

# Exotic hadrons in s-wave chiral dynamics



**Tetsuo Hyodo<sup>a</sup>,**

*YITP, Kyoto<sup>a</sup>*

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## Motivation 1 : Exotic hadrons

**Exotic hadrons : more than 4 valence quarks**

**non-exotic**

$uds, u\bar{d}, udsu\bar{u}, u\bar{d}u\bar{u}, \dots$

**exotic (in this talk)**

$uudd\bar{s}, ud\bar{s}\bar{s}, \dots$

**not considered**

$uuddss, c\bar{c}g, \bar{u}\bar{u}\bar{d}\bar{d}\bar{s}, \dots$

**Experimentally**, they are exotic  $\sim 1/300$ .

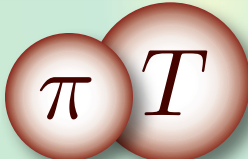
**Theoretically**, are they exotic?

--> There is no simple way to forbid exotic states in QCD, effective models, ...

--> Evidences of multiquark components in non-exotic hadrons.

**Why aren't the exotics observed??**

## Motivation 2 : Chiral unitary approaches

Hadron excited states  $\sim$  

- Interaction  $\leftarrow$  chiral symmetry
- Amplitude  $\leftarrow$  unitarity

R.H. Dalitz, and S.F. Tuan, *Ann. Phys. (N.Y.)* 10, 307 (1960)

J.H.W. Wyld, *Phys. Rev.* 155, 1649 (1967)

N. Kaiser, P. B. Siegel and W. Weise, *Nucl. Phys.* A594, 325 (1995)

E. Oset and A. Ramos, *Nucl. Phys.* A635, 99 (1998)

J. A. Oller and U. G. Meissner, *Phys. Lett.* B500, 263 (2001)

M.F.M. Lutz and E. E. Kolomeitsev, *Nucl. Phys.* A700, 193 (2002)

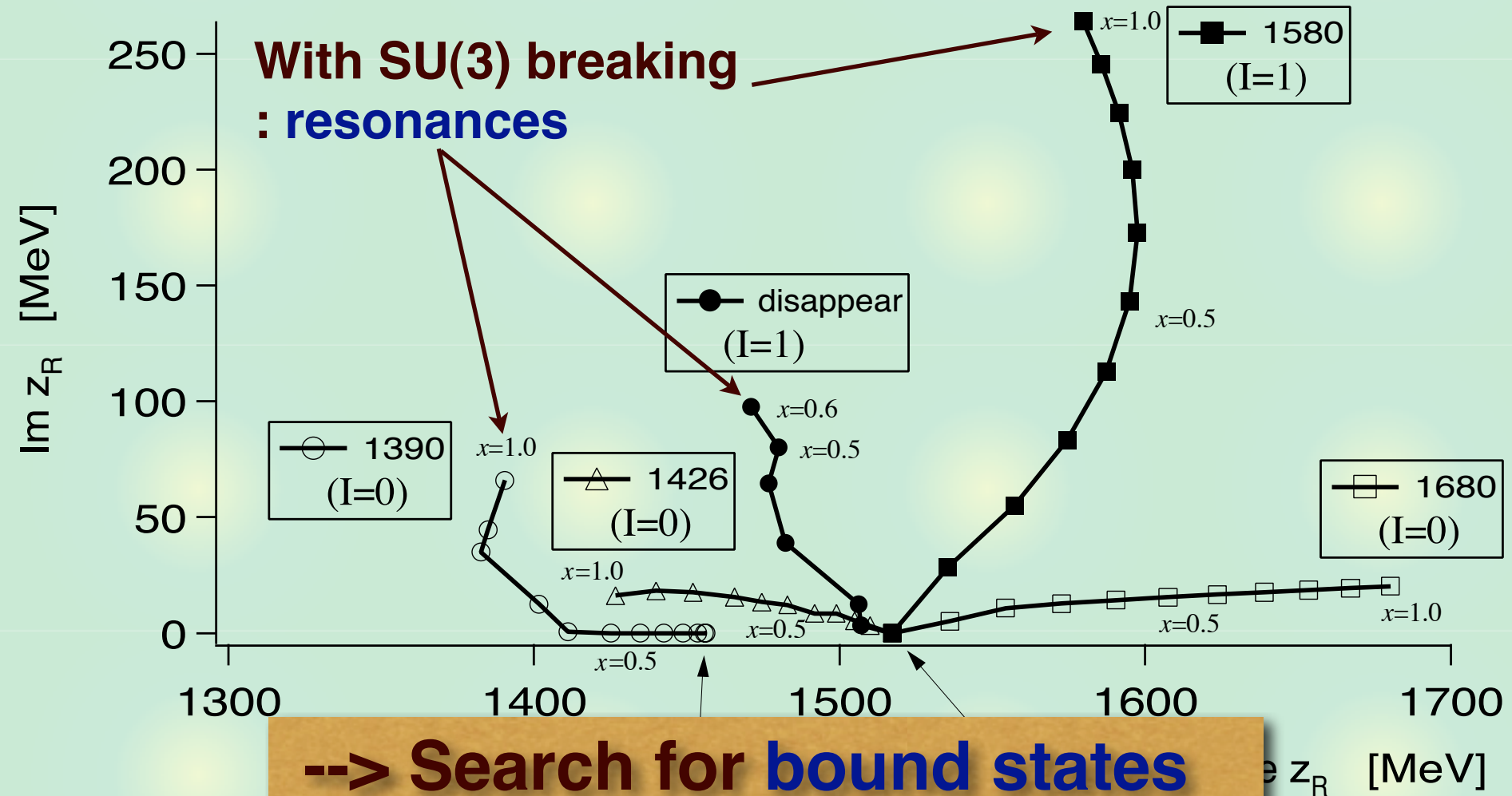
Many hadron resonances ( $\Lambda(1405)$ ,  $N(1535)$ ,  $\Lambda(1520)$ ,  $D_s(2317)$ ,... ) are well described.

