

$\bar{K}N$ interaction and Λ^*N interaction in chiral SU(3) dynamics







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Contents

-  Introduction to chiral SU(3) dynamics
-  $\bar{K}N$ interaction in chiral SU(3) dynamics
 - structure of the $\Lambda^* = \Lambda(1405)$
 - toward the “realistic $\bar{K}N$ - $\pi\Sigma$ interaction”
-  Λ^*N interaction in chiral SU(3) dynamics
 - Λ^*N potential in meson-exchange picture
 - structure of the Λ^*N bound state
-  Summary

Chiral symmetry breaking in hadron physics

Chiral symmetry: QCD with massless quarks

Consequence of chiral symmetry breaking in hadron physics

- **appearance of the Nambu-Goldstone (NG) boson**

$$m_\pi \sim 140 \text{ MeV}$$

- **dynamical generation of hadron masses**

$$M_p \sim 1 \text{ GeV} \sim 3M_q, \quad M_q \sim 300 \text{ MeV} \quad v.s. \quad 3 - 7 \text{ MeV}$$

- **constraints on the interaction of NG boson and a hadron**
low energy theorems \leftarrow current algebra
systematic low energy ($m, p/4\pi f_\pi$) expansion: ChPT

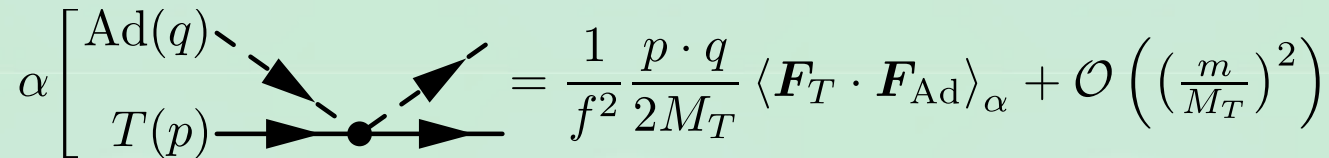
Chiral symmetry and its breaking

$$SU(3)_R \otimes SU(3)_L \rightarrow SU(3)_V$$

Underlying QCD \Leftrightarrow observed hadron phenomena

s-wave low energy interaction

Low energy NG boson (Ad)- target hadron (T) scattering

$$\alpha \left[\begin{array}{c} \text{Ad}(q) \\ T(p) \end{array} \right] = \frac{1}{f^2} \frac{p \cdot q}{2M_T} \langle \mathbf{F}_T \cdot \mathbf{F}_{\text{Ad}} \rangle_\alpha + \mathcal{O} \left(\left(\frac{m}{M_T} \right)^2 \right)$$


Projection onto s-wave: Weinberg-Tomozawa term

Y. Tomozawa, *Nuovo Cim.* **46A**, 707 (1966); S. Weinberg, *Phys. Rev. Lett.* **17**, 616 (1966)

$$V_{ij} = -\frac{C_{ij}}{4f^2} (\omega_i + \omega_j) \quad \text{energy dependence (derivative coupling)}$$

decay constant of π ($g_V=1$)

$$C_{ij} = \sum_{\alpha} C_{\alpha, T} \left(\begin{array}{cc} 8 & T \\ I_{M_i}, Y_{M_i} & I_{T_i}, Y_{T_i} \end{array} \parallel \begin{array}{c} \alpha \\ I, Y \end{array} \right) \left(\begin{array}{cc} 8 & T \\ I_{M_j}, Y_{M_j} & I_{T_j}, Y_{T_j} \end{array} \parallel \begin{array}{c} \alpha \\ I, Y \end{array} \right)$$

$$C_{\alpha, T} = \langle 2\mathbf{F}_T \cdot \mathbf{F}_{\text{Ad}} \rangle = C_2(T) - C_2(\alpha) + 3$$

Group theoretical structure and flavor **SU(3) symmetry** determines **the sign and the strength** of the interaction

Low energy theorem: leading order term in ChPT

Scattering amplitude and unitarity

Unitarity of S-matrix: Optical theorem

$$\text{Im} [T^{-1}(s)] = \frac{\rho(s)}{2} \quad \text{phase space of two-body state}$$

General amplitude by dispersion relation

$$T^{-1}(\sqrt{s}) = \sum_i \frac{R_i}{\sqrt{s} - W_i} + \tilde{a}(s_0) + \frac{s - s_0}{2\pi} \int_{s_+}^{\infty} ds' \frac{\rho(s')}{(s' - s)(s' - s_0)}$$

R_i, W_i, a : to be determined by chiral interaction

Identify dispersion integral = loop function G , the rest = V^{-1}

$$T(\sqrt{s}) = \frac{1}{V^{-1}(\sqrt{s}) - G(\sqrt{s}; a)}$$

Scattering amplitude

V? chiral expansion of T , (conceptual) matching with **ChPT**

$$T^{(1)} = V^{(1)}, \quad T^{(2)} = V^{(2)}, \quad T^{(3)} = V^{(3)} - V^{(1)}GV^{(1)}, \quad \dots$$

Amplitude T: consistent with chiral symmetry + unitarity

Chiral unitary approach

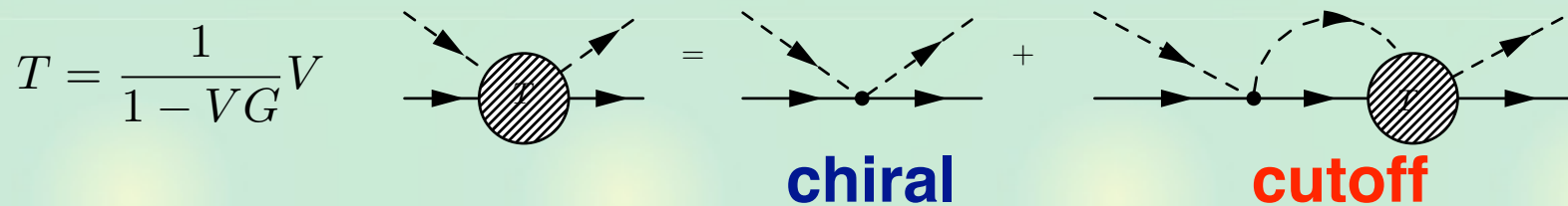
Description of $S = -1$, $\bar{K}N$ s-wave scattering: $\Lambda(1405)$ in $l=0$

