

# $\Lambda(1405)$ Resonance in Chiral SU(3)-Dynamics



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2007, Dec. 10th 1

# Introduction : (well) known facts on $\Lambda(1405)$

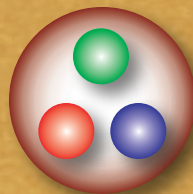
$\Lambda(1405) : J^P = 1/2^-, I = 0$

**Mass :  $1406.5 \pm 4.0$  MeV**

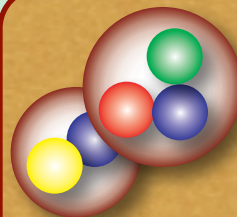
**Width :  $50 \pm 2$  MeV**

**Decay mode :  $\Lambda(1405) \rightarrow (\pi\Sigma)_{I=0}$  **100%****

“naive” quark model  
: p-wave  
~1600 MeV?



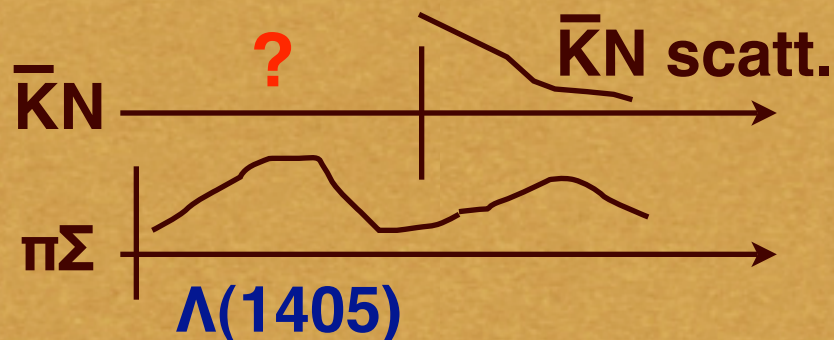
N. Isgur and G. Karl, PRD18, 4187 (1978)



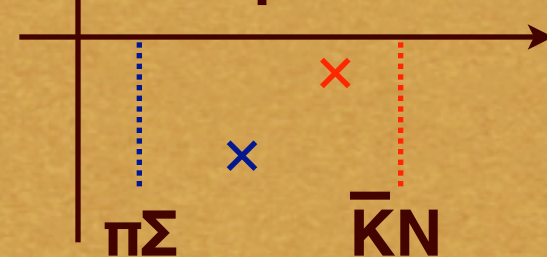
**Coupled channel  
multi-scattering**

R.H. Dalitz, T.C. Wong and  
G. Rajasekaran, PR153, 1617 (1967)

$\bar{K}N$  int.  
below  
threshold



**Two poles?**



# Contents



## Phenomenology of $\bar{K}N$ interaction

Construction of local  $\bar{K}N$  potential by chiral dynamics

With W. Weise, in preparation (about to submit)

Application to three-body  $\bar{K}NN$  system

With A. Doté, W. Weise, in preparation



## Structure of the $\Lambda(1405)$

Behavior at large  $N_c$

With L. Roca, D. Jido, in preparation

Dynamical or CDD (genuine quark state) ?

With D. Jido, A. Hosaka, in preparation

Electromagnetic properties

With T. Sekihara, D. Jido, in preparation

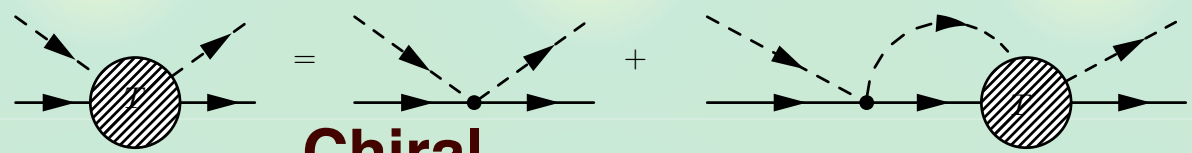
next  
opportunity...

# Chiral unitary approach

**S = -1,  $\bar{K}N$  s-wave scattering :  $\Lambda(1405)$  in  $l=0$**

- Interaction  $\leftarrow$  chiral symmetry
- Amplitude  $\leftarrow$  unitarity (coupled channel)

$$T = \frac{1}{1 - VG} V$$

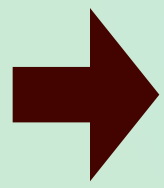


**Chiral  
(WT interaction)**

**cutoff  
(subtraction  
constant)**

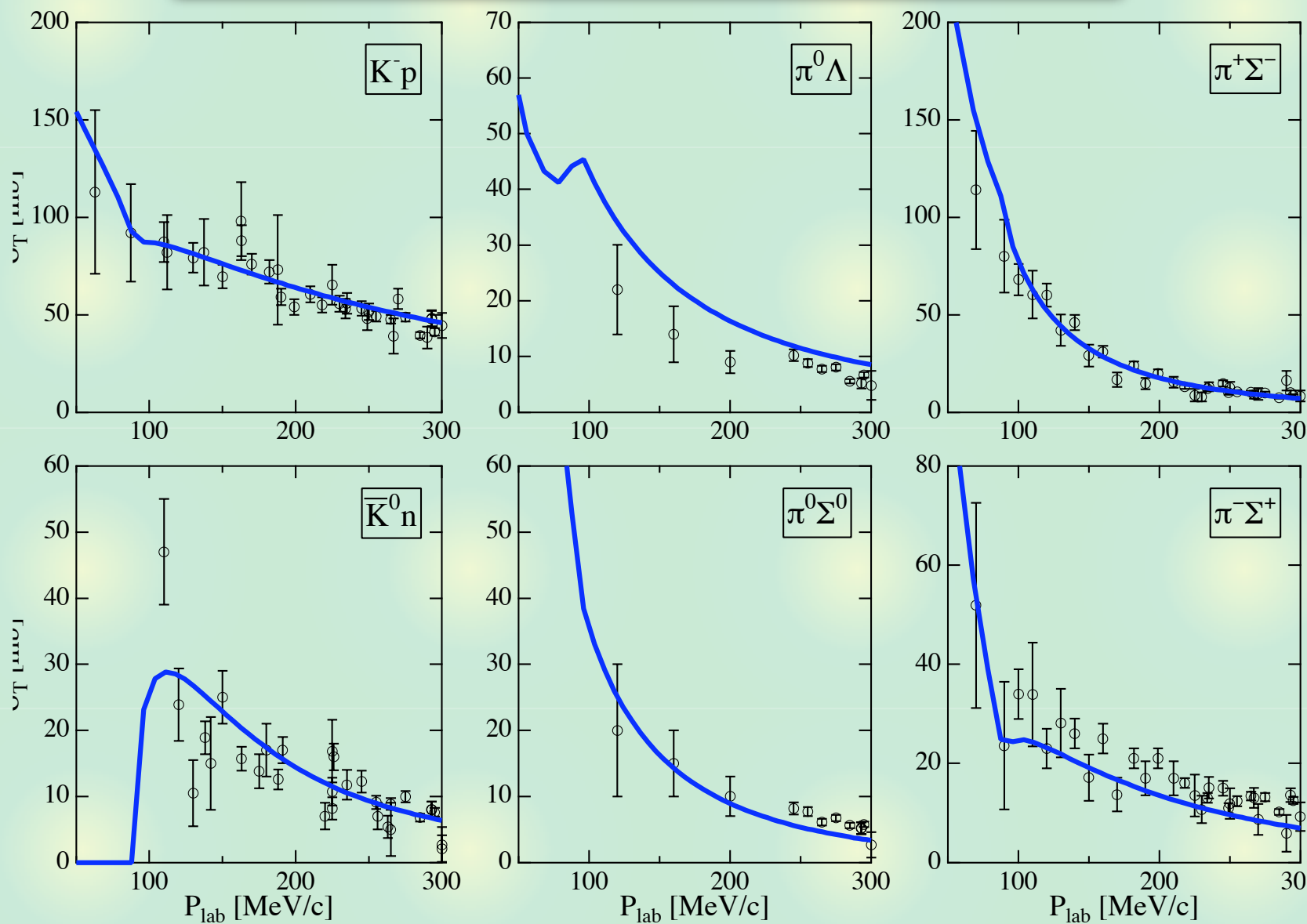
N. Kaiser, P. B. Siegel and W. Weise, Nucl. Phys. A594, 325 (1995)  
 E. Oset and A. Ramos, Nucl. Phys. A635, 99 (1998)  
 J. A. Oller and U. G. Meissner, Phys. Lett. B500, 263 (2001)  
 M.F.M. Lutz and E. E. Kolomeitsev, Nucl. Phys. A700, 193 (2002),  
 ... many others