What about exotic hadrons?

# Origin of the resonances

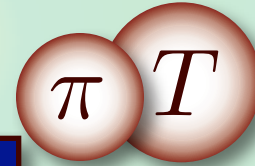
## Trajectory of poles

D. Jido, *et al.*, Nucl. Phys. A 723, 205 (2003)



## Outline

Hadron-NG boson bound state



## Chiral Symmetry

s-wave low energy interaction

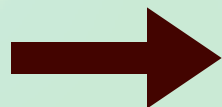
$$V_{\alpha} = -\frac{\omega}{2f^2} C_{\alpha,T} \quad C_{\text{exotic}} = 1$$

## Scattering theory

Critical strength for a bound state

$$C_{\text{crit}} = \frac{2f^2}{m[-G(M_T + m)]}$$

physical values :  $C_{\text{exotic}} < C_{\text{crit}}$



**No exotic state exists.**

## Low energy s-wave interaction

### Scattering of a target (T) with the pion (Ad)

$$\alpha \left[ \begin{array}{c} \text{Ad}(q) \\ T(p) \end{array} \right] \begin{array}{c} \text{---} \blacktriangle \text{---} \\ \text{---} \blacktriangle \text{---} \\ \text{---} \blacktriangle \text{---} \\ \bullet \\ \text{---} \blacktriangle \text{---} \\ \text{---} \blacktriangle \text{---} \end{array} = \frac{1}{f^2} \frac{p \cdot q}{2M_T} \langle \mathbf{F}_T \cdot \mathbf{F}_{\text{Ad}} \rangle_\alpha + \mathcal{O} \left( (m/M_T)^2 \right)$$

### s-wave : Weinberg-Tomozawa term

$$V_\alpha = -\frac{\omega}{2f^2} C_{\alpha,T}$$

$$C_{\alpha,T} \equiv -\langle 2\mathbf{F}_T \cdot \mathbf{F}_{\text{Ad}} \rangle_\alpha = C_2(T) - C_2(\alpha) + 3 \quad (\text{for } N_f = 3)$$

### Coupling : pion decay constant

### model-independent interaction at low energy

Y. Tomozawa, *Nuovo Cim.* 46A, 707 (1966)

S. Weinberg, *Phys. Rev. Lett.* 17, 616 (1966)

## Coupling strengths : Examples

### Coupling strengths : (positive is attractive)

$$C_{\alpha,T} = C_2(T) - C_2(\alpha) + 3$$

$\alpha$	1	8	10	$\overline{10}$	27	35
$T = \mathbf{8}(N, \Lambda, \Sigma, \Xi)$	6	3	0	0	-2	
$T = \mathbf{10}(\Delta, \Sigma^*, \Xi^*, \Omega)$		6	3		1	-3