- Interaction \leftarrow chiral symmetry

Y. Tomozawa, *Nuovo Cim.* 46A, 707 (1966); S. Weinberg, *Phys. Rev. Lett.* 17, 616 (1966)

- Amplitude \leftarrow unitarity in **coupled channels**

R.H. Dalitz, T.C. Wong, G. Rajasekaran, *Phys. Rev.* 153, 1617 (1967)



N. Kaiser, P. B. Siegel, W. Weise, *Nucl. Phys.* A594, 325 (1995),

E. Oset, A. Ramos, *Nucl. Phys.* A635, 99 (1998),

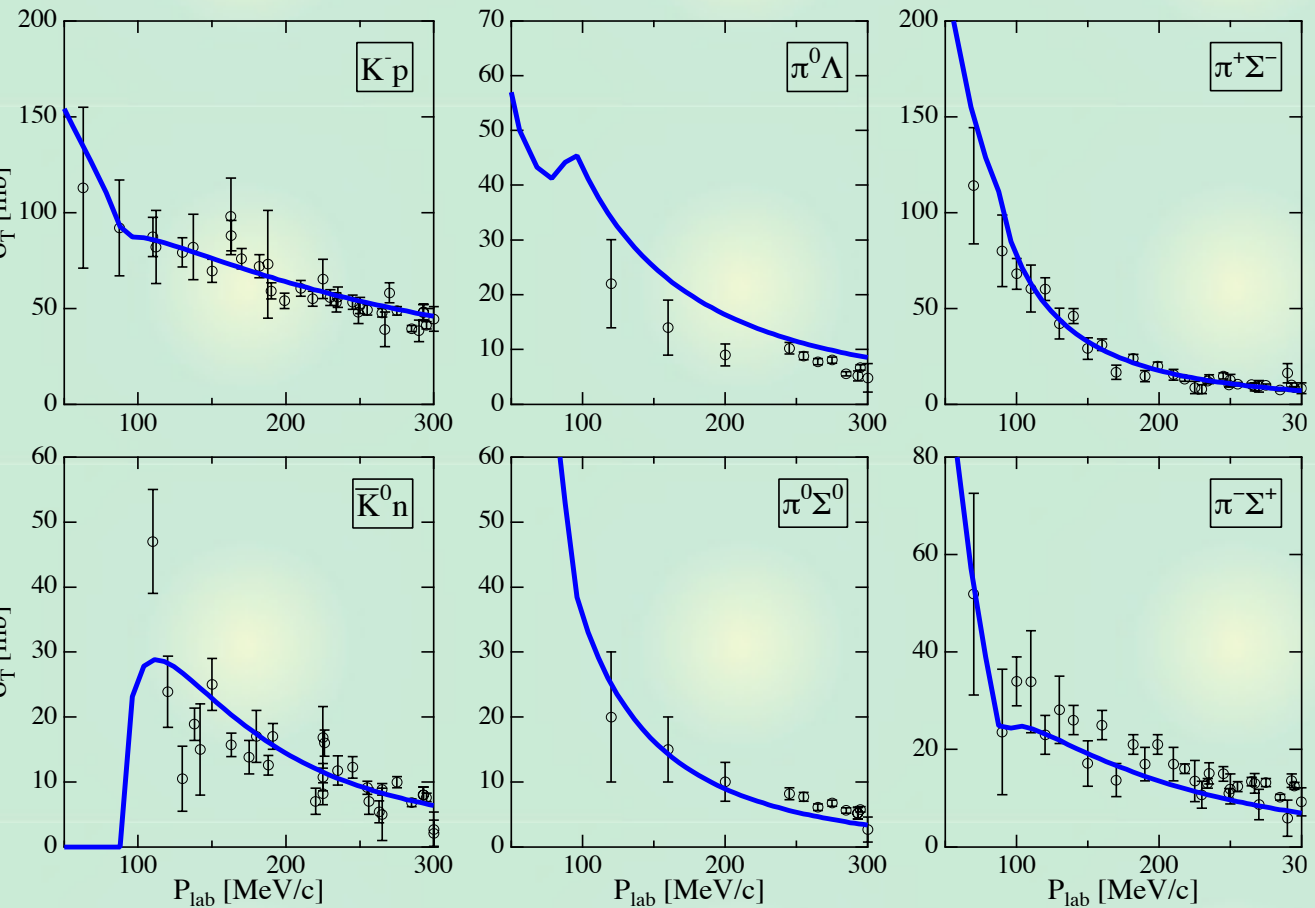
J. A. Oller, U. G. Meissner, *Phys. Lett.* B500, 263 (2001),

M.F.M. Lutz, E. E. Kolomeitsev, *Nucl. Phys.* A700, 193 (2002), ... many others

It works successfully, also in $S=0$ sector, meson-meson scattering sectors, systems including heavy quarks, ...

