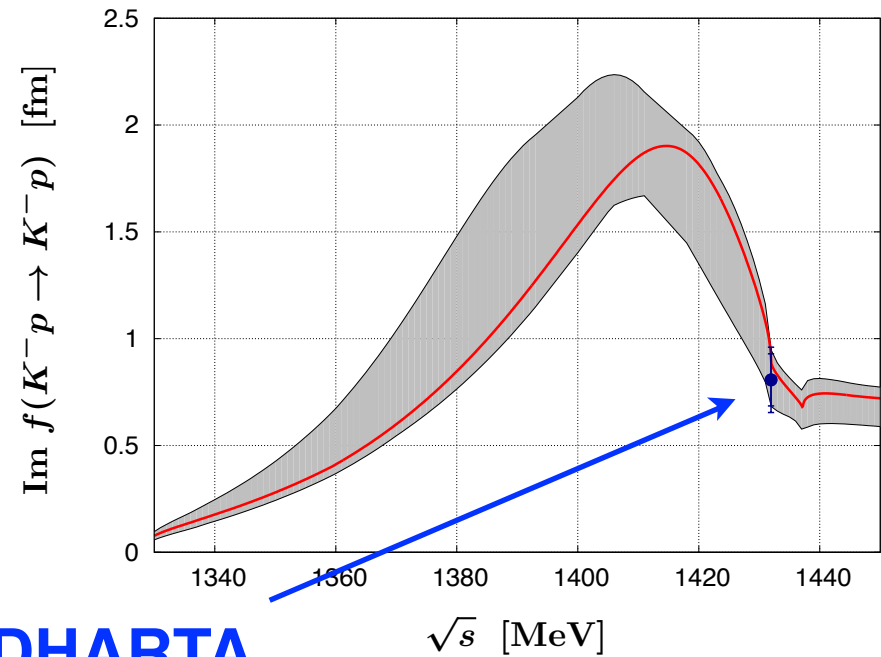
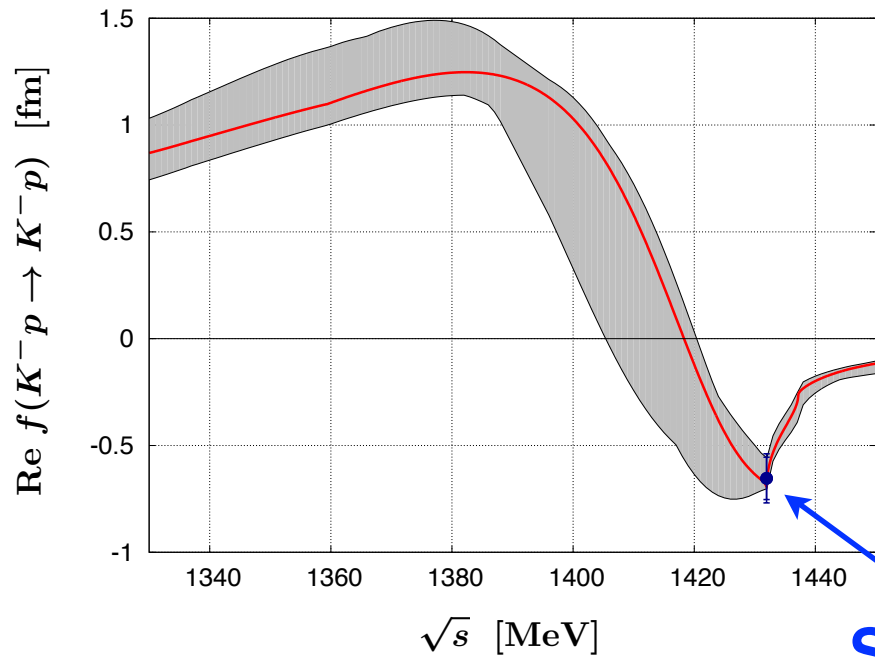
## Pole positions