$\alpha$	$\overline{3}$	6	$\overline{15}$	24
$T = \overline{\mathbf{3}}(\Lambda_c, \Xi_c)$	3	1	-1	
$T = \mathbf{6}(\Sigma_c, \Xi_c^*, \Omega_c)$	5	3	1	-2

- **Exotic channels** : mostly repulsive
- **Attractive interaction** : **C = 1**



## Coupling strengths : General expression

For a general target  $T = [p, q]$

$\alpha \in [p, q] \otimes [1, 1]$	$C_{\alpha, T}$	sign
$[p + 1, q + 1]$	$-p - q$	<b>repulsive</b>
$[p + 2, q - 1]$	$1 - p$	
$[p - 1, q + 2]$	$1 - q$	
$[p, q]$	$3$	<b>attractive</b>
$[p, q]$	$3$	<b>attractive</b>
$[p + 1, q - 2]$	$3 + q$	<b>attractive</b>
$[p - 2, q + 1]$	$3 + p$	<b>attractive</b>
$[p - 1, q - 1]$	$4 + p + q$	<b>attractive</b>

- **Strength should be integer.**
- **Sign is determined for most cases.**

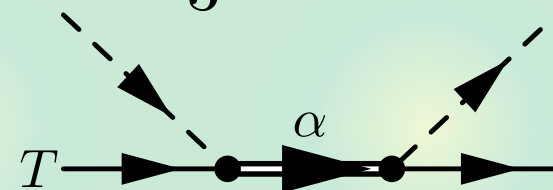
## Exotic channels

**Exoticness : minimal number of extra  $\bar{q}q$ .**

$$E = \epsilon\theta(\epsilon) + \nu\theta(\nu) \quad \epsilon \equiv \frac{p+2q}{3} - B, \quad \nu \equiv \frac{p-q}{3} - B$$

$\Delta E = E_\alpha - E_T = +1$  is realized when

○  $\alpha = [p+1, q+1] : C_{\alpha,T} = -p - q$   
repulsive



○  $\alpha = [p+2, q-1] : C_{\alpha,T} = 1 - p$

attraction :  $p = 0$  then  $\nu_T \geq 0 \rightarrow B \geq -q/3$   
not considered here

○  $\alpha = [p-1, q+2] : C_{\alpha,T} = 1 - q$

attraction :  $q = 0$  then  $\nu_T \leq 0 \rightarrow B \geq p/3$  OK!

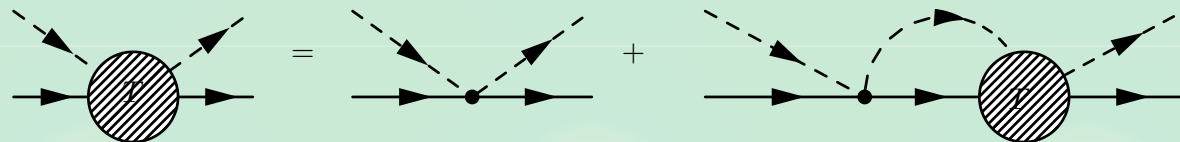
**Universal attraction for more “exotic” channel**

$$C_{\text{exotic}} = 1 \quad \text{for} \quad T = [p, 0], \quad \alpha = [p-1, 2]$$

# Renormalization and bound states

Solve the scattering problem with  $V_\alpha = -\frac{\omega}{2f^2} C_{\alpha,T}$

$$T = \frac{1}{1 - VG} V$$



**Unitarity : OK**

**Renormalization parameter : condition**

$$G(\mu) = 0, \quad \Leftrightarrow \quad T(\mu) = V(\mu) \quad \text{at} \quad \mu = M_T$$