The simplest model (1 parameter) v.s. experimental data

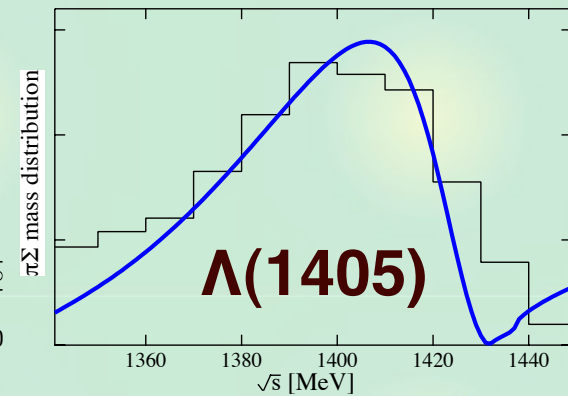
Total cross section of K-p scattering



Branching ratio

	γ	R_c	R_n
exp.	2.36	0.664	0.189
theo.	1.80	0.624	0.225

$\pi\Sigma$ spectrum



T. Hyodo, S.I. Nam, D. Jido, A. Hosaka, PRC68, 018201 (2003); PTP 112, 73 (2004)

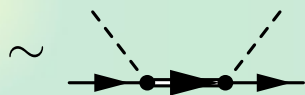
Good agreement with data above, at, and below $\bar{K}N$ threshold
 $\Lambda(1405)$ mass, width, couplings: prediction of the model

Two poles for one resonance

Poles of the amplitude in the complex plane: resonance

D. Jido, J.A. Oller, E. Oset, A. Ramos, U.G. Meissner, Nucl. Phys. A 723, 205 (2003);
 T. Hyodo, W. Weise, Phys. Rev. C 77, 035204 (2008)

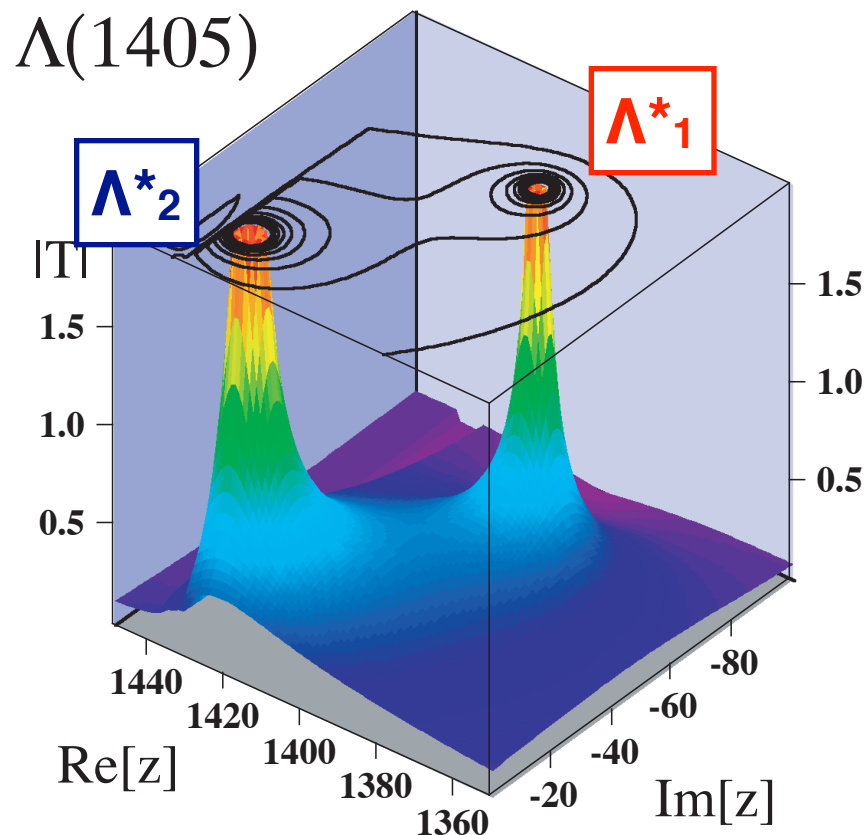
$$T_{ij}(\sqrt{s}) \sim \frac{g_i g_j}{\sqrt{s} - M_R + i\Gamma_R/2}$$



Physical Λ^* include two poles
 $\bar{K}N$ bound state
 + $\pi\Sigma$ resonance

short summary

- $\Lambda(1405)$: Λ^*_1 , Λ^*_2
- Λ^*_i masses, widths, Λ^*_i -MB couplings predicted



c.f.) Geng's talk

Origin of the two-pole structure

Leading order chiral interaction

T. Hyodo, W. Weise, Phys. Rev. C 77, 035204 (2008)

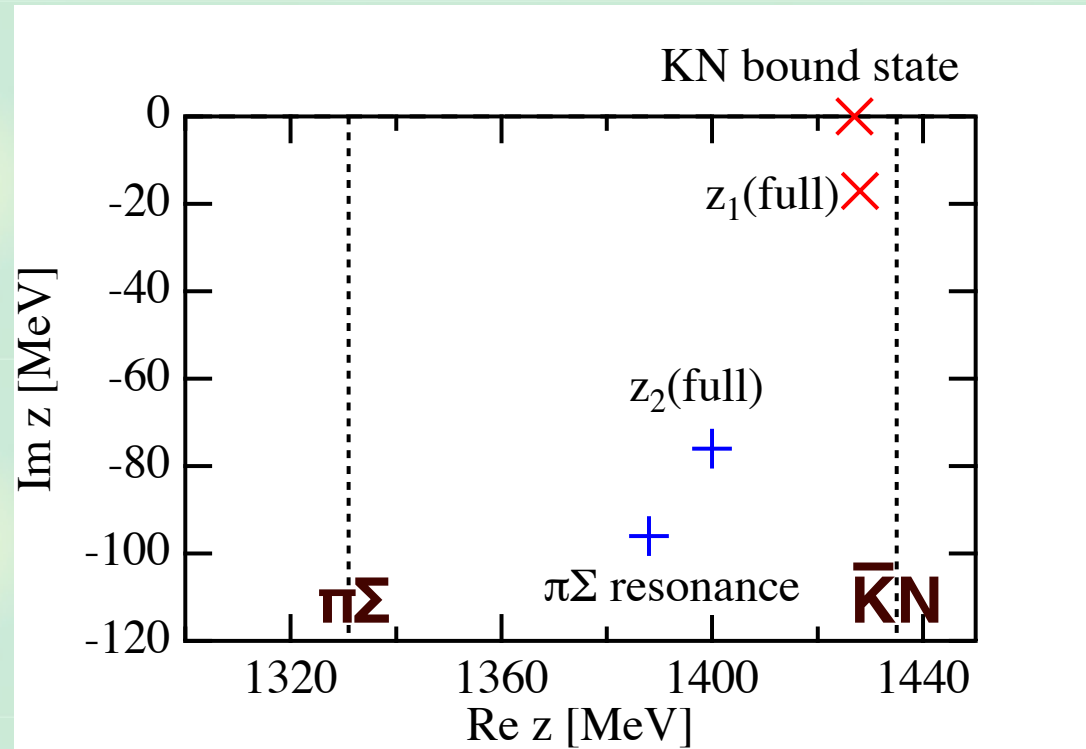
$$V_{ij} = -C_{ij} \frac{\omega_i + \omega_j}{4f^2}$$