**TW** and **TWB** are reasonable, while best-fit requires **NLO**. Pole positions are now converging.

# Subthreshold extrapolation

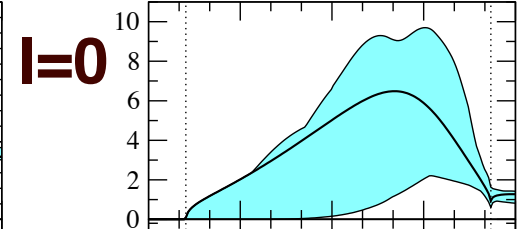
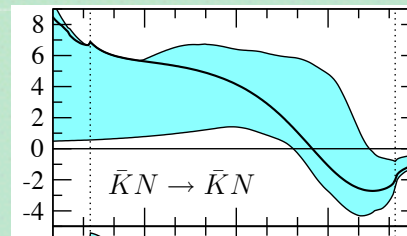
## Behavior of $K^-p$ amplitude below threshold



**SIDDHARTA**

- c.f. without SIDDHARTA

R. Nissler, Doctoral Thesis (2007)



Subthreshold extrapolation is now well controlled.

# Remaining ambiguity

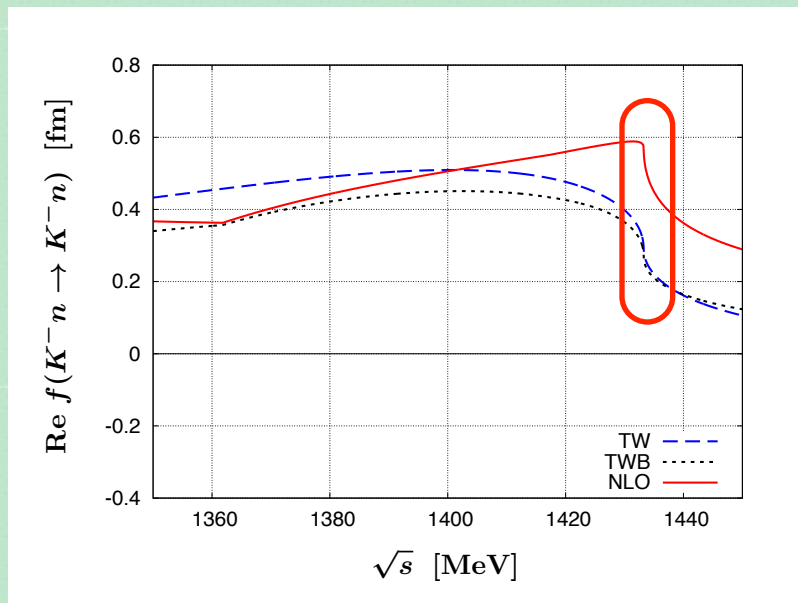
For  $\bar{K}$ -nucleon interaction, we need both  $K$ - $p$  and  $K$ - $n$ .

$$a(K^-p) = \frac{1}{2}a(I=0) + \frac{1}{2}a(I=1) + \dots, \quad a(K^-n) = a(I=1) + \dots$$

$$a(K^-n) = 0.29 + i0.76 \text{ fm (TW) ,}$$

$$a(K^-n) = 0.27 + i0.74 \text{ fm (TWB) ,}$$

$$a(K^-n) = 0.57 + i0.73 \text{ fm (NLO) .}$$



Some deviation: constraint on  $K$ - $n$  ( $\leftarrow$  kaonic deuterium?)

## Summary 1

We study the  $\bar{K}N-\pi\Sigma$  interaction based on chiral coupled-channel approach.

- With accurate kaonic hydrogen data, we can construct realistic  $\bar{K}N-\pi\Sigma$  interaction. **Ambiguity** in the subthreshold extrapolation ( $\Lambda(1405)$  energy region) **is significantly reduced.**
- Pole position** of  $\Lambda(1405)$  is converging.
- Future refinement:  **$l=1$  channel**  
← kaonic deuterium measurement.