**Interaction is strong  
Bound state below threshold**



**non-perturbative  
framework**

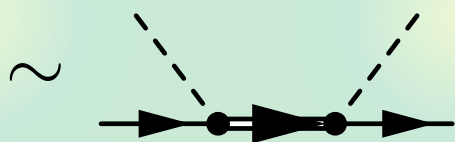
# Total cross sections of $K^-p$ scattering



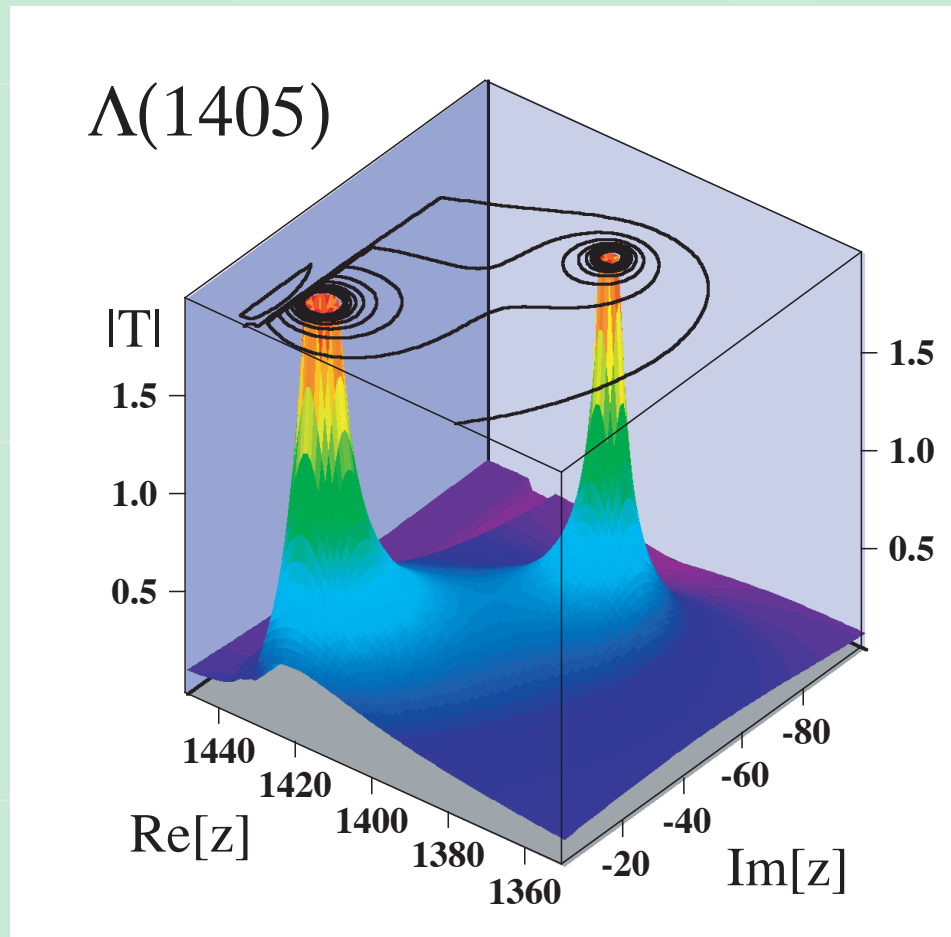
# Description of the resonances

## Poles of the amplitude : resonance

$$T_{ij}(\sqrt{s}) \sim \frac{g_i g_j}{\sqrt{s} - M_R + i\Gamma_R/2}$$

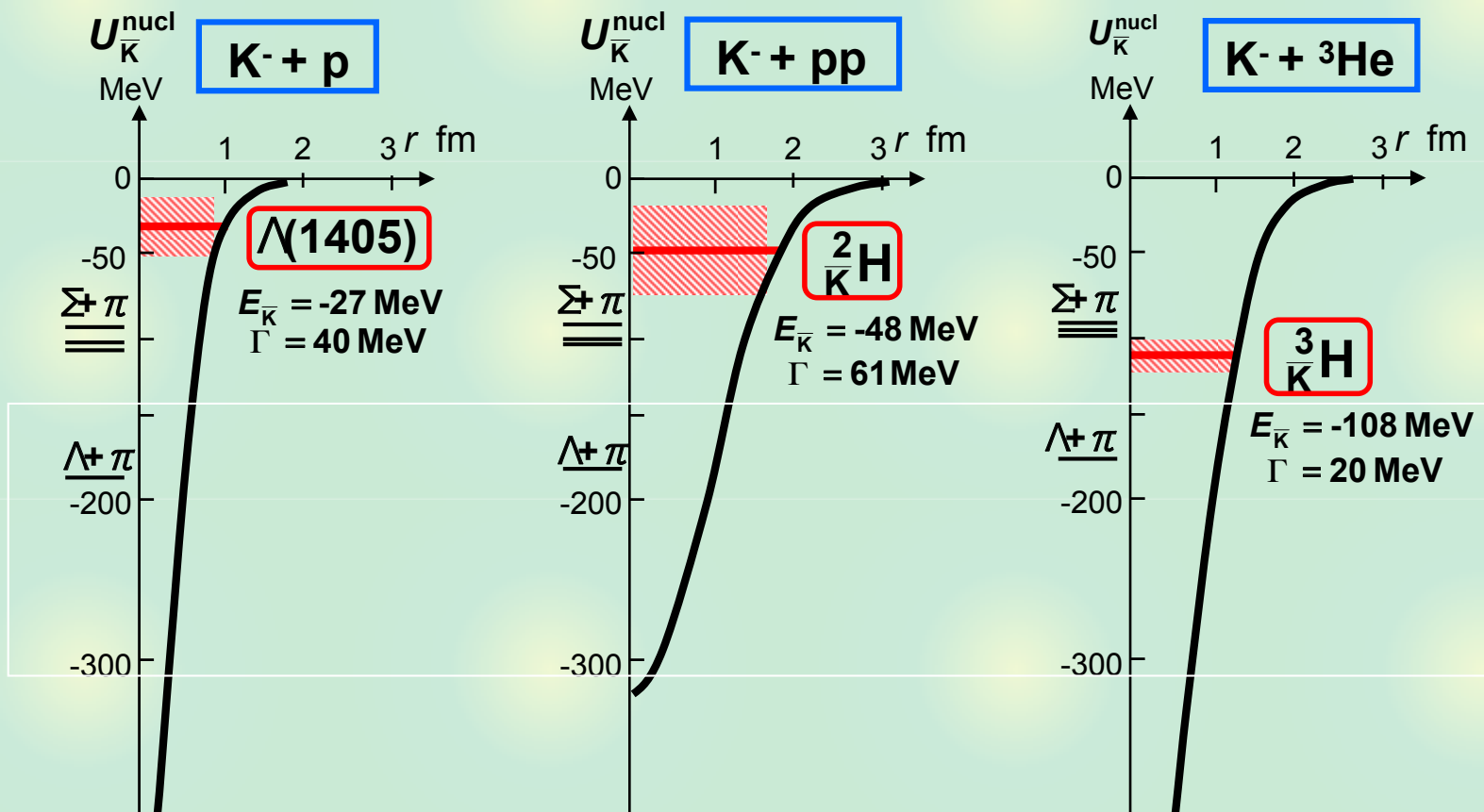


<b>Real part</b>	<b>Mass</b>
<b>Imaginary part</b>	<b>Width/2</b>
<b>Residues</b>	<b>Couplings</b>



**Successful description of  $\bar{K}N$  scattering**  
**Two poles are found for the  $\Lambda(1405)$**

# Deeply bound (few-body) kaonic nuclei?




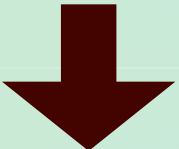
Potential is purely phenomenological.  
What does chiral dynamics tell us about it?