$$C_{ij} = \begin{pmatrix} \bar{K}N & \pi\Sigma \\ 3 & -\sqrt{\frac{3}{2}} \\ -\sqrt{\frac{3}{2}} & 4 \end{pmatrix}$$

at threshold

$$\omega_i \sim m_i, \quad 3.3m_\pi \sim m_K$$

$$\Rightarrow V_{\bar{K}N} \sim 2.5V_{\pi\Sigma}$$



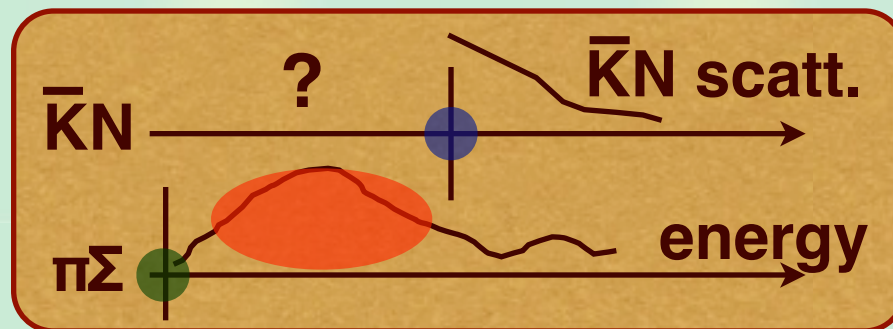
Very strong attraction in $\bar{K}N$ (higher energy) --> bound state
Strong attraction in $\pi\Sigma$ (lower energy) --> resonance

“realistic $\bar{K}N$ - $\pi\Sigma$ interaction”

Position of the second pole: model dependent

- higher order terms in the interaction kernel?
- energy dependence? (c.f. Ikeda’s talk)

--> **uncertainties in $\bar{K}N$ interaction below threshold**



Systematic χ^2 study including NLO interactions

Y. Ikeda, T. Hyodo, W. Weise, in preparation

- Precise data of $\bar{K}N$ scattering length <-- SIDDHARTA
- Precise data of $\pi\Sigma$ spectrum <-- FOPI (this afternoon?)
- Any information of $\pi\Sigma$ scattering length <-- lattice QCD?

==> the “realistic $\bar{K}N$ - $\pi\Sigma$ interaction”

\bar{K} in nuclei

- $\bar{K}N$ interaction is strongly attractive $\leftarrow \Lambda(1405)$.
Formation of (deeply) bound kaonic nuclei?

Y. Akaishi, T. Yamazaki, Phys. Rev. C65, 044005 (2002)

- Structure of the $\Lambda(1405)$, kaon condensation, ...

The simplest \bar{K} -nucleus: $\bar{K}NN$ three-body system

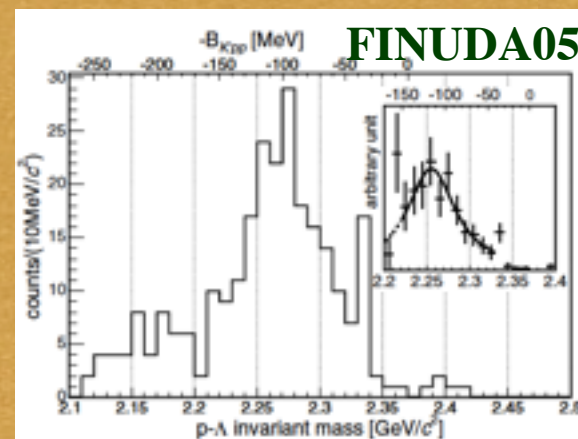
Theory: rigorous few-body calculations with realistic interactions

Yamazaki-Akaishi, Shevchenko, et al.,
Ikeda-Sato, Doté et al., Wycech-Green,

- System **bounds**
- Quantitative **difference**:
uncertainties in $\bar{K}N$ int. at
far below threshold

Experiment: some
“evidences” in ΛN mass
spectra

FINUDA,
DISTO,
OBELIX,
etc.