**K. Igi, and K. Hikasa, Phys. Rev. D59, 034005 (1999)**

**M.F.M. Lutz, and E. Kolomeitsev, Nucl. Phys. A700, 193-308 (2002)**

**Scale at which ChPT works.**

**Matching with the u-channel amplitude : OK**

**Bound state:**

$$1 - V(M_b)G(M_b) = 0 \quad M_T < M_b < M_T + m$$

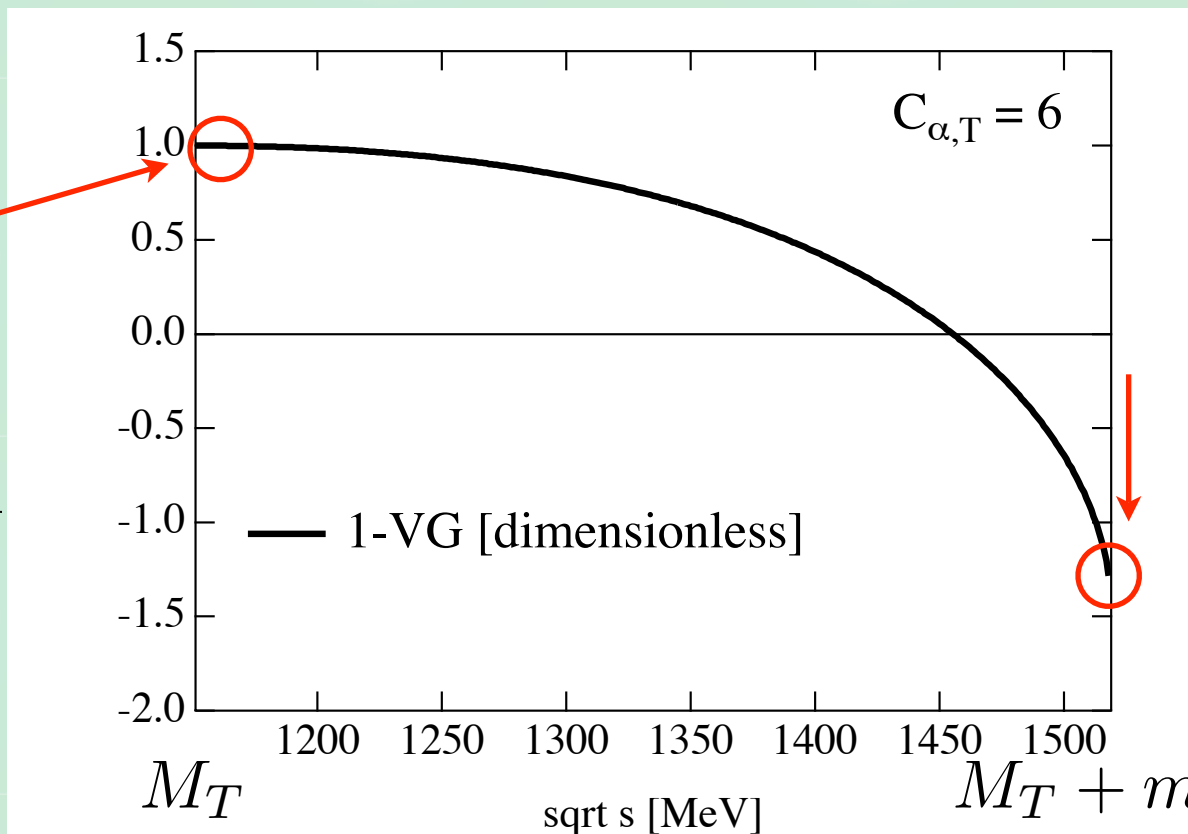
# Critical attraction

$1 - V(\sqrt{s})G(\sqrt{s})$  : monotonically decreasing.