# Effective interaction based on chiral SU(3) dynamics

Result of chiral dynamics --> **local potential**

**Coupled-channel BS**  $T_{ij}(\sqrt{s})$   
**+ real interaction**  $V_{ij}(\sqrt{s})$

 **(exact)**

  
**few-body  
kaonic nuclei**

**Single-channel BS**  $T^{\text{eff}}(\sqrt{s}) = T_{ii}(\sqrt{s})$   
**+ complex interaction**  $V^{\text{eff}}(\sqrt{s})$

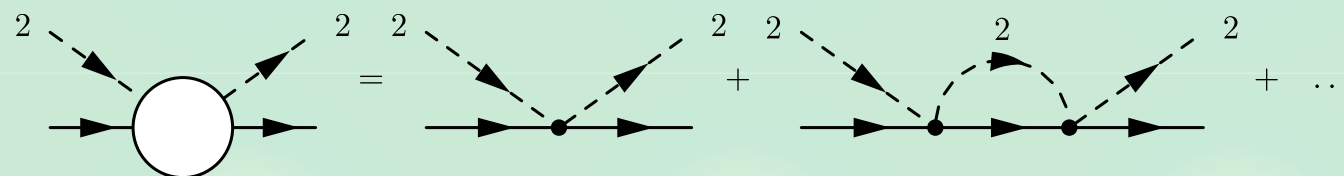
 **(approximate)**

**Schrödinger equation**  $f^{\text{eff}}(\sqrt{s}) \sim T^{\text{eff}}(\sqrt{s})$   
**+ local potential**  
**complex, energy-dependent**  $U^{\text{eff}}(r, \sqrt{s})$

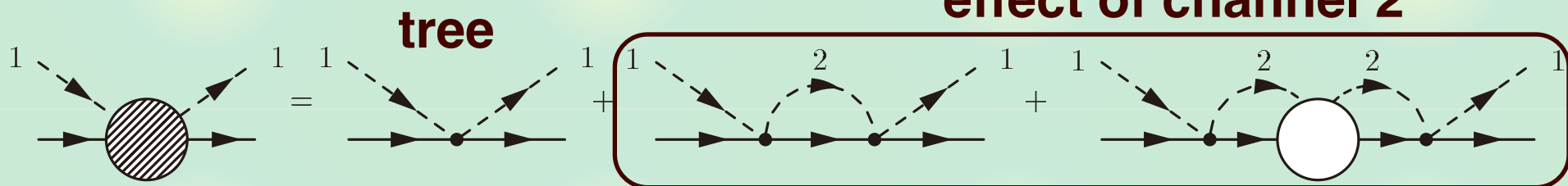


# Construction of the single channel interaction

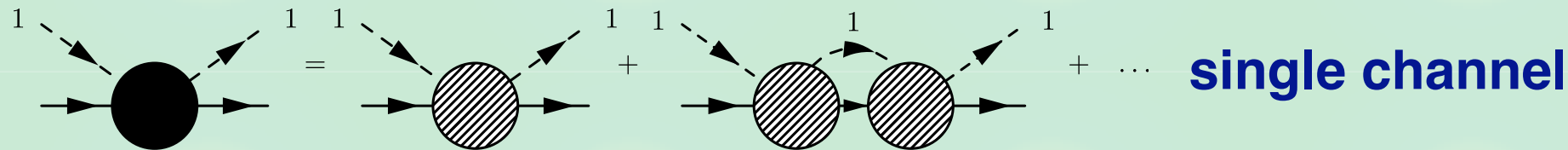
## Resummation of the channel to be eliminated



$$T_{22}^{\text{single}} = V_{22} + V_{22}G_2T_{22}^{\text{single}}$$



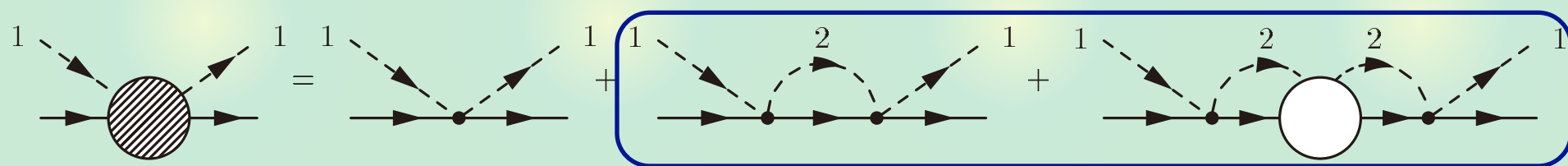
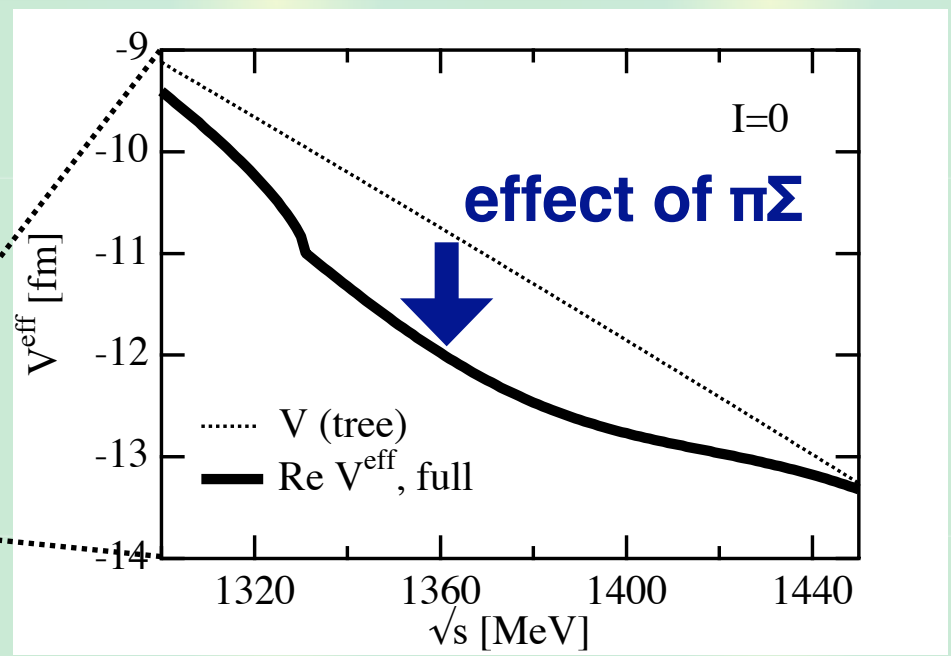
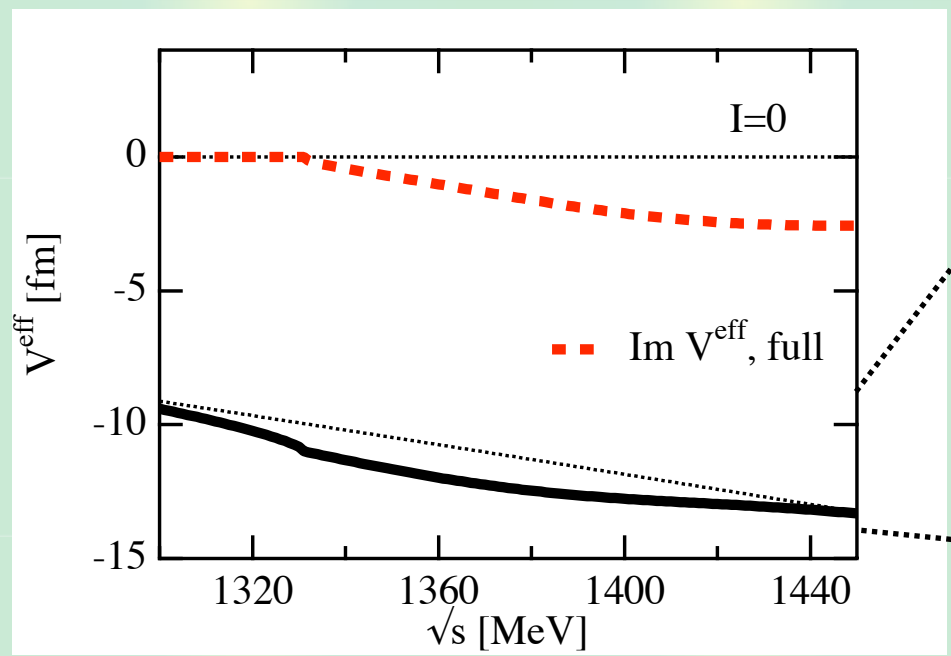
$$V^{\text{eff}} = V_{11} + V_{12}G_2V_{21} + V_{12}G_2T_{22}^{\text{single}}G_2V_{21}$$