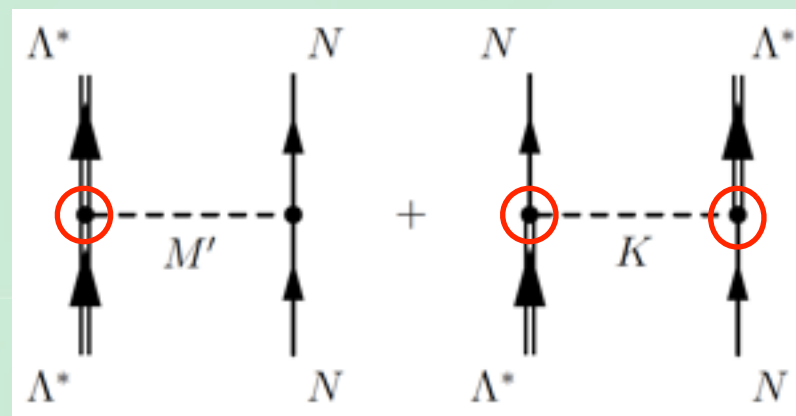


- **Interpretation** ($\pi\Sigma N$? FSI?)

Λ^* hypernuclei model

Regarding a $\bar{K}N(I=0)$ pair as the $\Lambda^*=\Lambda(1405)$, construct the “ Λ^*N potential” with the meson-exchange picture

A. Arai, M. Oka, S. Yasui, *Prog. Theor. Phys.* **119**, 103 (2008)



$\Leftarrow \Lambda^*$ structure seems to be surviving in $\bar{K}NN$ system.

T. Yamazaki, Y. Akaishi, *Phys. Rev. C* **76**, 045201 (2007),

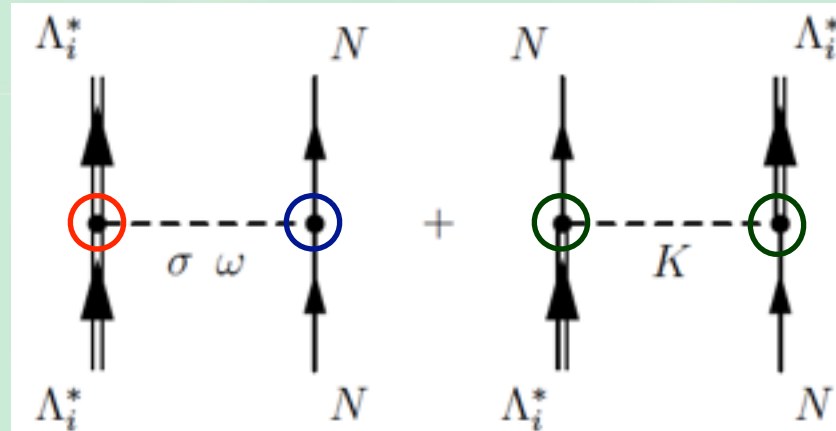
A. Doté, T. Hyodo, W. Weise, *Nucl. Phys. A* **804**, 197 (2008); *Phys. Rev. C* **79**, 014003 (2009)

Λ^* coupling constants: **unknown** (\Leftarrow FINUDA data).

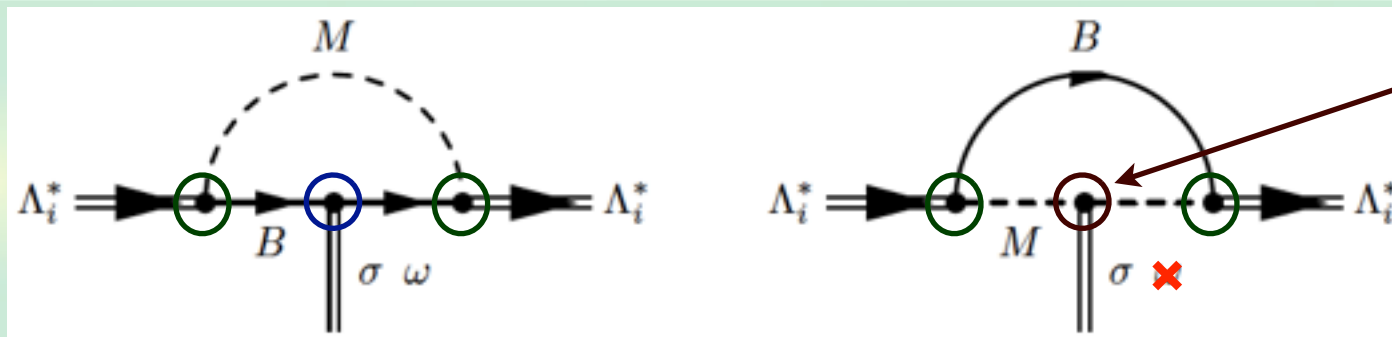
To determine the coupling and make predictions, we need a framework to describe the $\Lambda^* \Leftarrow$ **chiral unitary approach**

Λ^*N potential with meson-exchange picture

$\Lambda^*_i N$ potential with one boson exchange ($i=1,2$)



- $NN\sigma, NN\omega$ couplings: Jülich (model A) YN potential
- $\Lambda^*_i KN$ coupling: chiral unitary approach (pole residue)
- $\Lambda^*_i \Lambda^*_i \sigma, \Lambda^*_i \Lambda^*_i \omega$ couplings
 --> estimated by microscopic $MB=(\bar{K}N, \pi\Sigma)$ couplings