Y. Ikeda, T. Hyodo, W. Weise, PLB 706, 63 (2011); NPA 881 98 (2012)

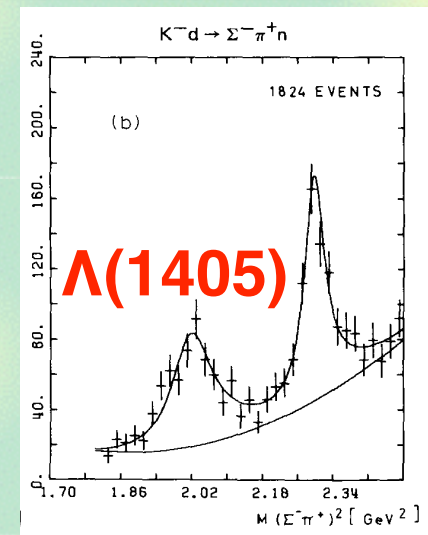


# Kaon induced reaction : experiments

## Bubble chamber experiment

O. Braun, *et al.*, Nucl. Phys. B129, 1 (1977)

- $\rho_K$  @ 686-844 MeV
- $\pi^+\Sigma^-$  spectrum



## J-PARC E31 (forthcoming)

[http://j-parc.jp/researcher/Hadron/en/pac\\_0907/pdf/Noumi.pdf](http://j-parc.jp/researcher/Hadron/en/pac_0907/pdf/Noumi.pdf)

- $\rho_K$  @ 1 GeV
- Missing mass spectroscopy
- Separation of  $\pi^+\Sigma^-$  /  $\pi^-\Sigma^+$  /  $\pi^0\Sigma^0$  spectra

## Note for the K-d reaction

$$K^-d \sim [\bar{K}[NN]_{I=0}]_{I=1/2} \sim 1[[\bar{K}N]_{I=0}N]_{I=1/2} + 3[[\bar{K}N]_{I=1}N]_{I=1/2}$$

- large  $|=1$  MB fraction

# Kaon induced reaction : theory

## Two-step approaches with chiral/phenomenological int.

D. Jido, E. Oset, T. Sekihara, *Eur. Phys. J. A*42, 257 (2009);

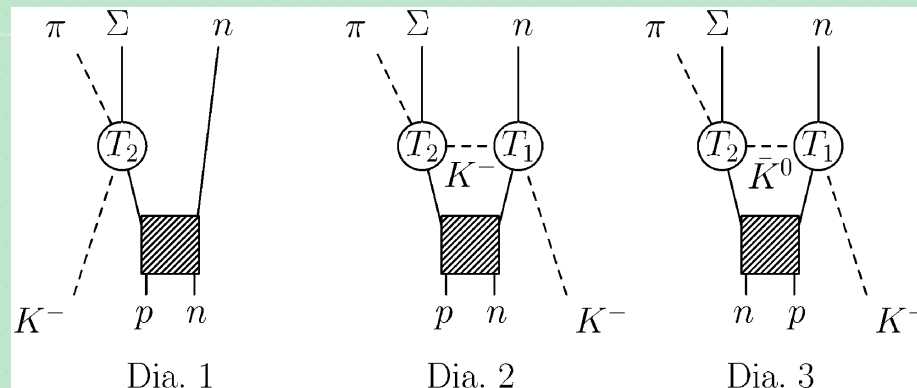
J. Esmaili, Y. Akaishi, T. Yamazaki, *Phys. Rev. C*83, 055207 (2011);