$$T_{11} = T^{\text{eff}} = V^{\text{eff}} + V^{\text{eff}}G_1T^{\text{eff}}$$

Equivalent to the coupled-channel equations

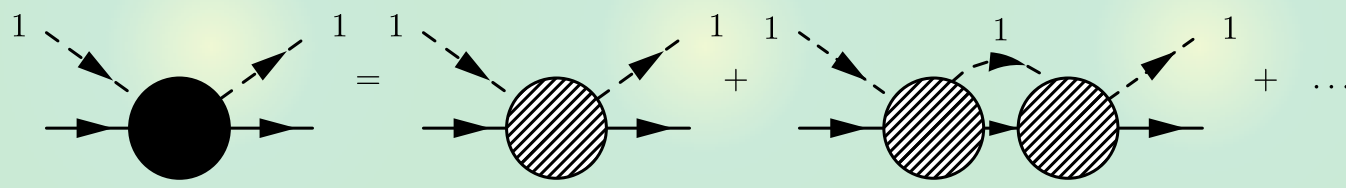
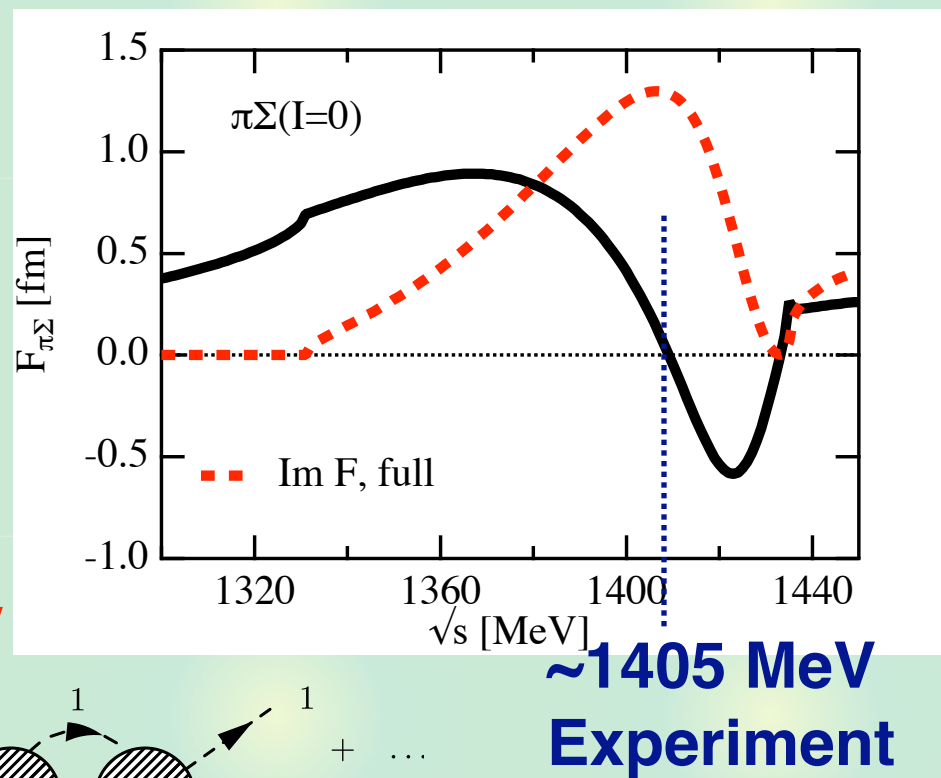
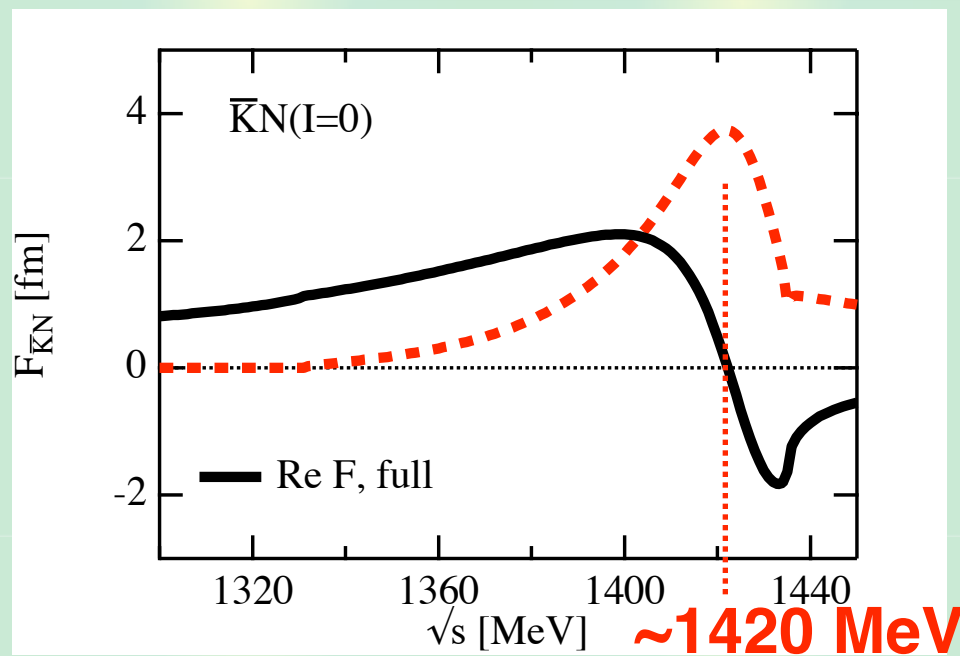
# Single channel $\bar{K}N$ interaction with $\pi\Sigma$ dynamics