σ decay to $\pi\pi$
 $g_{KK\sigma} = 0$

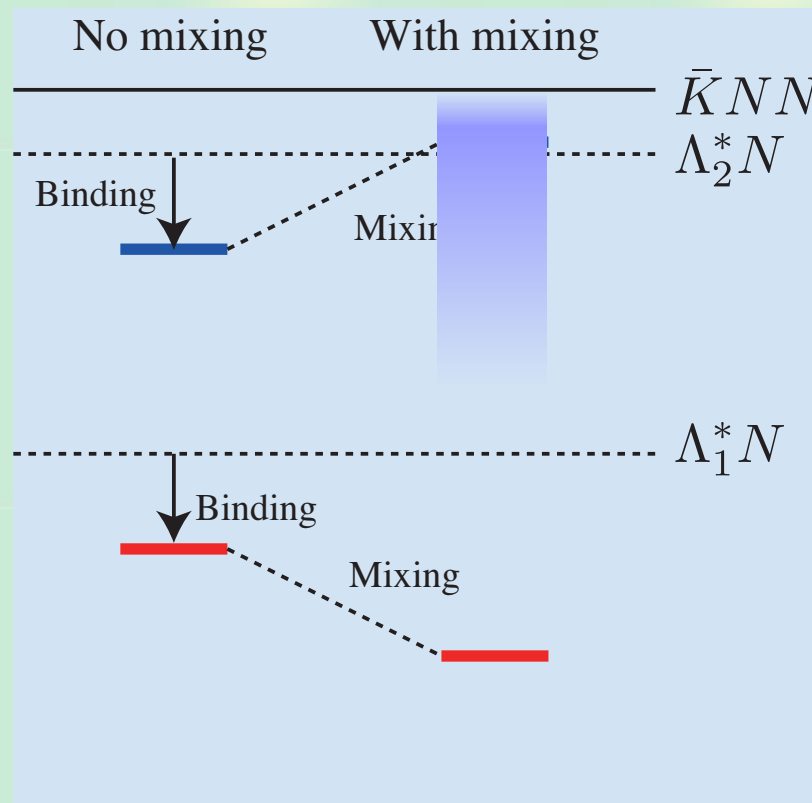
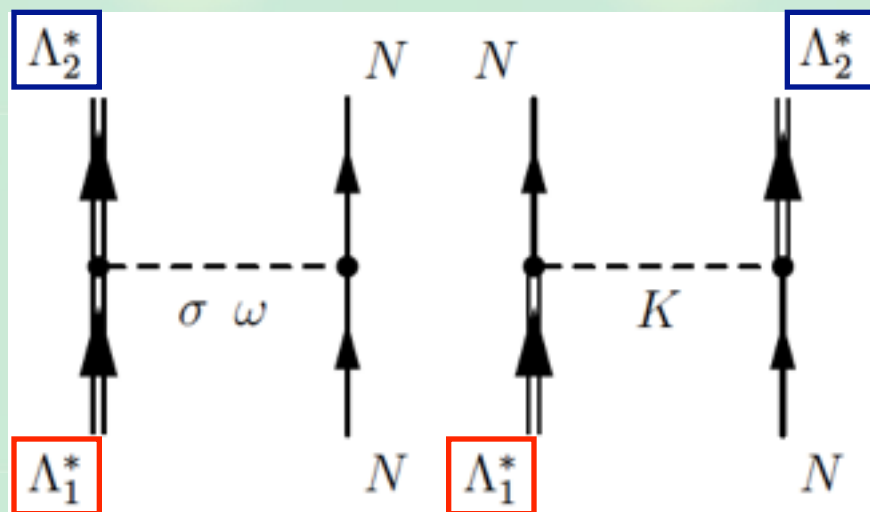
Λ^*N potential: mixing interaction

Chiral unitary approach --> two Λ^* states : Λ^*_1 , Λ^*_2

With sufficient attraction,

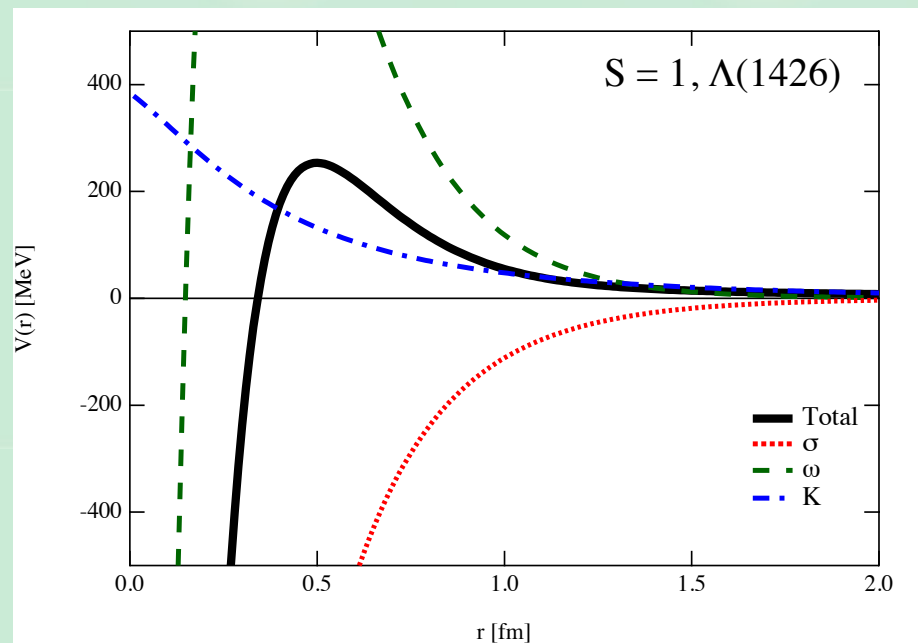
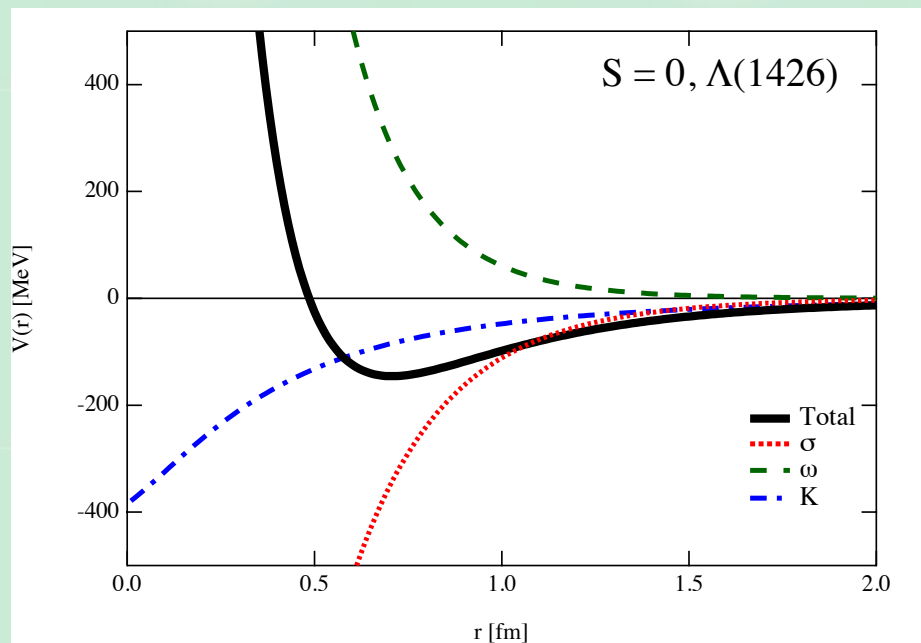
two Λ^*N bound states in B=2 system : Λ^*_1N , Λ^*_2N