**Fixed**

$$G(M_T) = 0$$

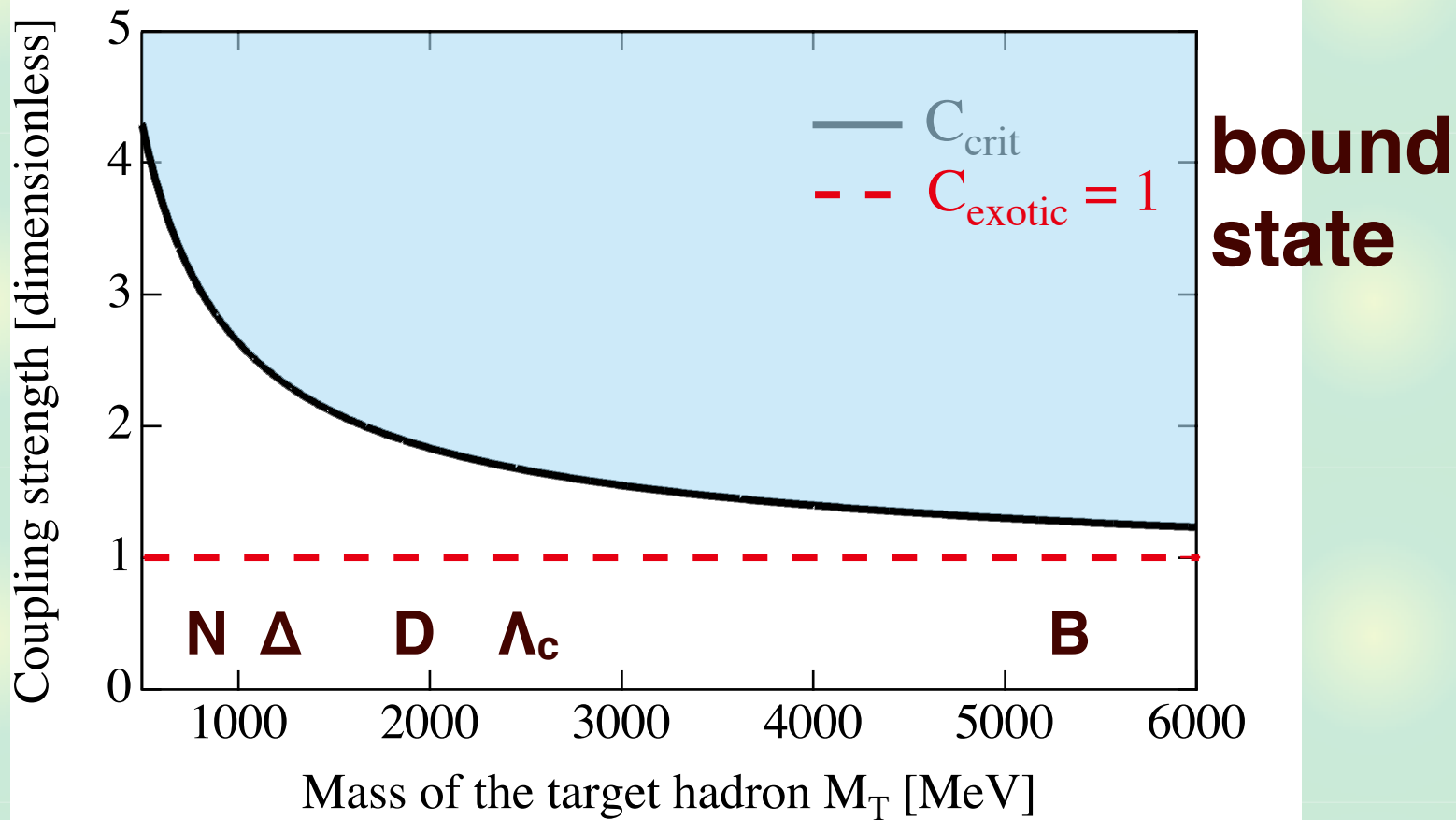
$$1 - VG = 1$$



**Critical attraction** :  $1 - VG = 0$  at  $\sqrt{s} = M_T + m$

$$\longrightarrow C_{\text{crit}} = \frac{2f^2}{m[-G(M_T + m)]}$$

# Critical attraction and exotic channel



$$m = 368 \text{ MeV and } f = 93 \text{ MeV}$$

**➔ Strength is not enough.**

## Summary 1 : SU(3) limit




We study the exotic bound states in s-wave chiral dynamics in flavor SU(3) limit.

- The interaction in exotic channels is in most cases **repulsive**.
- There are **attractive interactions** in exotic channels, with **universal** and the smallest strength :  $C_{\text{exotic}} = 1$
- The strength is **not enough** to generate a bound state :  $C_{\text{exotic}} < C_{\text{crit}}$

The result is **model independent** as far as we respect chiral symmetry.

## Summary 2 : Physical world

### Caution!

-  The exotic hadrons here are the **s-wave** meson-hadron molecule states ( $1/2^-$  for  $\Theta^+$ ).
-  We do not exclude the exotics which have **other origins** (genuine quark state, soliton rotation,...).
-  In practice, **SU(3) breaking** effect, **higher order** terms,...

In Nature, it is **difficult** to generate exotic hadrons as in the same way with  $\Lambda(1405)$ ,  $\Lambda(1520)$ ,... based on chiral interaction.

[T. Hyodo, D. Jido, A. Hosaka, Phys. Rev. Lett. 97, 192002 \(2006\)](#)

[T. Hyodo, D. Jido, A. Hosaka, Phys. Rev. D 75, 034002 \(2007\)](#)