**Strength : comparable with the WT term**

**~ 1/2 of phenomenological (Akaishi-Yamazaki) potential**  
 **$\pi\Sigma$  resummation : small but pole exists**

# Scattering amplitude in $\bar{K}N$ and $\pi\Sigma$



**Resonance in  $\bar{K}N$  : around 1420 MeV**  
 <-- two-pole structure (coupled-channel)

**Binding energy :  $B = 12$  MeV <--> 27 MeV**

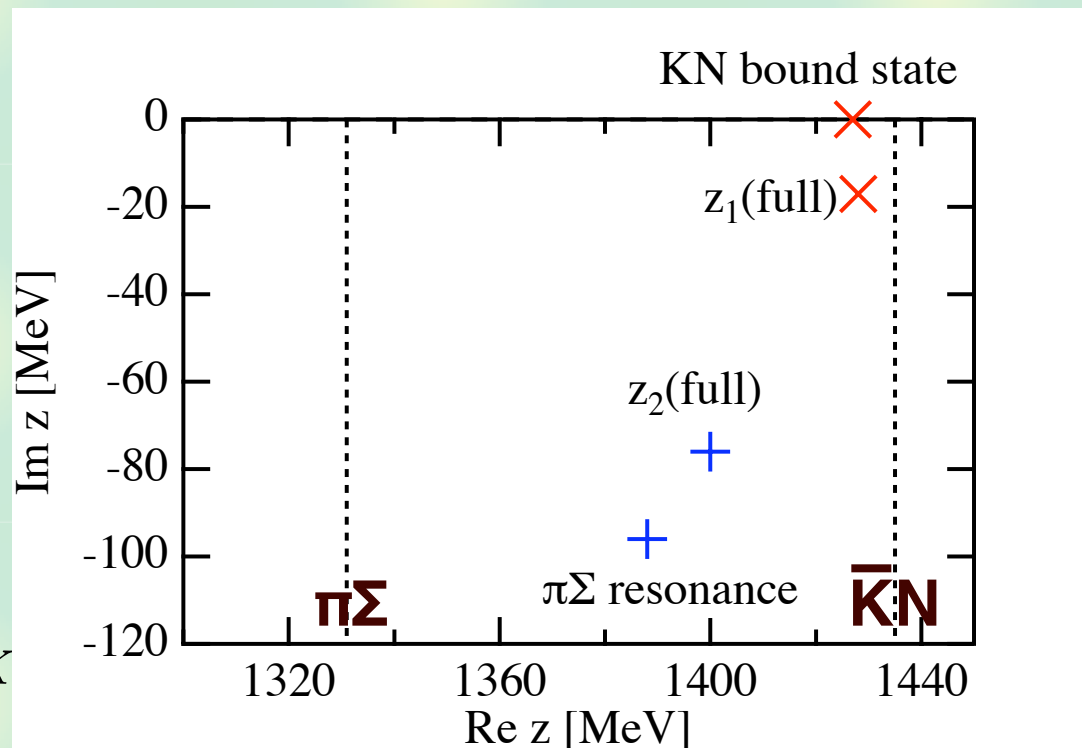
# Origin of the two-pole structure

## Chiral interaction

$$V_{ij} = -C_{ij} \frac{\omega_i + \omega_j}{4f^2}$$

$$C_{ij} = \begin{pmatrix} \bar{K}N & \pi\Sigma \\ 3 & -\sqrt{\frac{3}{2}} \\ -\sqrt{\frac{3}{2}} & 4 \end{pmatrix}$$

$$\omega_i \sim m_i, \quad 3.3m_\pi \sim m_K$$



**Very strong attraction in  $\bar{K}N$  (higher energy) --> bound state**  
**Strong attraction in  $\pi\Sigma$  (lower energy) --> resonance**

Two poles : natural consequence of chiral interaction

higher order correction? --> theoretical uncertainty (later)

B. Borasoy, R. Nissler, W. Weise, *Eur. Phys. J. A25*, 79-96 (2005)

# Comparison with phenomenological potential

## Chiral interaction

$$V_{ij} = -C_{ij} \frac{\omega_i + \omega_j}{4f^2}$$

$$C_{ij} = \begin{pmatrix} \bar{K}N & \pi\Sigma \\ 3 & -\sqrt{\frac{3}{2}} \\ -\sqrt{\frac{3}{2}} & 4 \end{pmatrix}$$

## phenomenological

T. Yamazaki, Y. Akaishi,  
Phys. Rev. C76, 045201 (2007)

$$v_{ij}(r) \sim - \begin{pmatrix} \bar{K}N & \pi\Sigma \\ 436 & 412 \\ 412 & 0 \end{pmatrix} g(r)$$

## Absence of $\pi\Sigma$ diagonal coupling

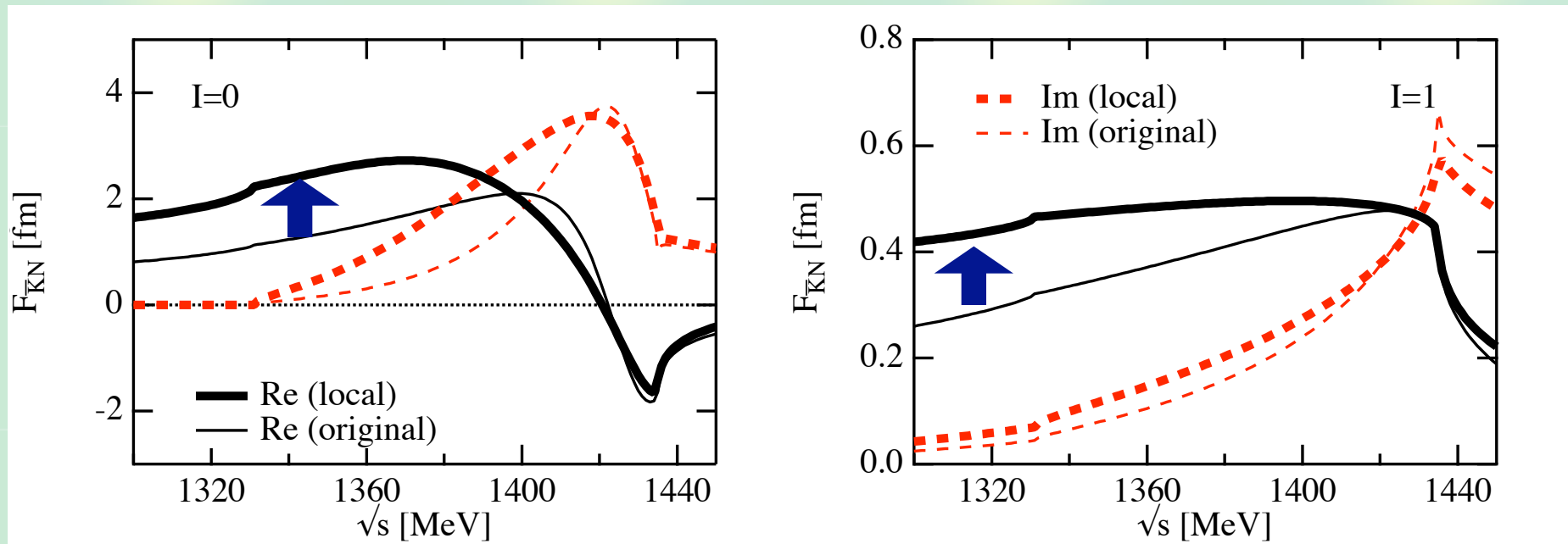
--> absence of  $\pi\Sigma$  dynamics, resonance

--> strong ( $\times 2$ ) attractive interaction in  $\bar{K}N$

$\pi\Sigma \rightarrow \pi\Sigma$  attraction : flavor SU(3) symmetry

energy dependence : derivative coupling

# $\bar{K}N$ amplitude with local potential



$$U(r, \sqrt{s}) = \frac{M_N V^{\text{eff}}(\sqrt{s})}{2\sqrt{s}\tilde{\omega}(\sqrt{s})} g(r) \quad g(r) = \frac{e^{-r^2/b^2}}{\pi^{3/2}b^3}$$

$b = 0.47$  fm : to reproduce the resonance

agreement around threshold : OK

**Deviation** at lower energy : model dependence

BS eq.  $\leftrightarrow$  local potential + Schrödinger eq.

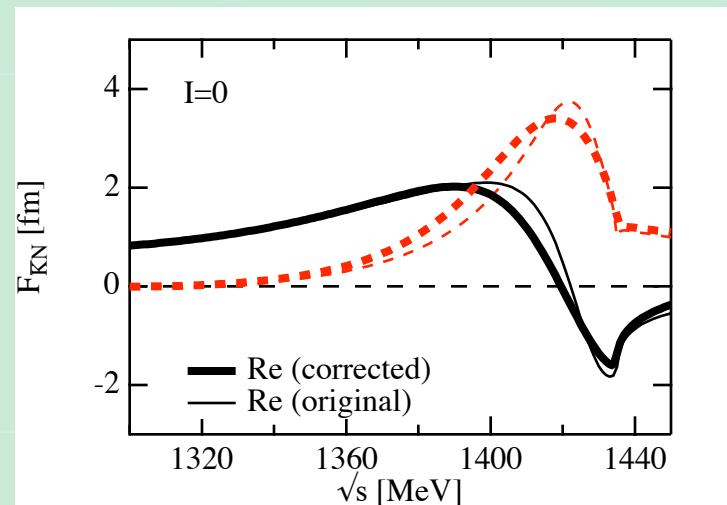
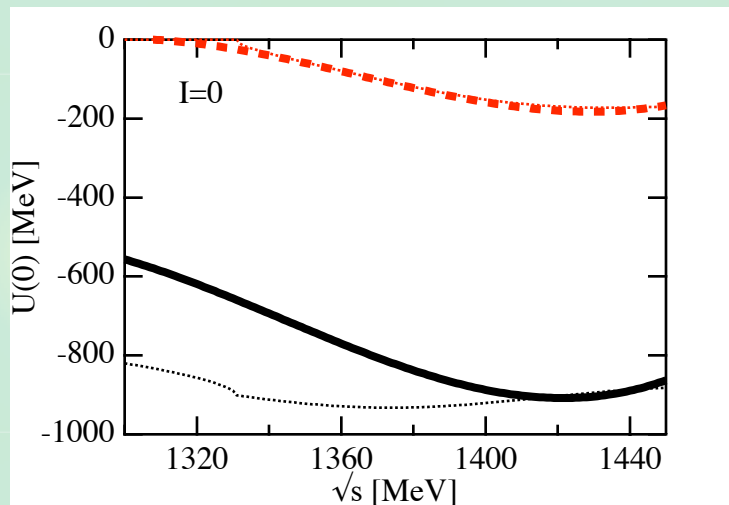
## Summary 1 : $\bar{K}N$ interaction

We derive single-channel local potentials based on chiral SU(3) dynamics.