There can be the mixing of $\Lambda^*_1N \leftrightarrow \Lambda^*_2N$



Λ^*N potential: each contribution

Diagonal potentials for Λ^*_2N in $S=0$ and $S=1$, s-wave



$S=0$: attractive pocket at intermediate range

\leftarrow K exchange is attractive

$S=1$: no intermediate attraction, but a short range dip

\leftarrow K exchange is repulsive

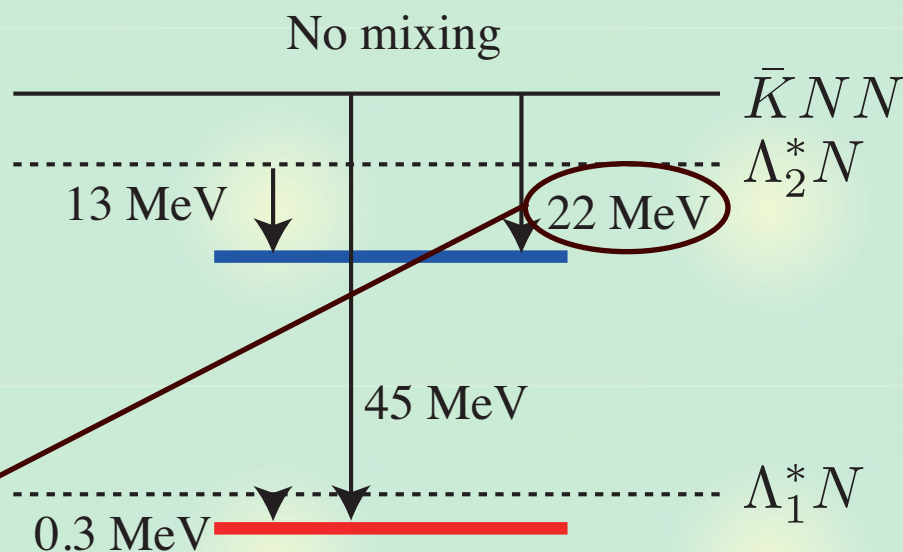
Qualitatively similar potential for Λ^*_1N

Λ^*N bound states without mixing

Solve the schrödinger equation for the s-wave $\Lambda^*_i N$ potential **without** the mixing interaction.

- no physical bound states in $S=1$ channels (consistent with the analysis of the volume integral)
- for $S=0$ we obtain the bound states in both Λ^*_i

binding from	Λ^*N th. [MeV]	$\bar{K}NN$ th. [MeV]
$\Lambda^*_2 N$	13.39	22.39
$\Lambda^*_1 N$	0.34	45.34



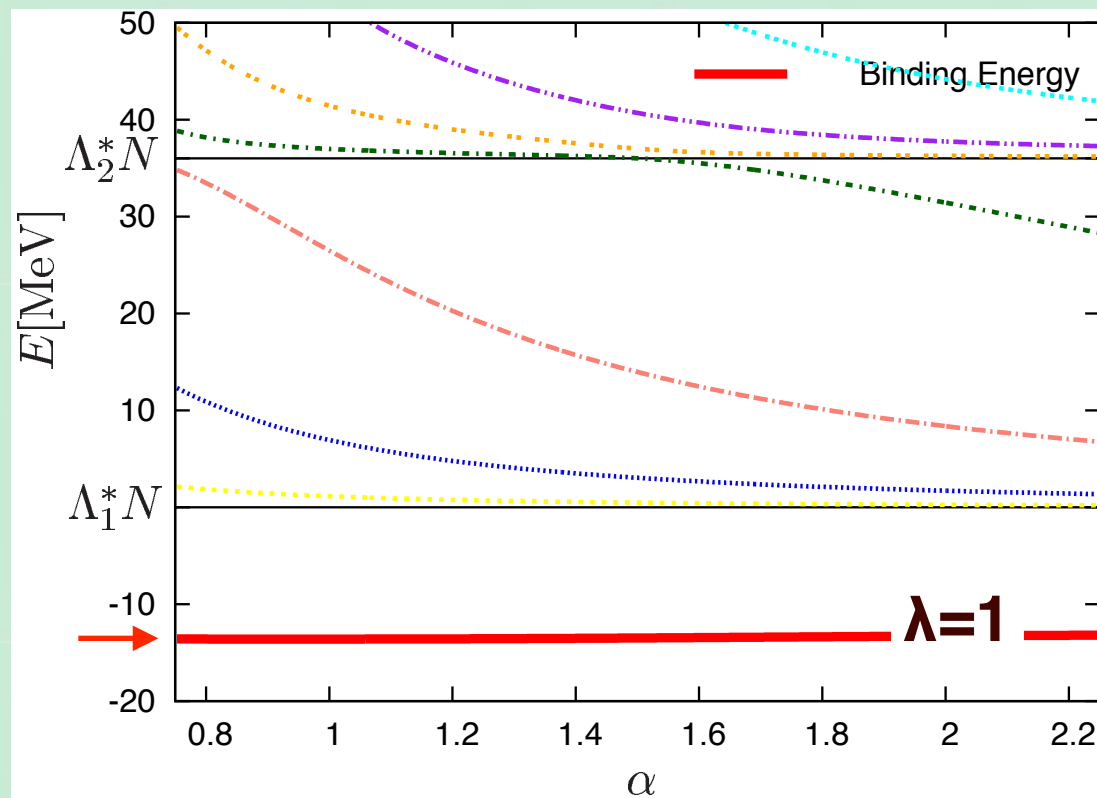
Similar value (20 ± 3 MeV) in KNN single-channel approach