D. Jido, E. Oset, T. Sekihara, *Eur. Phys. J. A*47, 42 (2011);

K. Miyagawa, J. Haidenbauer, *Phys. Rev. C*85, 065201 (2012);

J. Yamagata-Sekihara, T. Sekihara, D. Jido, *PTEP* 043D02 (2013)

- **Perturbative: full three-body dynamics is not included.**



## Faddeev(AGS) approach

J. Revai, *Few-Body Syst.* 54, 1865 (2013)

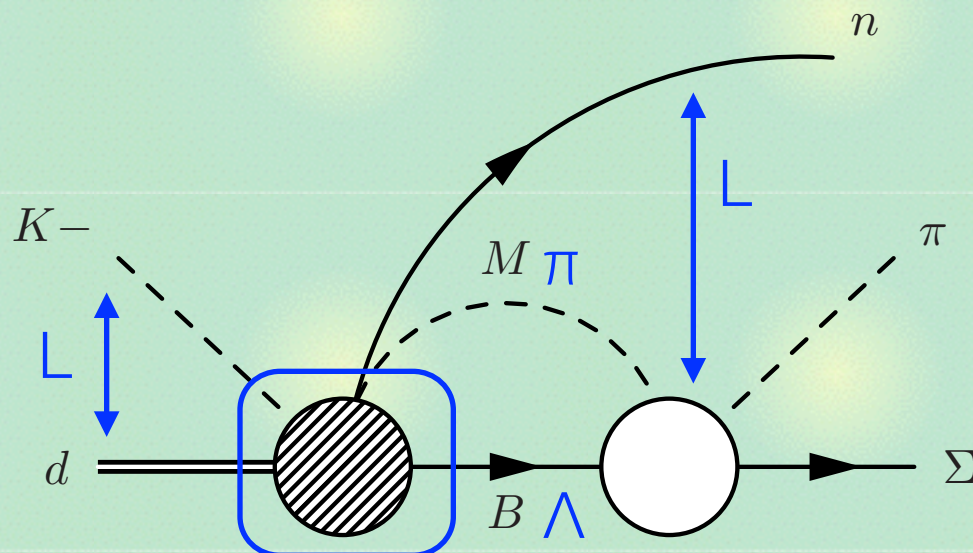
-  $\pi\Lambda N$  channel is **not included**.

- **s-wave** interactions **only** (valid at low energy)

## Strategy for J-PARC E31

Our framework of K-d  $\rightarrow$   $\pi\Sigma n$  for J-PARC E31

- **Faddeev(AGS)** amplitude: full three-body dynamics
- Inclusion of the  $\pi\Lambda$  channel: proper  $l=1$  contribution
- Inclusion of **relative L**: 1 GeV incident momentum



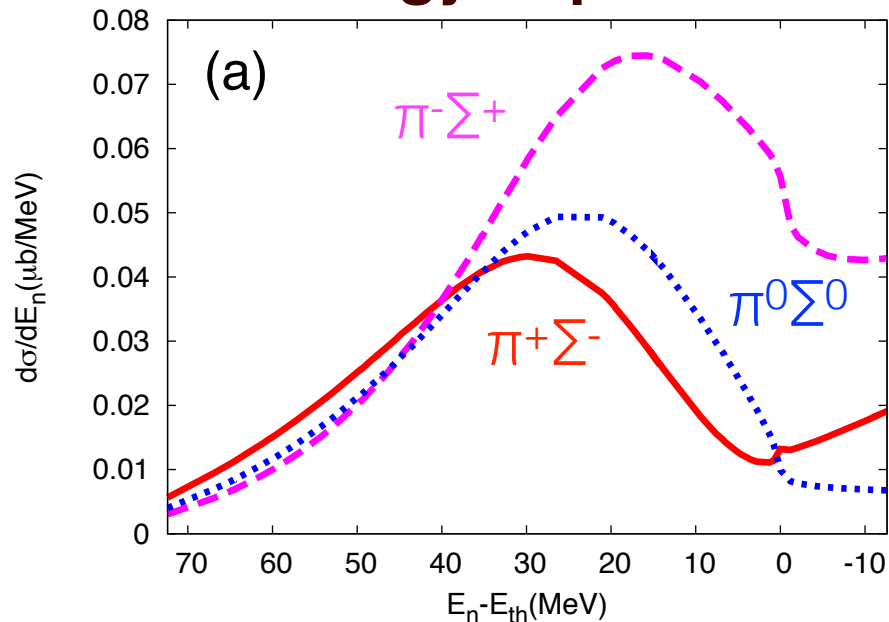
**Faddeev(AGS)**

- MB interaction: energy-dep. and energy-indep. interactions (fitted to cross sections, to be constrained by SIDDAHRTA)