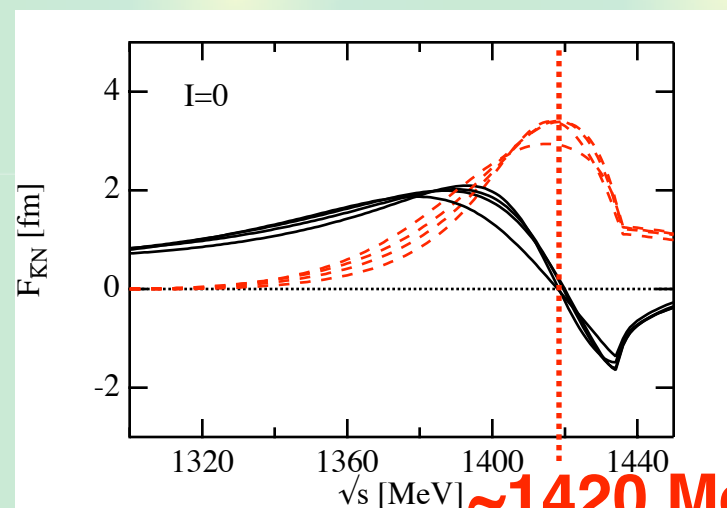
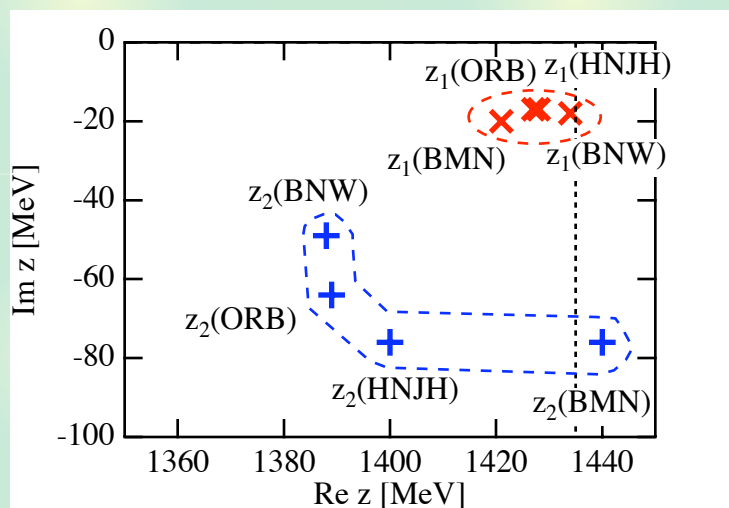
- The strength of the  $\bar{K}N$  interaction is comparable with the  $WT$  term.
- Resonance structure in  $\bar{K}N$  appears at around **1420 MeV**  $\leftarrow$  two-pole  $\Lambda(1405)$ .
- Two poles are the consequence of **two attractive interactions in  $\bar{K}N$  and  $\pi\Sigma$** .
- Extrapolation of local potential to the deep region is **model dependent**.

# Theoretical uncertainties

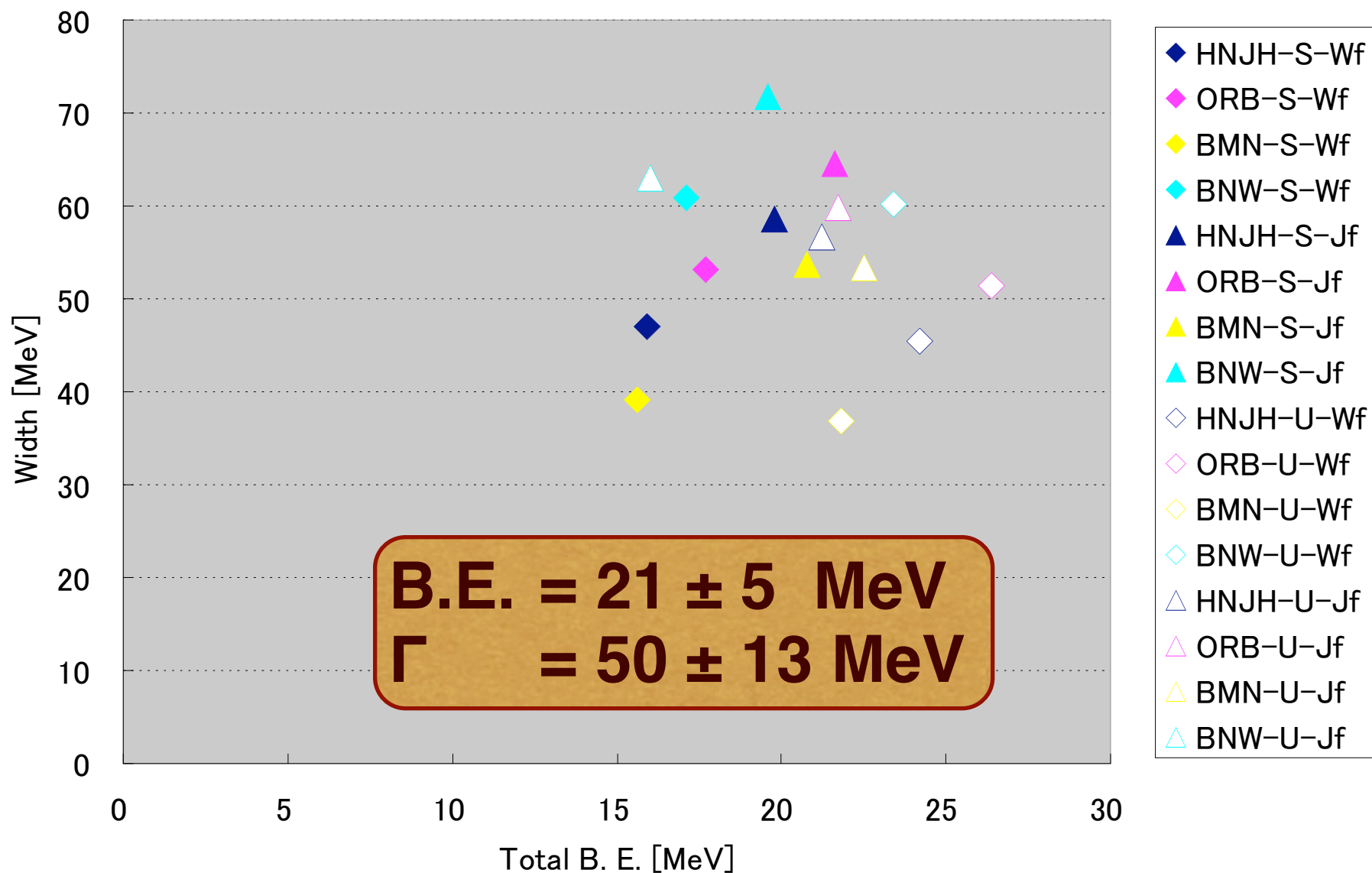
## Strength of the potential



## Different models of chiral dynamics





**$\bar{K}NN$  state with local potential**

## Summary 2 : $\bar{K}NN$ system

We study the  $\bar{K}NN$  system with chiral SU(3) potentials in a variational approach.