Λ^*N bound states with mixing

With mixing, the higher state becomes a **resonance**.

Real scaling method \approx changing the box size α

λ : strength of the mixing interaction, physical for $\lambda=1$



resonance
(compact object)
--> **stable** against
the box size

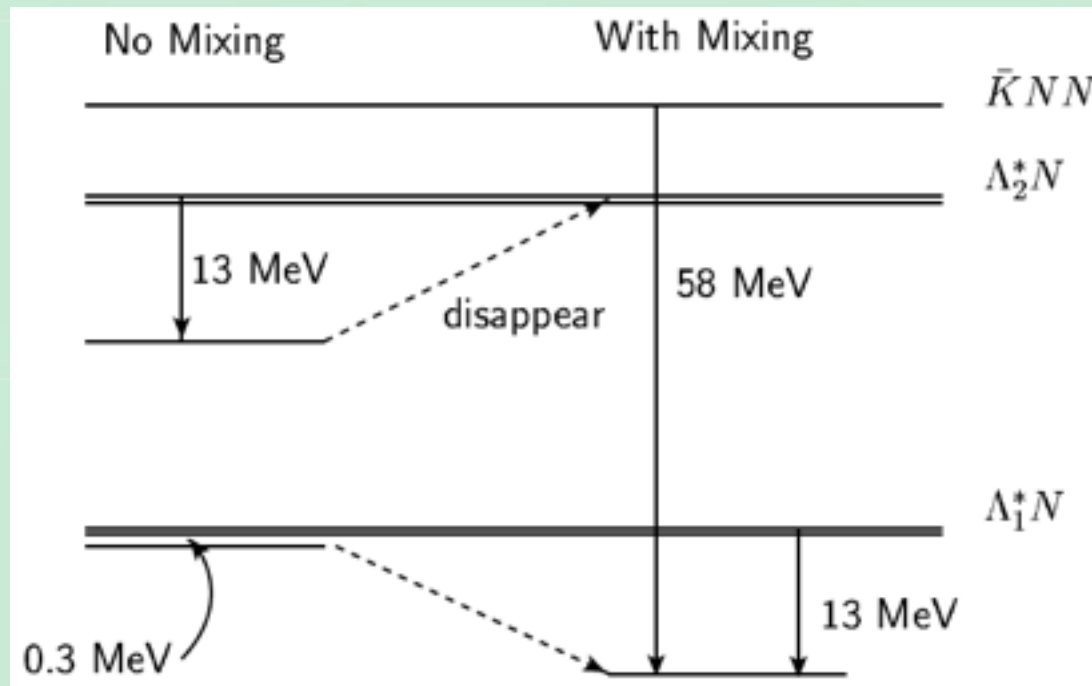
The lower energy state bounds more.

The higher energy state disappears (above $\Lambda_2^* N$ threshold?)₁₇

Result of Λ^*N bound states

Result in one figure:

taken from T. Uchino, Master thesis



decomposition of constituents

$$(\Lambda^*N) \sim 0.7(\Lambda_1^*N) + 0.3(\Lambda_2^*N)$$


$$\sim 0.5(\bar{K}NN) + 0.5(\pi\Sigma N)$$


substantial mixture of $\pi\Sigma N$ component

- The Λ^*N bound state decays into $\pi\Sigma N$ and YN .
- Disappeared state could be a very broad state.
- Physical Λ^* (especially the lower one) has a finite width.
- Comparison with three-body calculation (Ikeda et al)


Summary: $\bar{K}N$ interaction

We study the $\bar{K}N$ - $\pi\Sigma$ system and $\Lambda(1405)$ based on chiral SU(3) symmetry and unitarity

 Chiral low energy theorem: constrains for the NG boson dynamics

 Two poles for the $\Lambda(1405)$
<-- attractive $\bar{K}N$ and $\pi\Sigma$ interactions


T. Hyodo and W. Weise, Phys. Rev. C 77, 035204 (2008)

 Systematic study for the $\bar{K}N$ - $\pi\Sigma$ system
<-- new data, such as $\bar{K}N$ scattering length, $\pi\Sigma$ spectrum are called for.


Y. Ikeda, T. Hyodo, W. Weise, in preparation

Summary: Λ^*N interaction

We study the Λ^*N two-body system based on the Λ^*N potential with chiral SU(3) dynamics.

 Chiral dynamics: **two states** Λ^*_1, Λ^*_2

 Both Λ^*_i generate bound states with N in spin **S=0** channels \leftarrow K exchange

 With the mixing, **the lower state bounds more**, and **the higher state dissolves**.

mass of $\Lambda^*N \sim 2316\text{-}2322$ MeV

\leftarrow substantial **mixture of $\pi\Sigma N$**