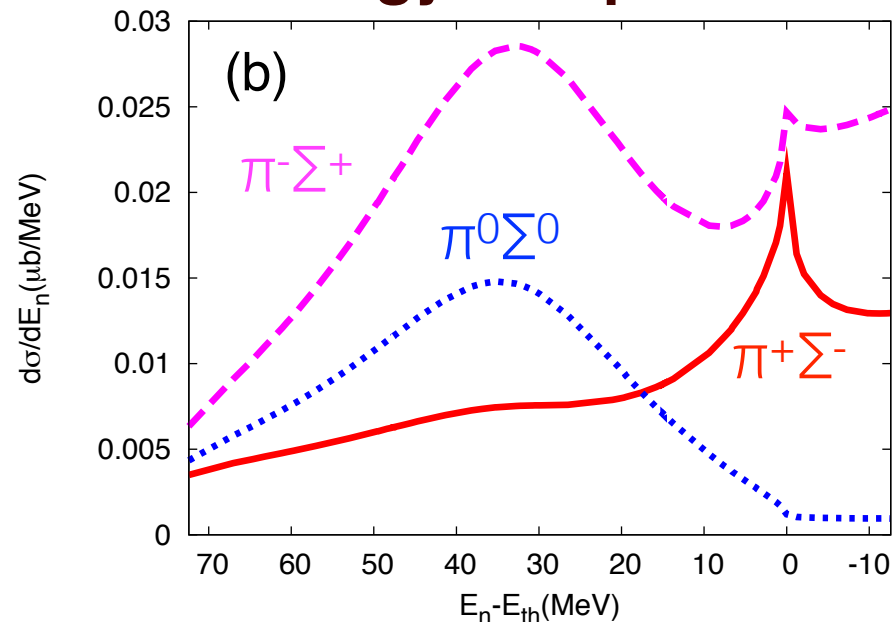
# $\pi\Sigma$ spectra with various charge combinations

$\pi\Sigma$  spectra @  $P_{K^-} = 1$  GeV

energy-dep.



energy-indep.



Deviation of  $\pi^- \Sigma^+$  and  $\pi^+ \Sigma^-$  spectra

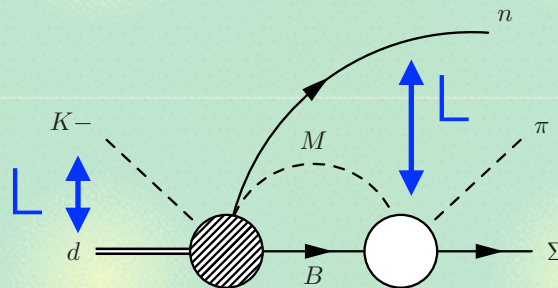
- large **interference** effect with  $l=1$  components

Difference of energy-dep. / energy-indep. (shape, magnitude)