With theoretical uncertainties,

$$\text{B.E.} = 21 \pm 5 \text{ MeV}$$

$$\Gamma = 50 \pm 13 \text{ MeV}$$

Phenomenological potential	B.E. $\sim 48$ MeV
( $\sim 2$ times stronger than ours)	$\Gamma \sim 60$ MeV

T. Yamazaki, Y. Akaishi, *Phys. Rev. C* **76**, 045201 (2007)

Faddeev with chiral interaction	B.E. $\sim 79$ MeV
(separable, non-rel, ...?)	$\Gamma \sim 74$ MeV

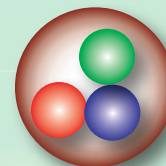
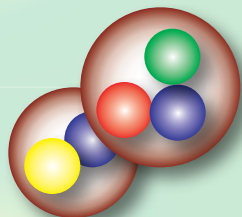
Y. Ikeda, T. Sato, *Phys. Rev. C* **76**, 035203 (2003)

Width :  $\bar{K}NN \rightarrow \pi YN$

No two-nucleon absorption :  $\bar{K}NN \rightarrow YN$

## Structure of dynamically generated resonances

**Resonances  $\sim$  quasi-bound two-body states**



**$\leftrightarrow$  in some case, CDD pole (genuine state).**

**c.f.  $\rho$  meson in  $\pi\pi$  scattering**

**$\leftarrow$  originate from the contracted resonance propagator  
in higher order terms**

**J.A. Oller, E. Oset and J.R. Pelaez, Phys. Rev. D59, 074001 (1999)**

**G. Ecker, J. Gasser, A. Pich, and E. de Rafael, Nucl. Phys. B321, 311 (1989)**

**analysis of  $N_c$  scaling  $\rightarrow \rho \sim q\bar{q}$**

**J.R. Pelaez, Phys. Rev. Lett. 92, 102001 (2004)**

**Baryon resonances?**

**$\rightarrow$  analysis of  $N_c$  scaling**

## Nc scaling in the model

**Introduce the  $N_c$  scaling into the model and study the behavior of resonance.**

$$m \sim \mathcal{O}(1), \quad M \sim \mathcal{O}(N_c), \quad f \sim \mathcal{O}(\sqrt{N_c})$$

**Leading order WT interaction has  $N_c$  dep.**

$$V = -C \frac{\omega}{2f^2} \sim \mathcal{O}(1/N_c) \quad (\Leftarrow C \sim \mathcal{O}(1))$$

**(for baryon and  $N_f > 2$ )**

$$V = -C \frac{\omega}{2f^2}, \quad \underline{C \sim \mathcal{O}(N_c)} \quad \Rightarrow V \sim \mathcal{O}(1)$$

T. Hyodo, D. Jido and A. Hosaka, Phys. Rev. Lett. 97, 192002 (2006)

T. Hyodo, D. Jido and A. Hosaka, Phys. Rev. D75, 034002 (2007)

**c.f. meson-meson scattering :  $V_{LO} \sim \mathcal{O}(1/N_c) = \text{trivial}$   
Nontrivial  $N_c$  dependence of the interaction is in **NLO**.**

**$S = -1$   $I = 0$  channel in  $SU(3)$  basis**

## Coupling strengths with $N_c$ dependence

$$V = -C \frac{\omega}{2f^2} \quad f \sim \mathcal{O}(\sqrt{N_c})$$

$$C_{ij}^{SU(3)}(N_c) = \begin{pmatrix} \mathbf{1} & \mathbf{8} & \mathbf{8} & \mathbf{27} \\ \frac{9}{2} + \frac{N_c}{2} & 0 & 0 & 0 \\ 3 & 0 & 0 & 0 \\ & 3 & & 0 \\ & & & -\frac{1}{2} - \frac{N_c}{2} \end{pmatrix}$$

**$C \propto N_c$  : finite interaction at  $N_c \rightarrow \infty$**

**Attractive** interaction in **singlet** channel  
: strong enough to make a **bound state**

**$S = -1$   $I = 0$  channel in Isospin basis**

## Coupling strengths with $N_c$ dependence

$$C_{ij}^I(N_c) = \begin{pmatrix} \bar{K}N & \pi\Sigma & \eta\Lambda & K\Xi \\ \frac{1}{2}(3 + N_c) & -\frac{\sqrt{3}}{2}\sqrt{-1 + N_c} & \frac{\sqrt{3}}{2}\sqrt{3 + N_c} & 0 \\ & 4 & 0 & \frac{\sqrt{3 + N_c}}{2} \\ & & 0 & -\frac{3}{2}\sqrt{-1 + N_c} \\ & & & \frac{1}{2}(9 - N_c) \end{pmatrix}$$

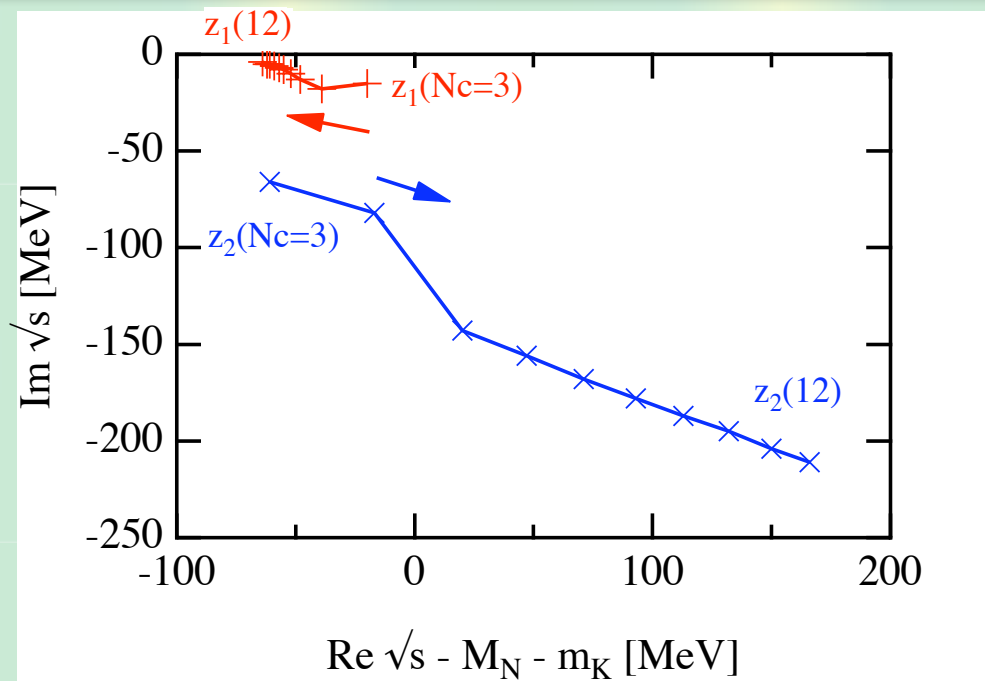
Off-diagonal couplings vanish at  $N_c \rightarrow \infty$

**Attractive** interaction in  $\bar{K}N \rightarrow \bar{K}N$

: strong enough to make a **bound state**

$K\Xi \rightarrow K\Xi$  : **attractive**  $\rightarrow$  **repulsive** for  $N_c > 9$

# Pole trajectories with varying $N_c$



**1 bound state** and **1 dissolving resonance**

$$\Gamma_R \neq \mathcal{O}(1)$$

**~ non-qqq (i.e. dynamical) structure**

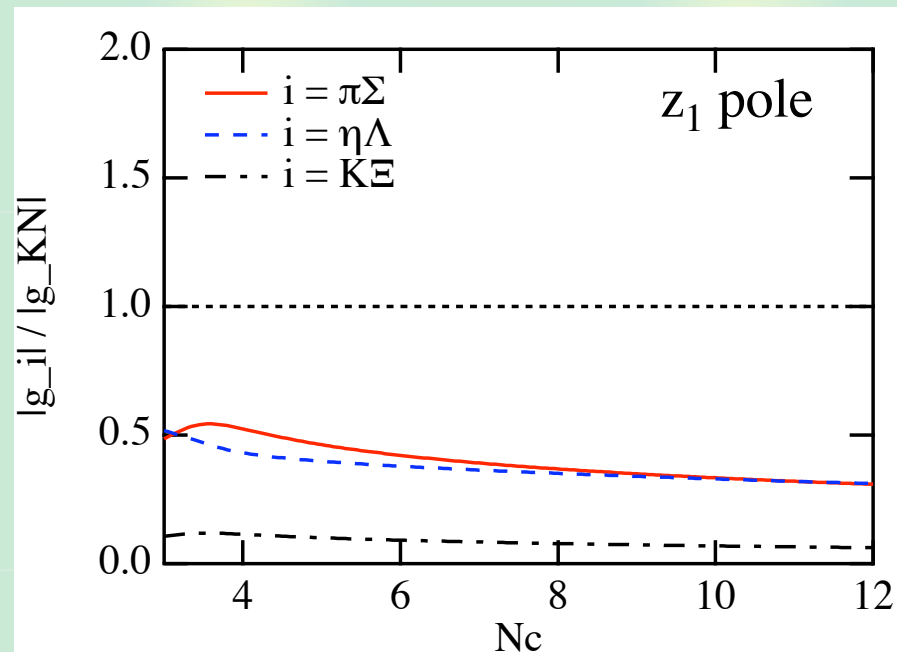
**Excited qqq baryon in large  $N_c$**

$$M_R \sim \mathcal{O}(N_c), \quad \Gamma_R \sim \mathcal{O}(1)$$

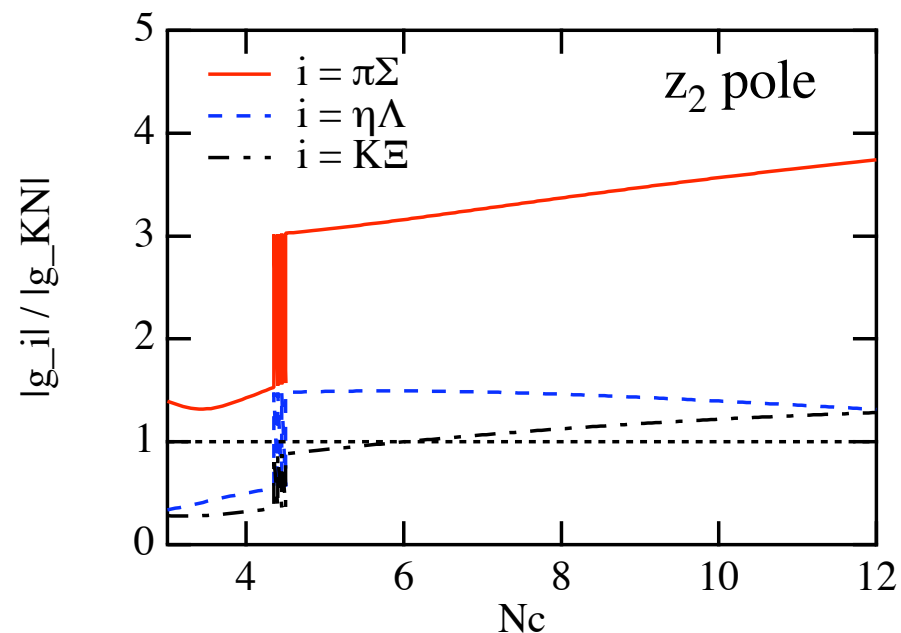
# Isospin components of the poles

## Residues in the isospin basis

$$\frac{|g_i|}{|g_{\bar{K}N}|} \begin{cases} < 1 : \bar{K}N \text{ dominant} \\ > 1 : \text{non } \bar{K}N \text{ dominant} \end{cases}$$



**bound state**  
 **$\bar{K}N$  dominant**



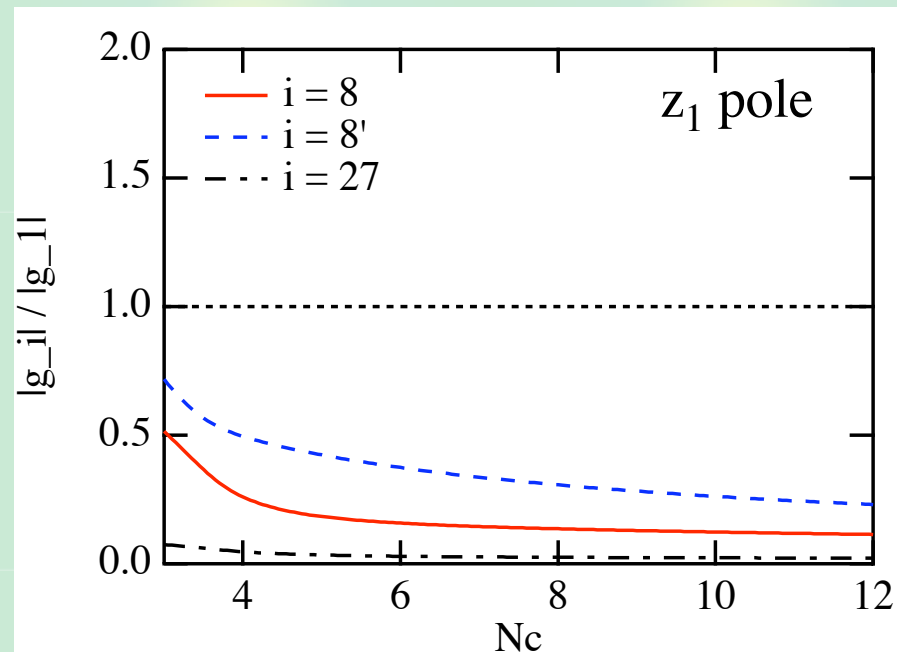
**dissolving**  
**other components**



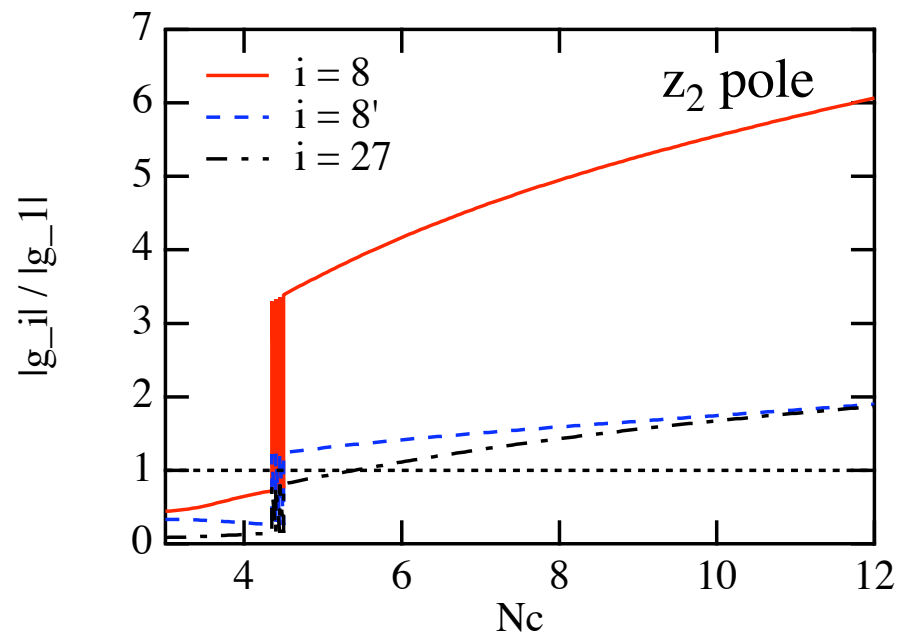
# SU(3) components of the poles

## Residues in the SU(3) basis

$$\frac{|g_i|}{|g_1|} \begin{cases} < 1 : \text{singlet dominant} \\ > 1 : \text{non singlet dominant} \end{cases}$$



**bound state  
1 dominant**



**dissolving  
other components**

## Summary 3 : Nc behavior of $\Lambda(1405)$

We study the Nc scaling of the  $\Lambda(1405)$



Large Nc limit

Existence of a **bound state** in “1” and  $\bar{K}N$  channel even in the **large Nc limit**



Behavior around  $N_c = 3$

1 bound state and 1 dissolving pole  
: signal of the **non-qqq state**.

Residues of the would-be-bound-state  
: dominated by “1” and  $\bar{K}N$   
: consistent with large Nc limit.