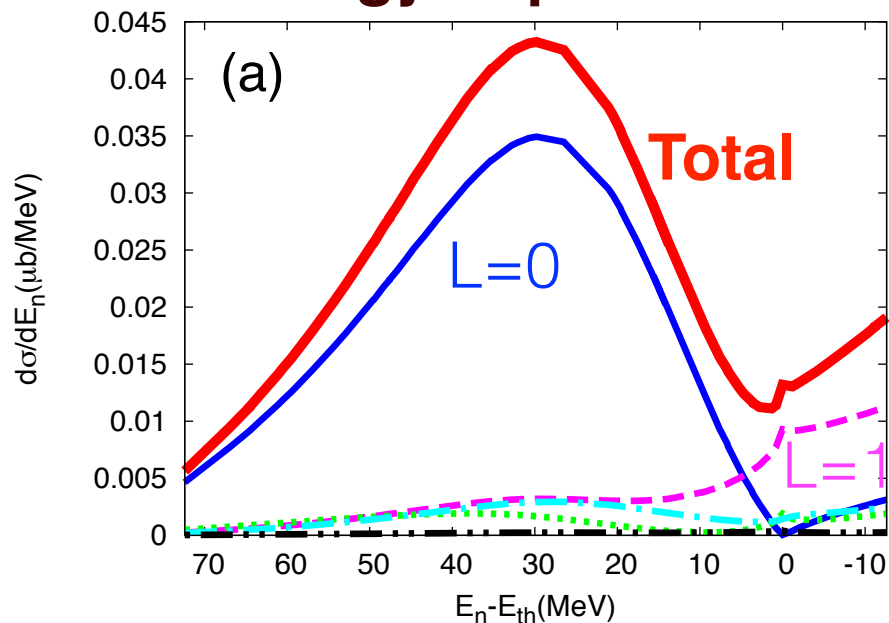
- distinction of **subthreshold  $\bar{K}N$  amplitude**

# Partial wave contributions

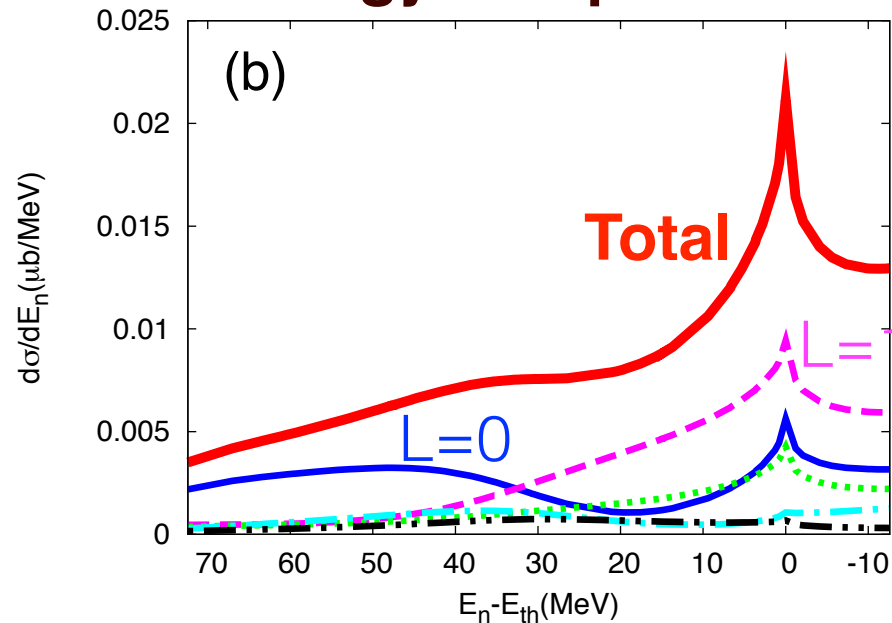
Effect of the higher partial wave components @  $P_{K^-} = 1$  GeV



energy-dep.  $\pi^+\Sigma^-$







energy-indep.  $\pi^+\Sigma^-$



$L \neq 0$  partial waves are important around threshold.

## Summary 2

**We study the K-d  $\rightarrow$   $\pi\Sigma n$  reaction for J-PARC E31**

-  We employ the **Faddeev(AGS)** amplitude with  **$\pi\Lambda N$  channel** and **relative  $L$**  effects included.
-  Deviation of different charged  $\pi\Sigma$  states indicates the large **interference with  $l=1$** .
-  Lineshape and the magnitude of  $\pi\Sigma$  spectra are sensitive to **subthreshold  $\bar{K}N$  interaction**.
-  **Higher  $L$**  components affect around threshold.

S. Ohnishi, Y. Ikeda, T. Hyodo, E. Hiyama, W. Weise, arXiv:1408.0118